

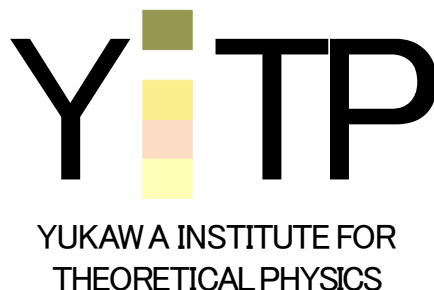
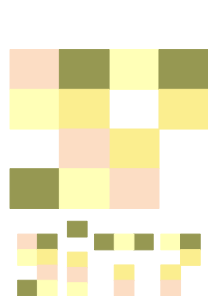
# ブラックホール磁場中性子星連星合体 の数値相対論シミュレーション

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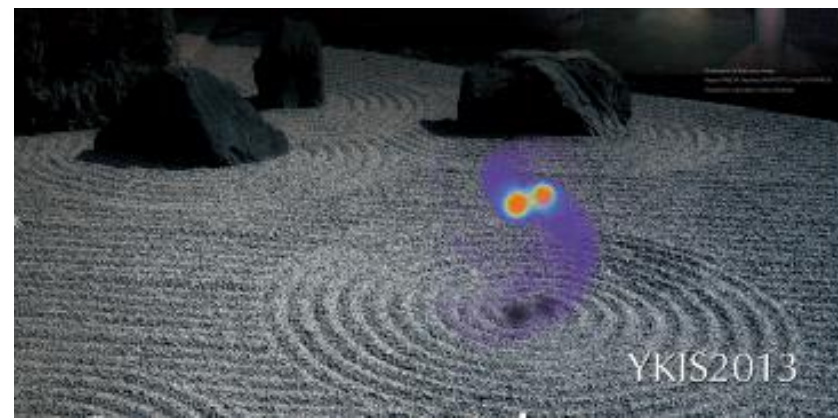
Kiuchi et al. 15, submitted on last Monday



# Motivation

1. Gravitational waves = Ripples of the space-time

- ▶ Verification of GR
- ▶ The EOS of neutron star matter
- ▶ The central engine of Short Gamma Ray Burst
- ▶ ~10 events / yr for adv. LIGO (KAGRA will be in operation in 2018)



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2. A possible site of the r-process synthesis

A significant amount of neutron star matter could be ejected from BH-NS mergers ;  $M_{\text{eje}} \approx 10^{-6} - 10^{-1} M_{\odot}$  (Kyutoku et al. 15)

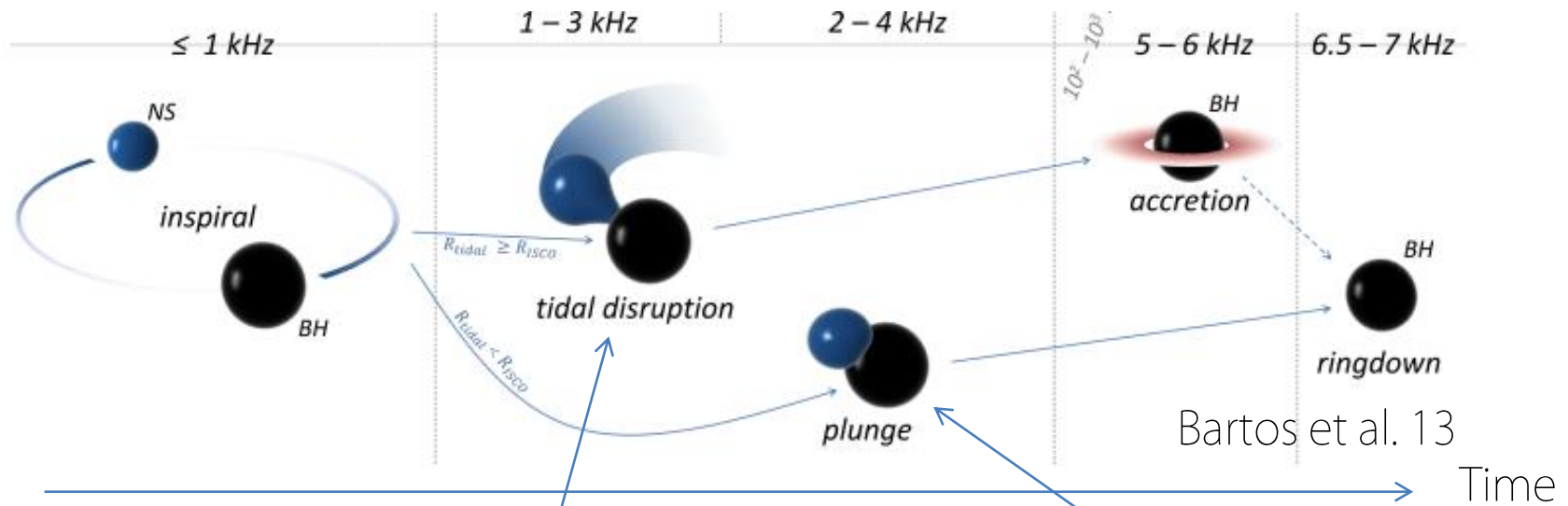
Nuclear synthesis in the ejecta (Lattimer & Schramm 74)

⇒ Radio active decay of the r-process elements (Li-Paczynski 98)

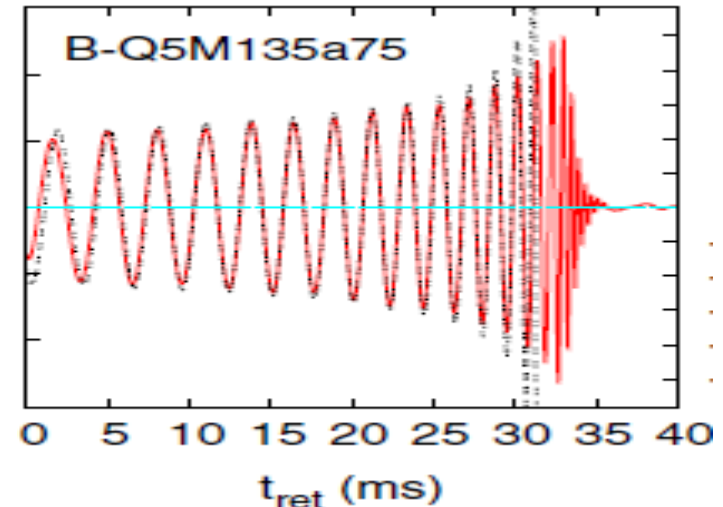
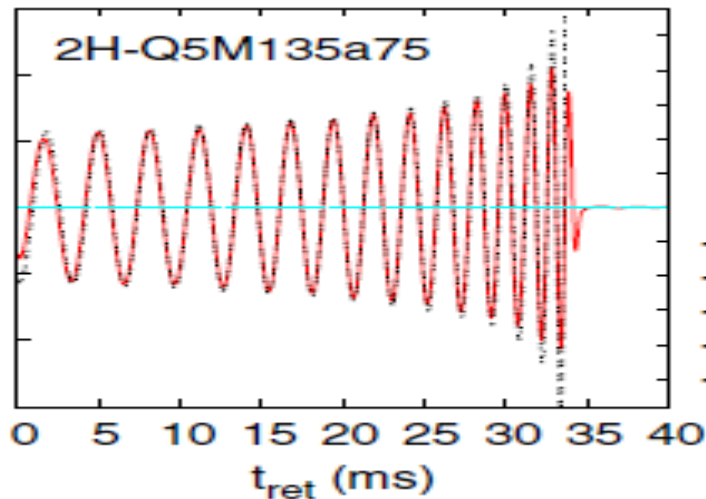
Electromagnetic counterpart = kilonova/macronova (Kulkarni 05, Metzger & Berger 12, Kasen et al. 13, Barnes & Kasen 13, Tanaka & Hotokezaka 13, Berger et al. 13, Tanvir et al. 13, Takami et al. 14, Kisaka et al. 15)

# Overview of Black Hole (BH) – Neutron Star (NS) merger

Q: Tidal disruption or not ? (Mass ratio, BH spin, EOS of NS)



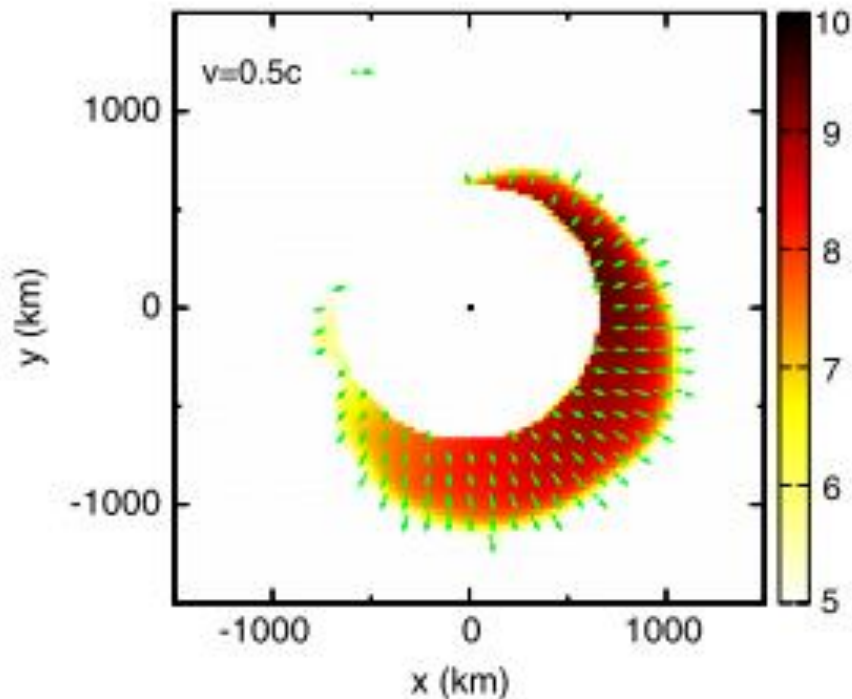
GW forms (Kyutoku et al. 11) \*More detailed classification



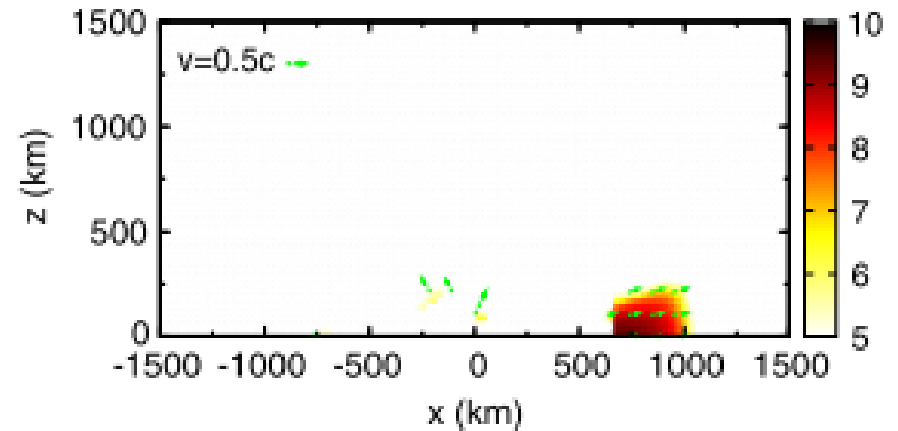
# Mass ejection due to tidal torque (Kyutoku et al. 13, Kyutoku et al. 15)

A part of the tidal tail  $\Rightarrow$  Crescent like shape of the ejecta

$\rho_{\text{eje}}$  on the orbital plane  $\text{Log}[\rho \text{ (g/cc)}]$



$\rho_{\text{eje}}$  on the meridional plane



This dynamical ejecta is a primary component in BH-NS mergers.

# What's else ?

- Neutrino driven wind (Qian & Woosley 96)

$$\dot{M} \approx 4.5 \times 10^{-3} L_{\bar{\nu}_e, 53}^{5/3} \epsilon_{\bar{\nu}_e, 10}^{10/3} R_6^{5/3} M_{2.7}^{-2} M_{\odot} / \text{s},$$

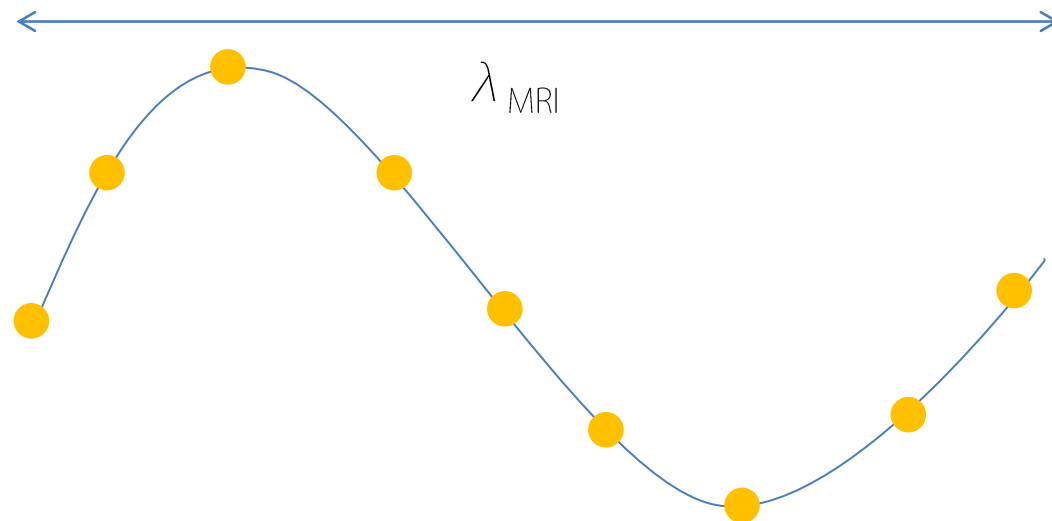
- Disk wind due to the nuclear recombination/viscous heating (Fernandez & Metzger 13)

$M_{\text{ej}} \sim 0.1 M_{\text{disk}}$  for the viscous timescale (e.g.,  $O(1)\text{s}$ )

- **Magnetic-field effect** (Liu et al. 08, Etienne et al. 12a, 12b, Paschalidis et al 14)

But, the role of the B-fields is still unclear during the merge.  
Why ? Because the wavelength of the unstable mode is too short.

What if you miss it ?  
 $\Rightarrow$  **Turbulence** is not developed .



## Difficulty in MHD simulation

- ▶ A short wavelength mode has a high growth rate.
- ▶ Turbulent eddies are killed by a numerical viscosity.

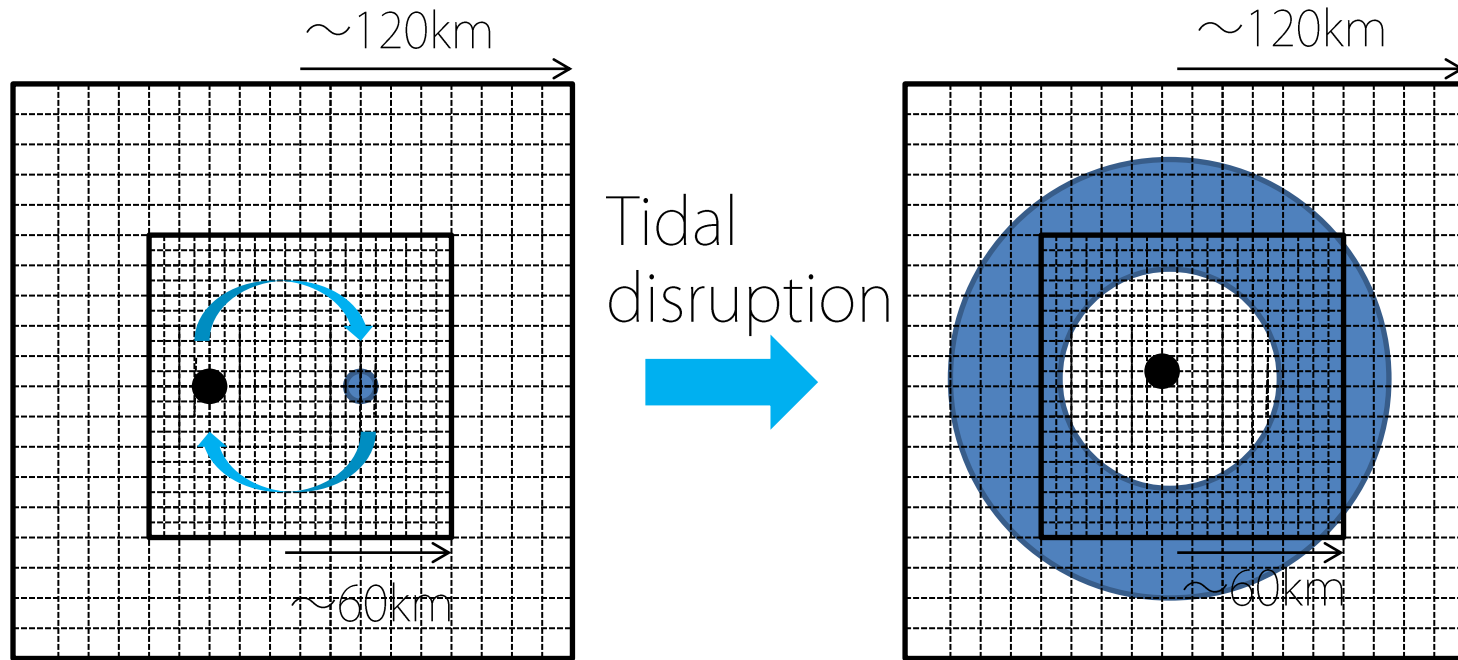
Mandatory to do an in-depth resolution study, which is lacking in a bunch of the simulations .

- ▶ High resolution ;  $\Delta x = 120\text{m}$ ,  $N = 1028^3$  (K ; 32,768 cores)
  - ▶ Middle resolution ;  $\Delta x = 160\text{m}$ ,  $N = 756^3$  (XC30 ; 4,096 cores)
  - ▶ Normal resolution ;  $\Delta x = 202\text{m}$ ,  $N = 612^3$  (XC30 ; 4,096 cores)
  - ▶ Low resolution ;  $\Delta x = 270\text{m}$ ,  $N = 448^3$  (FX10 ; 3,456 cores)
- c.f. highest-res. in BH-magnetized NS simulation is  $\Delta x \approx 260\text{m}$ ,  $N = 140^3$

## Fiducial model

- ▶ EOS : APR4 ( $M_{\text{max}} \approx 2.2M_{\odot}$ ),  $M_{\text{NS}} = 1.35 M_{\odot}$
- ▶  $M_{\text{BH}}/M_{\text{NS}} : 4$
- ▶ BH spin : 0.75
- ▶  $B_{\text{max}} : 10^{15}\text{G}$

# Outline of numerical relativity-MHD code (Kiuchi et al. 12, 14)



- ▶ Time step is limited by the speed of light
- ▶ Interpolation of B-fields on the refinement boundary is non-trivial : Flux conservation and  $\text{Div } \mathbf{B} = 0$  (KK et al. 12, Balsara 01)
- ▶ Larger B/F
- ▶ MPI communication rule is complicated, e.g., refinement boundary
- ▶ Good scaling up to about 80,000 cores (Execution performance 12-13%)

# Japanese supercomputer K @ AICS

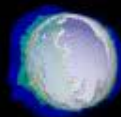


► Total peak efficiency is 10.6 PFLOPS (663,552 cores)

This study is one of the main subject of the HPCI strategic program field 5.



$t = 0.2270 \text{ ms}$



$10^{12} \text{ g/cm}^3$

$10^{11} \text{ g/cm}^3$

$10^{10} \text{ g/cm}^3$

$10^9 \text{ g/cm}^3$

$t = 0.0000$  ms



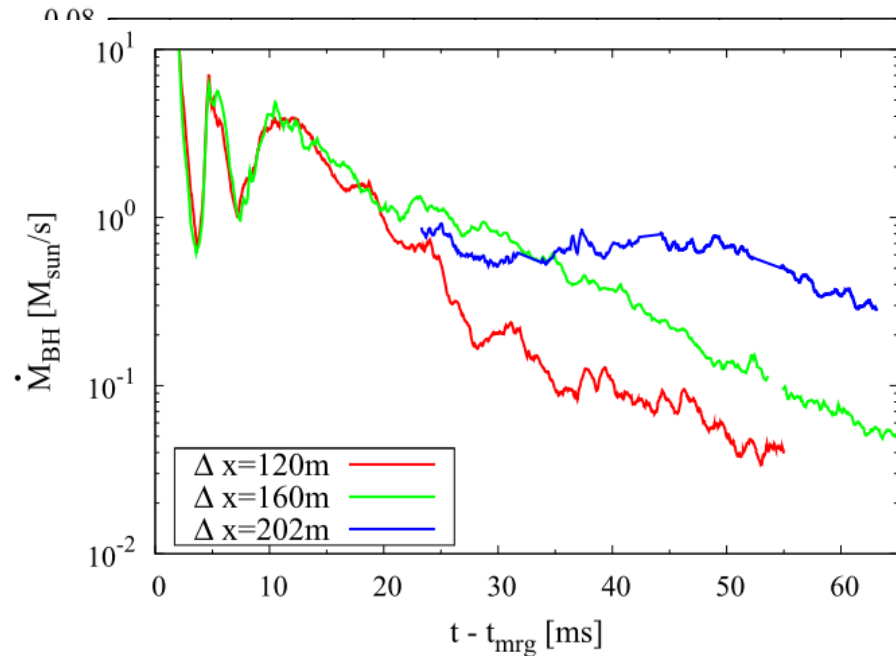
$10^{14.0}$  G

$10^{14.5}$  G

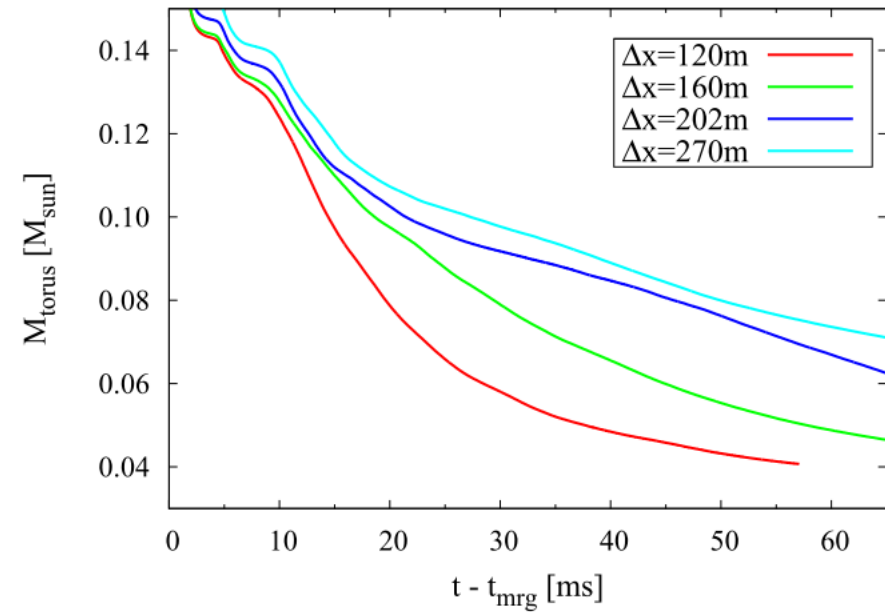
$10^{15.0}$  G

# Mass ejection

Mass accretion rate evolution



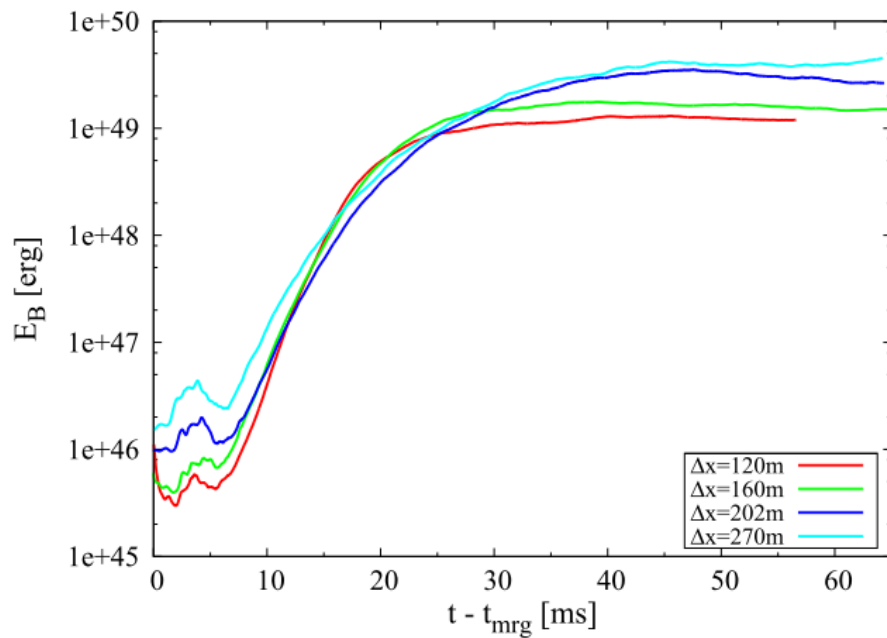
Torus mass evolution



- ▶  $t \lesssim 10\text{ms} \Rightarrow$  Dynamical mass ejection (Kyutoku et al. 15)
  - ▶  $10\text{ms} \lesssim t \Rightarrow$  New component = torus wind
  - ▶ Mass accretion onto the BH for 10-20ms  $\Rightarrow \approx 0.02M_{\odot}$
  - ▶ Disk mass decreases by  $\approx 0.05M_{\odot}$  for 10-20ms
- In the higher-resolution run,
- ▶ The launch time  $\Rightarrow$  earlier, The amount of the wind  $\Rightarrow$  larger, The mass accretion rate  $\Rightarrow$  smaller in the higher-res. runs.

# B-field amplification

## Evolution of B-field energy



Magneto Rotational Instability (MRI) (Balbus & Hawley 91);

Powerful amplification mechanism of the B-fields. If  $d\Omega/dr < 0$ , it turns on and amplifies the B-fields exponentially.

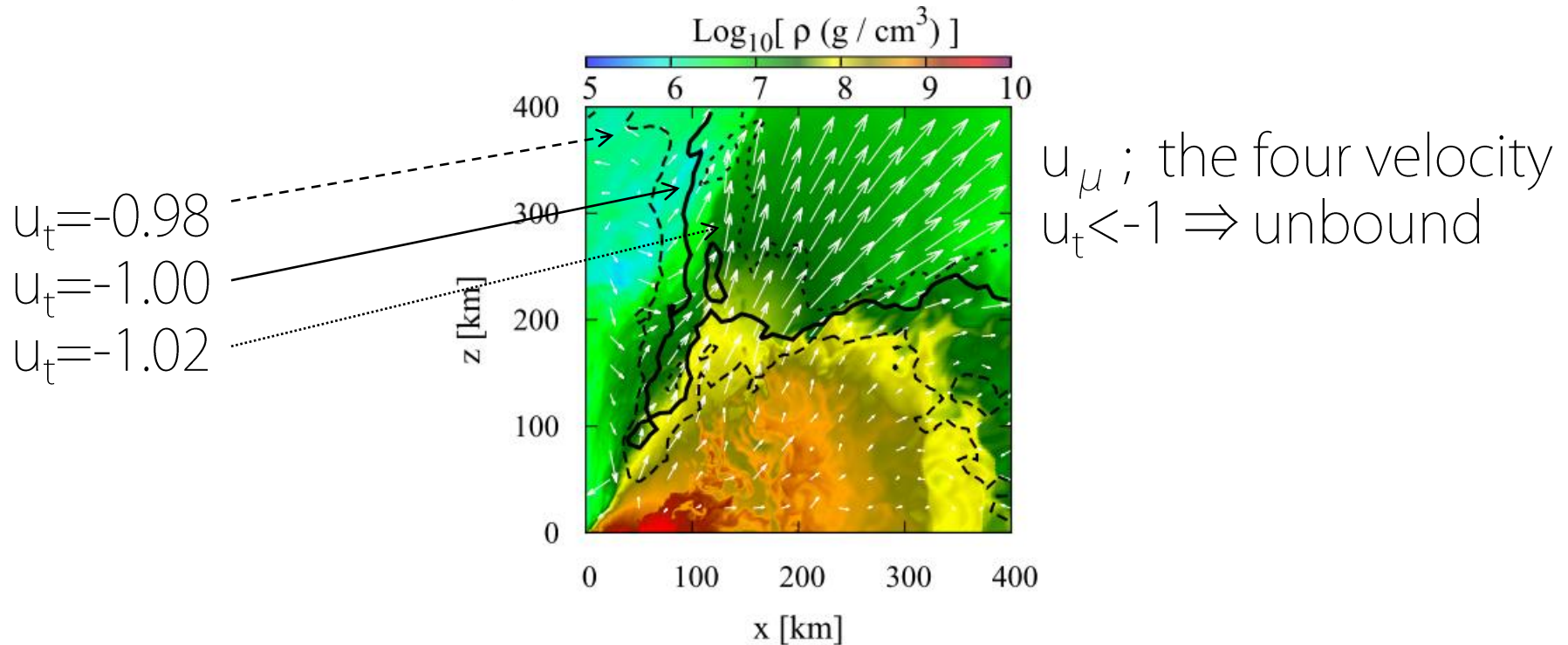
→ Turbulent eddies are produced

→ Physical viscosity

- ▶  $t \lesssim 10\text{ms} \Rightarrow$  highly dynamical phase (winding / stretching)
- ▶  $10\text{ms} \lesssim t \Rightarrow$  Magneto Rotational Instability activates ( $\lambda_{\text{MRI, fastest}} = B/(4\pi\rho)^{1/2}2\pi/\Omega$ )
- ▶ Linear growth rates are approximately converged;  $0.07-0.08\Omega$  (Non-axisymmetric MRI,  $\lambda_{\text{MRI, fastest}}/\Delta x \gtrsim 10$ )
- ▶ Well-resolved turbulent eddies might play an important role.

# Structure of the torus wind

## Density of a meridional plane at $\approx 50\text{ms}$

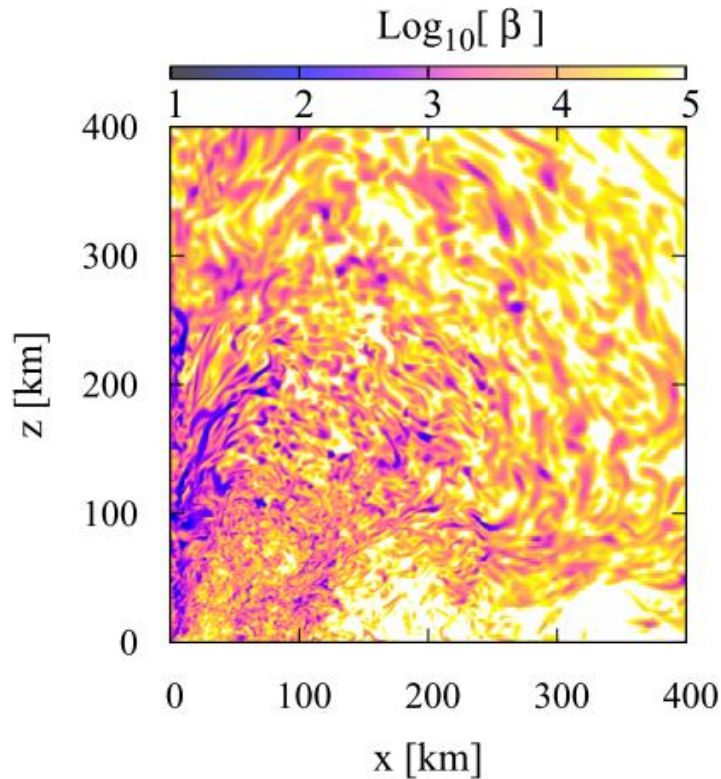


- $u_t = -1$  is approximately parabolic in the vicinity of the z-axis
- Effective potential :  $\ln(-u_t) \rightarrow -GM_{\text{BH}}/(R^2+z^2)^{1/2} + l^2/2R^2$  (constant specific angular momentum  $l$ )
- $\Rightarrow u_t = -1$  becomes parabolic (Hawley & Krolik 06, Blandford & Begelman 99)

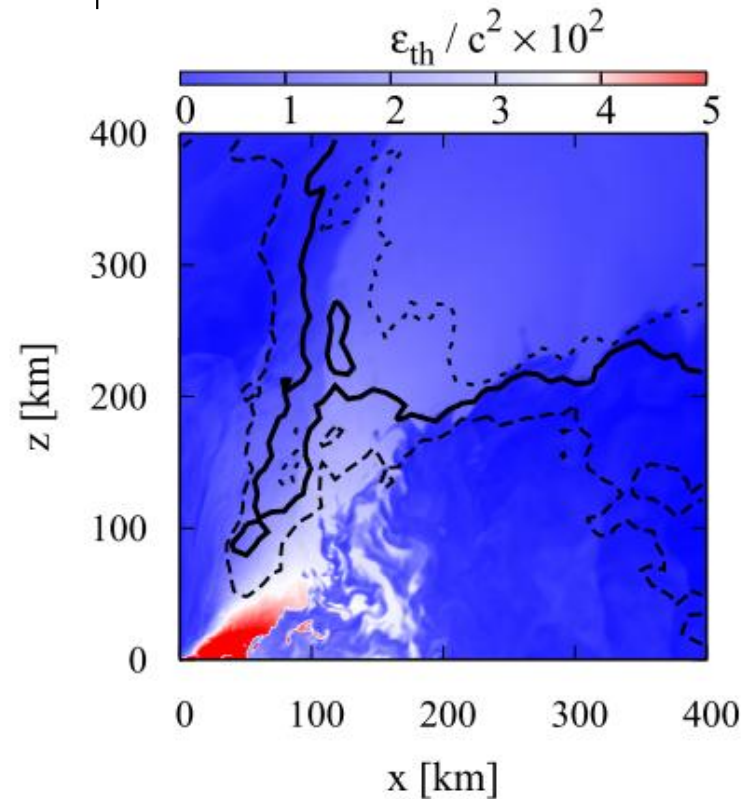
Formation of a region with  $u_t < -1$  is natural consequence for the accretion torus formation in the BH-NS mergers.

# Mechanism of the injection into a region with $u_t < -1$

$P / P_{\text{mag}}$  on a meridional plane  
at  $\approx 20\text{ms}$



Thermal component of the  
internal energy on a meridional  
plane at  $\approx 50\text{ms}$



- Magnetic pressure is not the main agent of the injection.
  - A hot region in the vicinity of the BH  $\Rightarrow$  Steep pressure gradient
- The fluid elements are accelerated radially and become unbound.

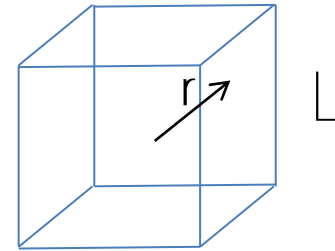
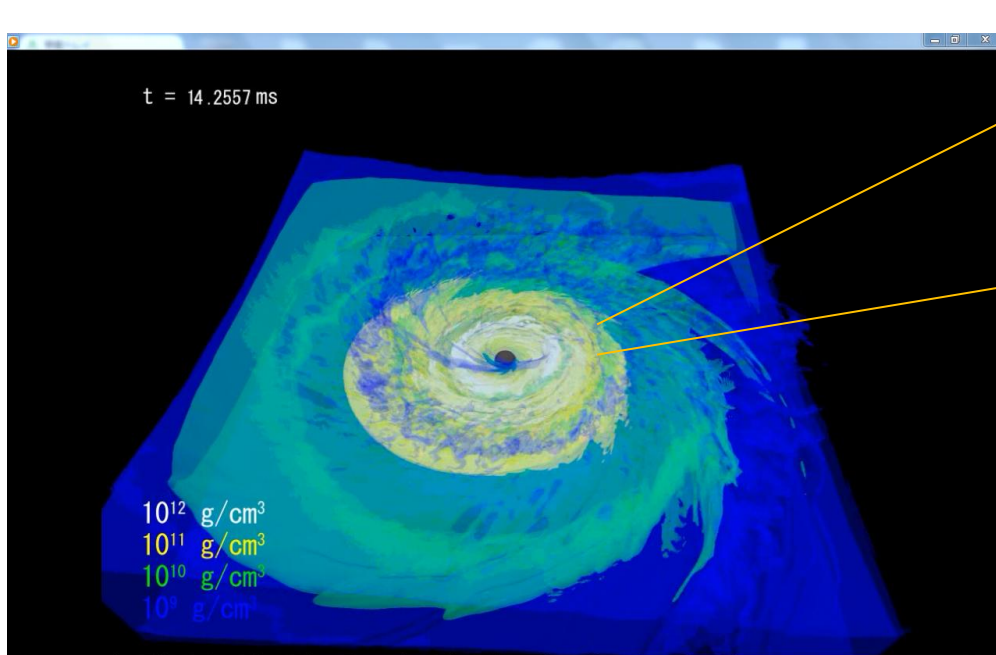
# Mechanism of the injection into a region with $u_t < -1$

- ▶ The high BH spin is a key ingredient as well.
  - ▶ Spin up  $\chi : 0.75 \Rightarrow \approx 0.90$
  - ▶ Inner Stable Circular Orbit radius  $\approx 2.32 GM_{\text{BH}}/c^2 \Rightarrow$  The accretion onto the BH is suppressed.
  - ▶ The high BH spin prevents the fluid elements from being accreted onto the BH.
- $\Rightarrow$  They tend to stay in the vicinity of the BH.
- $\Rightarrow$  Steep pressure gradient (Shibata et al. 07)

The point : high BH spin is necessary for tidal disruption of realistic BH-NS binaries (mass ratio  $\gtrsim 7$ ).

# Mechanism to enhance the thermal pressure

## Energy spectrum of the turbulent flow



Step 1. Choose a cubic region

Step 2.  $\delta v^i = v^i - \langle v^i \rangle$

$\langle \rangle$  Time average

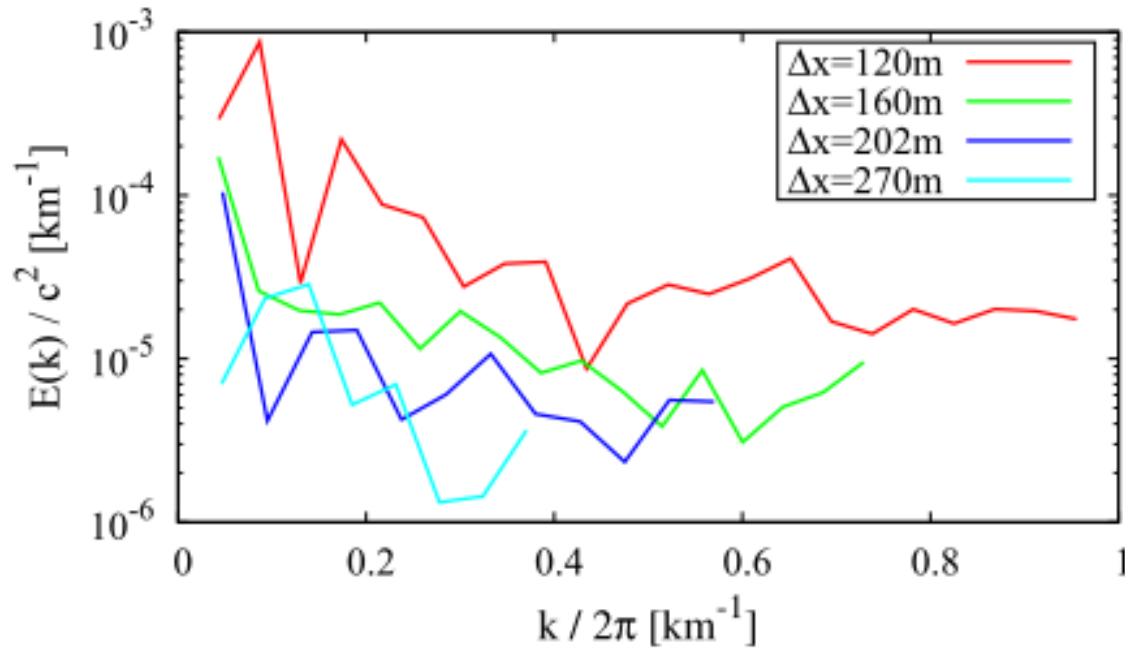
Step 3.  $R_{ij}(\mathbf{r}) = \langle \delta v^i(\mathbf{x} + \mathbf{r}) \delta v^j(\mathbf{x}) \rangle$

Step 4.  $\varphi_{ij}(\mathbf{k}) = \iiint R_{ij}(\mathbf{r}) e^{-i\mathbf{k} \cdot \mathbf{r}} d\mathbf{r}$

Step 5.  $E(k) = \iint \varphi_{ii}(\mathbf{k}) d\Omega_k$   
 $k = |\mathbf{k}|$



## Energy spectrum of the turbulent flow

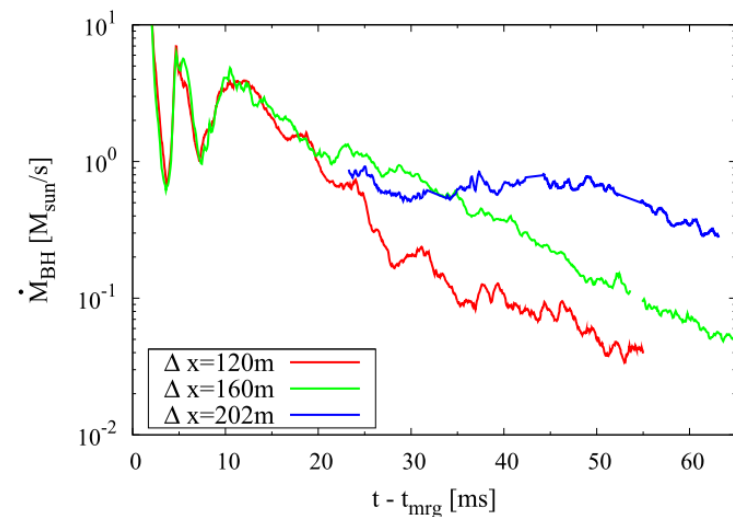
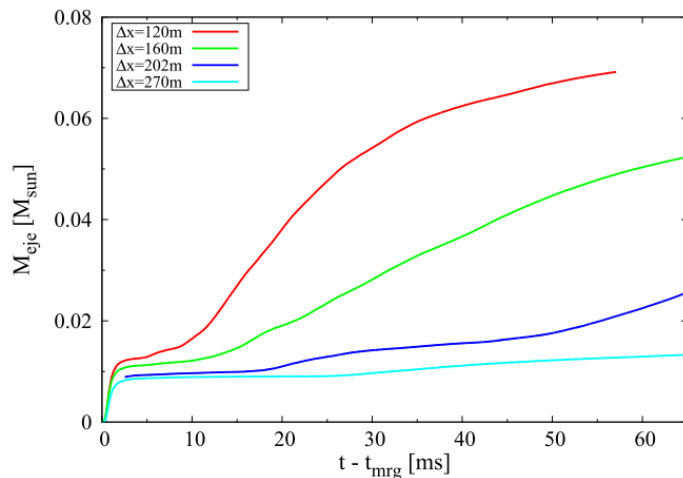
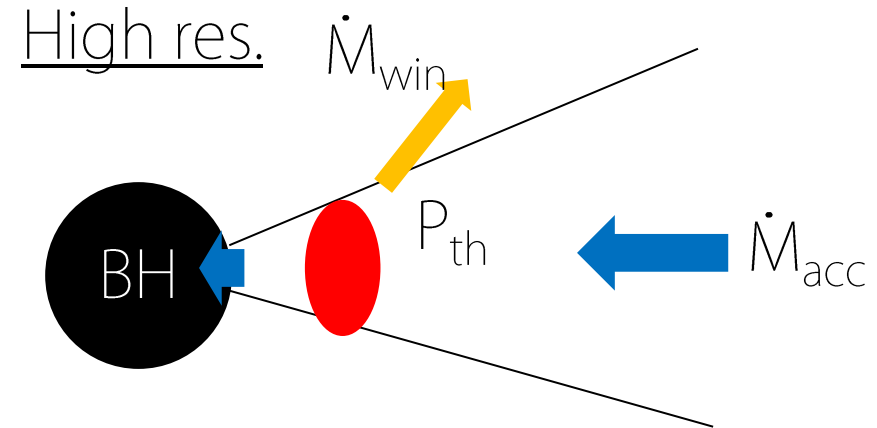
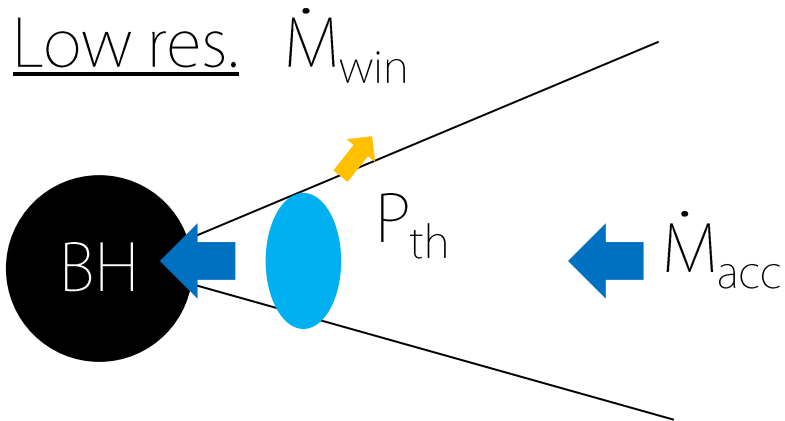


- The spectrum extends to smaller scales in the higher-res. runs  
⇒ The energy injection at a smaller scale where MRI develops.
- The spectrum amplitude is higher in the higher-res. runs.

In the turbulent state, the energy dissipation rate is  $\sim \delta v^3 / l_{\text{edd}}$   
⇒ Energy spectrum indicates the viscosity becomes higher in the higher-resolution runs.

# Mechanism to enhance the thermal pressure

- The realistic high viscosity enhances the mass accretion inside the torus and converts the mass accretion energy to thermal energy efficiently.

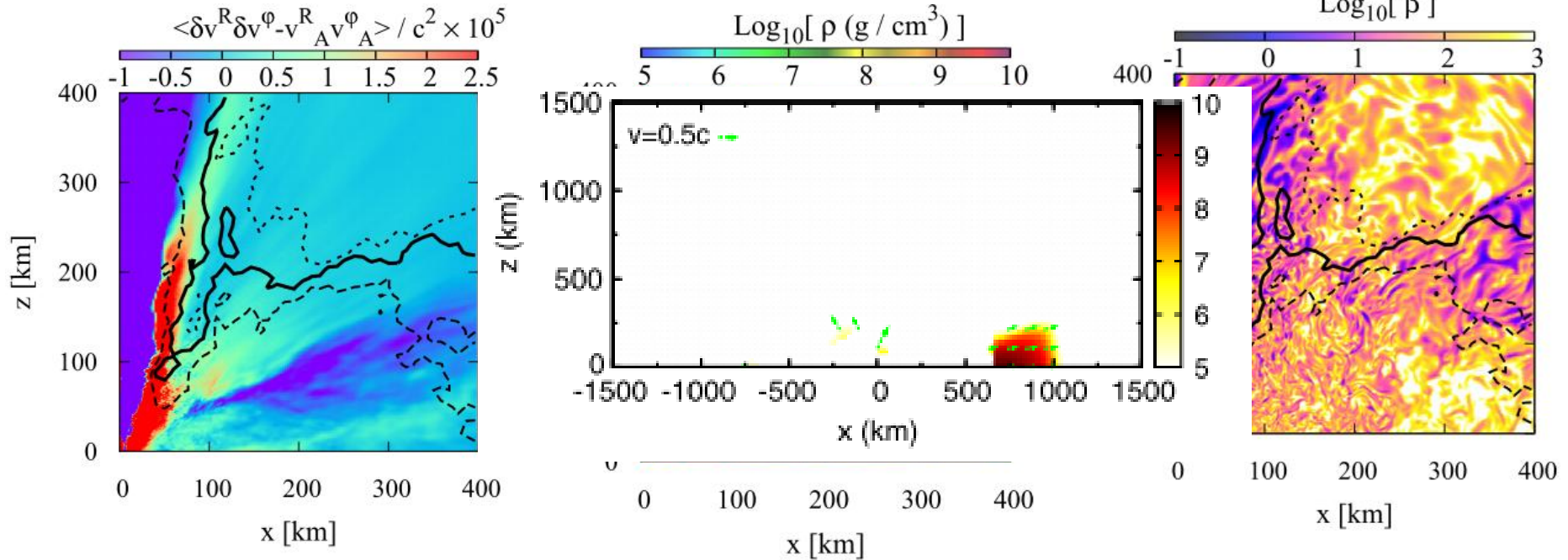


# Formation of the funnel wall and magnetosphere

Reynolds+Maxwell stress

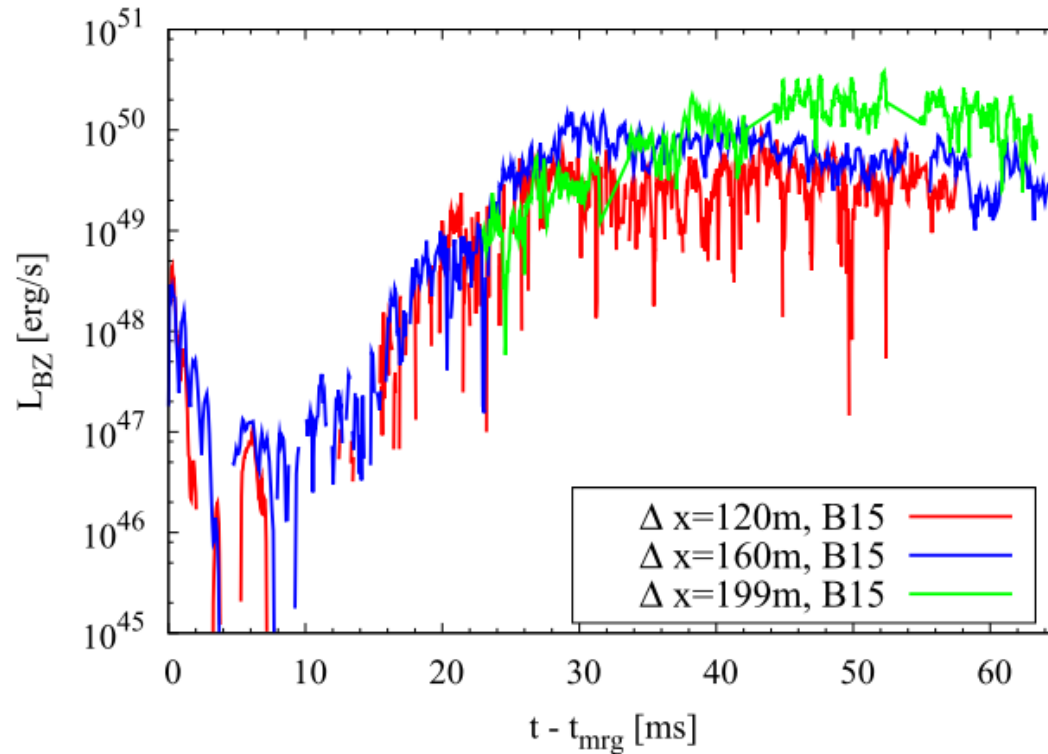
Density

$P / P_{\text{mag}}$   
 $\text{Log}_{10}[\beta]$



- Energy is transported in a region with  $u_t < -1$
- Funnel wall formation by the torus wind
- Torus wind  $\Rightarrow$  Coherent poloidal B-field  $\Rightarrow$  Formation of a low plasma beta region  $\Rightarrow$  Formation of the magnetosphere

Blandford–Znajek mechanism = Extraction of the BH rotational energy via B-fields



► Outgoing Poynting flux is as high as  $\approx 2 \times 10^{49}$  erg/s  
⇒ It could be a central engine for the SGRBs with low luminosity (Lee & Ramires-Ruiz 07)

► Jet could be naturally collimated by the funnel wall once it launches.

# Implications of the torus wind

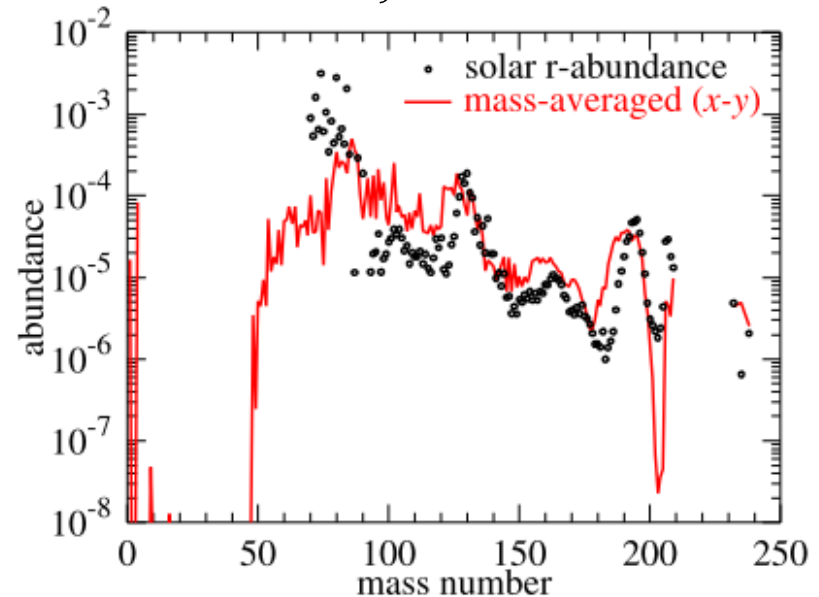
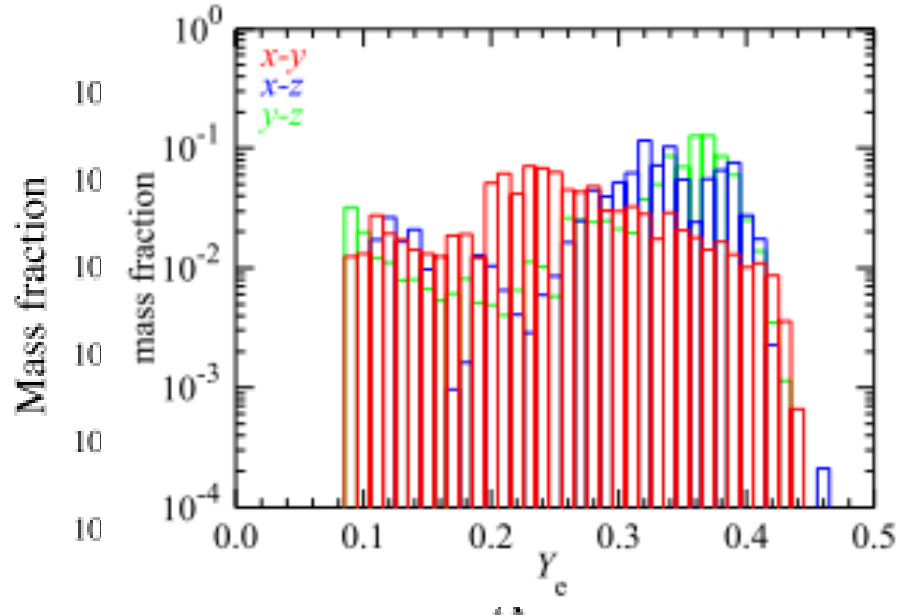
## ► Nucleosynthesis in the BH-NS merger

Electron fraction of the dynamical ejecta is  $\lesssim 0.1$

$\Rightarrow$  Reproduce the third peak of the solar abundance

Wanajo et al. 14

Wanajo et al. 14



► Torus wind is hot  $\Rightarrow$  Different Ye distribution from that for the dynamical component composed of the non-hot neutron rich matter.

► Broad distribution of the Ye could reproduce the solar abundance (BH-NS: Just et al. 15, NS-NS: Sekiguchi et al. 15, Wanajo et al. 14)

# Implications of the torus wind

Macronova/kilonova model in the BH-NS merger (Li-Paczynski 98)

- ▶ Dynamical ejecta  $\sim 10^{-6}$ - $10^{-1} M_{\odot}$  (Hotokezaka et al. 13, Kyutoku et al. 15)
- ▶ Thermal driven torus wind  $M_{\text{ej}} \sim 0.06 M_{\odot}$  ( $\sim 0.5 M_{\text{disk}}$ ),  
but only one point in the parameter spaces

Systematic study should be done.

# Caveat and summary

NR simulations of the BH-magnetized NS mergers on K

- ▶ Resolution study is essential.
- ▶ Tidal disruption  $\Rightarrow$  Accretion torus formation  $\Rightarrow$  Torus wind launch  $\Rightarrow$  Funnel wall formation  $\Rightarrow$  Magnetosphere formation in a self-consistent simulation
- ▶ Turbulent eddies are the agent to drive the mass accretion and to convert the kinetic energy to thermal energy

## Implications

- ▶ Central engine of the SGRBs
- ▶ The nucleosynthesis of the r-process elements
- ▶ The radioactively-powered transient emission