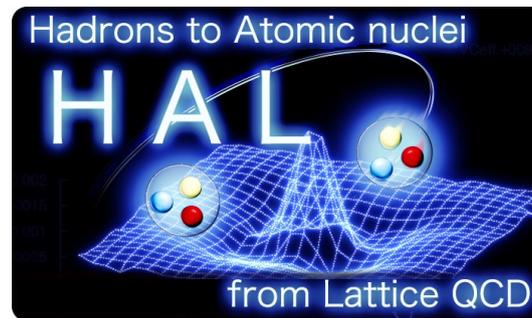


# *Dibaryon searches from lattice QCD*

Kenji Sasaki (*CCS, University of Tsukuba*)

for HAL QCD collaboration



## ***HAL** (**H**adrons to **A**tomical nuclei from **L**attice) QCD Collaboration*

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(*YITP*)

**T. Doi**  
(*RIKEN*)

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**H. Nemura**  
(*Univ. of Tsukuba*)

**T. Miyamoto**  
(*YITP*)

**T. Iritani**  
(*Stony Brook U.*)

**S. Gongyo**  
(*YITP*)

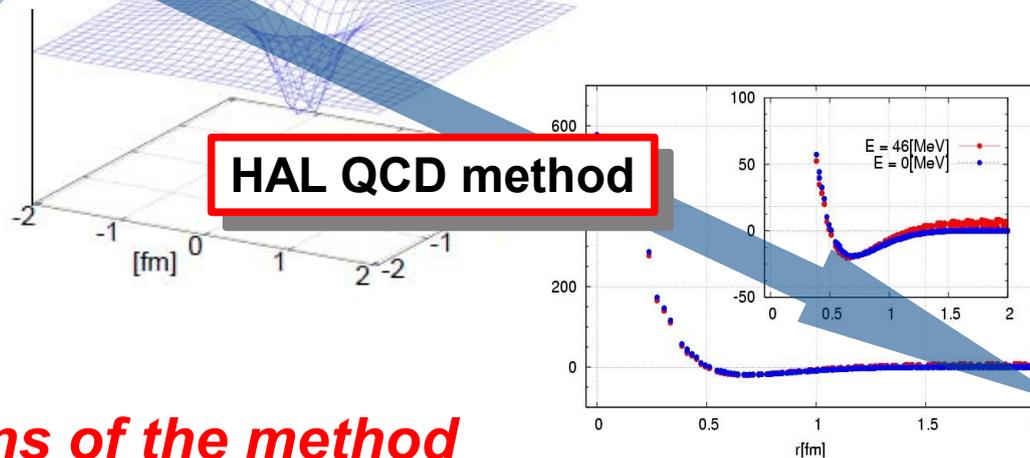
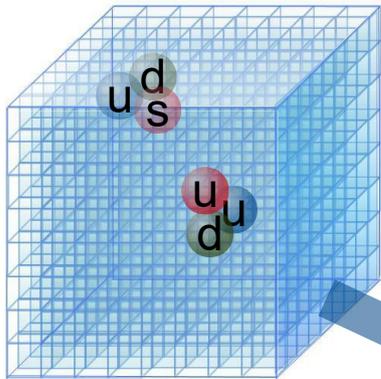
**D. Kawai**  
(*YITP*)

# *Introduction*

# Strategy of HAL QCD

## Technical improvements

- Unified Contraction Algorithm,
- Time dependent method,
- Higher partial waves,
- Finite volume method vs potential

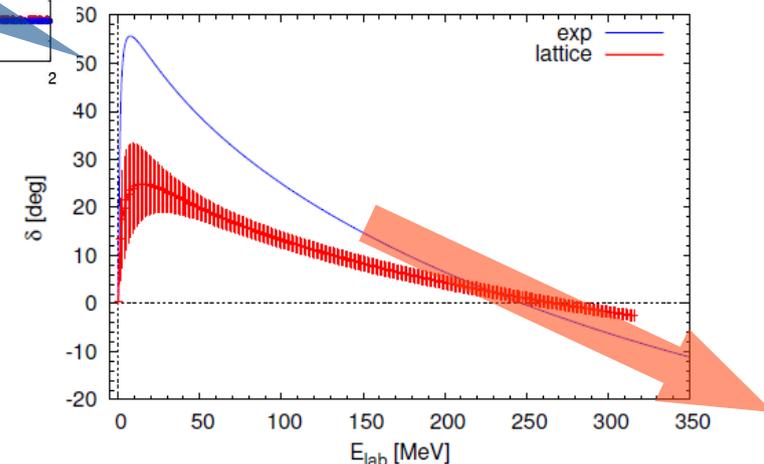


## Applications

- Few-body system
- Medium heavy system
- Neutron star EOS

## Extensions of the method

- Generalized BB interaction
- Generalized Dec-Dec interaction
- Charmed baryon system
- Meson-meson, meson-baryon system
- Three-body interaction

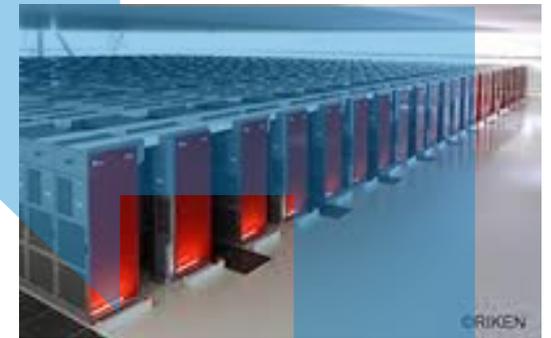


# Role of our work

Study of BB interaction and search for dibaryon state

## Experiment

- Advantageous for **less strange quarks**
- Collision experiment getting more difficult as increasing the number of strange quarks due to short lifetime of flavored quarks



Joint Project between KEK and JAEA

## Lattice QCD simulation

- Advantageous for **more strange quarks**
- Signals getting worse as increasing the number of light quarks due to suffering statistical noise.
- **Complementary role to experiment.**

**It is best to collaborate to yield a high quality BB potential**

# *Dibaryon candidates*

Some dibaryon candidates are predicted by model calculations

- **H-dibaryon**

- ▶ R.L.Jaffe PRL38(1977)

- **N- $\Omega$  system**

- ▶ F.Wang et al. PRC51(1995)

- ▶ Q.B.Li, P.N.Shen, EPJA8(2000)

- **$\Delta\Delta$  and  $\Omega\Omega$  system**

- ▶ F.J.Dyson, N-H.Xuong, PRL13(1964)

- ▶ M.Oka, K.Yazaki, PLB 90(1980)

- Predicted B.E. and structures are highly depend on the model parameters.
- Some of them are still not found in experiments.

**Lattice QCD study of hadron interactions is awaited.**

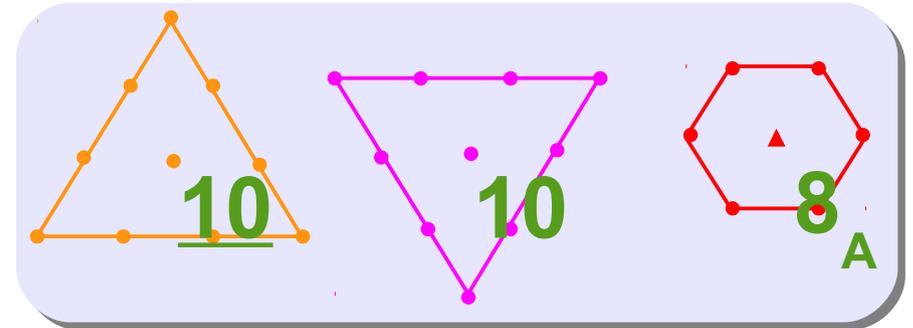
# *S=-2 BB interaction*

*--- focus on the H-dibaryon ---*

# $SU(3)$ feature of BB interaction

## SU(3) classification

$$8 \times 8 = 27 + 8_s + 1 + \underline{10} + 10 + 8_A$$



## In view of quark degrees of freedom

- Short range repulsion in BB interaction could be a result of **Pauli principle** and **color-magnetic interaction** for the quarks.
- Strengths of repulsive core in YN and YY interaction are largely depend on their flavor structures.
- For the s-wave BB system, **no repulsive core** is predicted in **flavor singlet state** which is known as **H-dibaryon** channel.

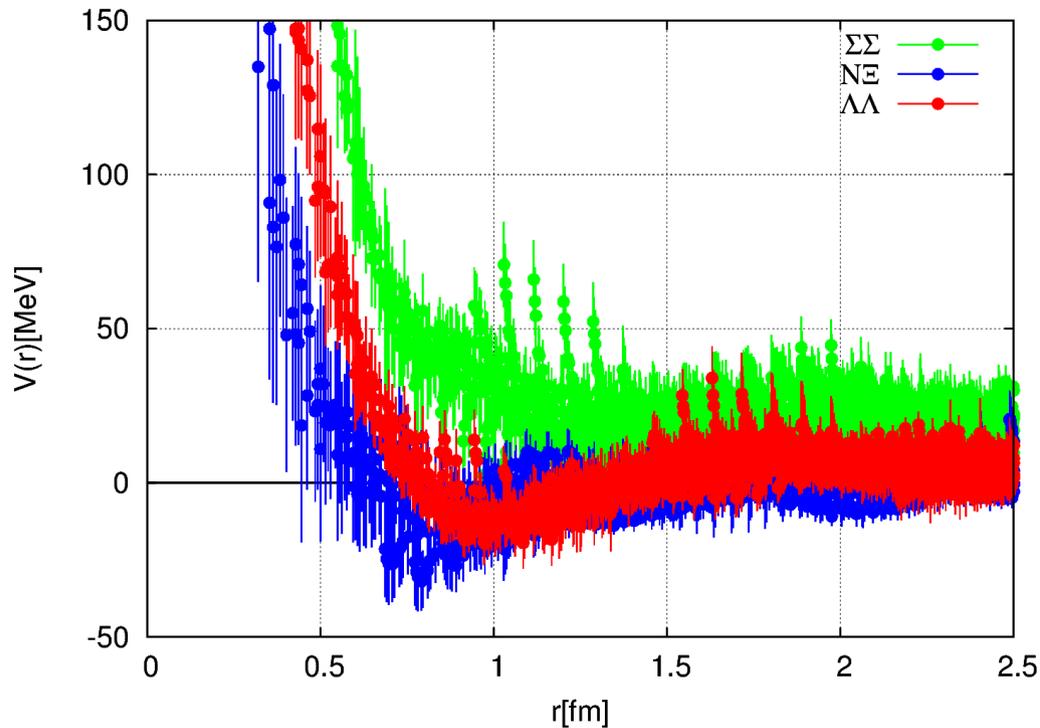
	Flavor symmetric states			Flavor anti-symmetric states		
	27	8	1	<u>10</u>	10	8
Pauli	mixed	forbidden	allowed	mixed	forbidden	mixed
CMI	repulsive	repulsive	attractive	repulsive	repulsive	repulsive

# $\Lambda\Lambda, N\Xi, \Sigma\Sigma$ ( $I=0$ ) $^1S_0$ channel near the physical point

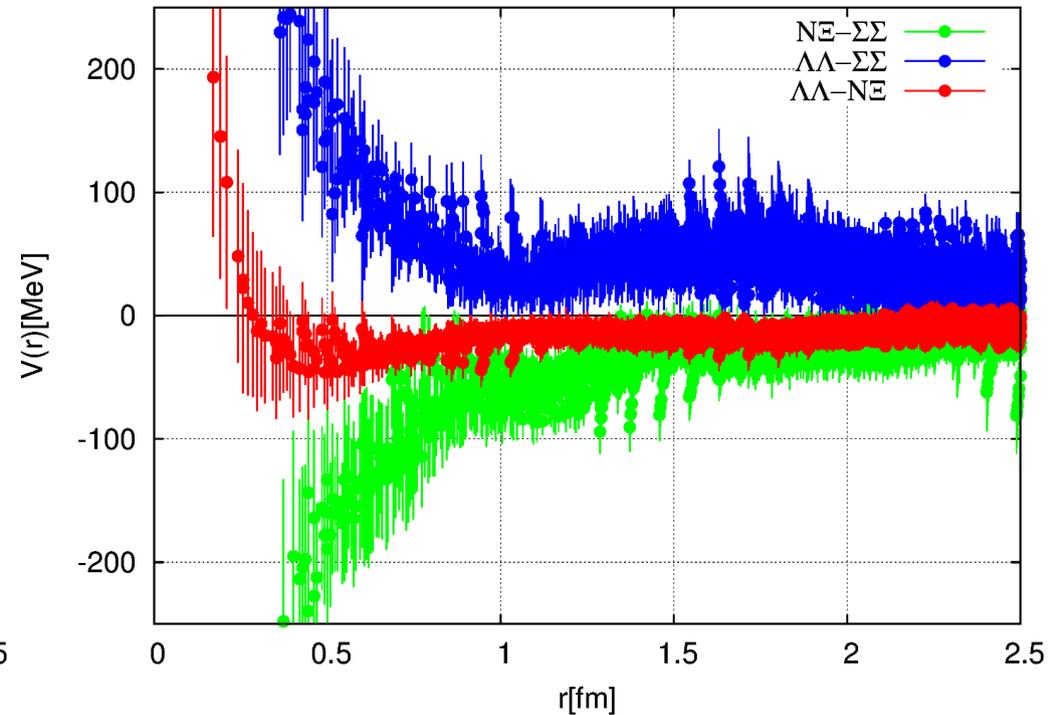
►  $N_f = 2+1$  full QCD with  $L = 8\text{fm}$ ,  $m_\pi = 145\text{ MeV}$

Preliminary!

## Diagonal elements



## Off-diagonal elements



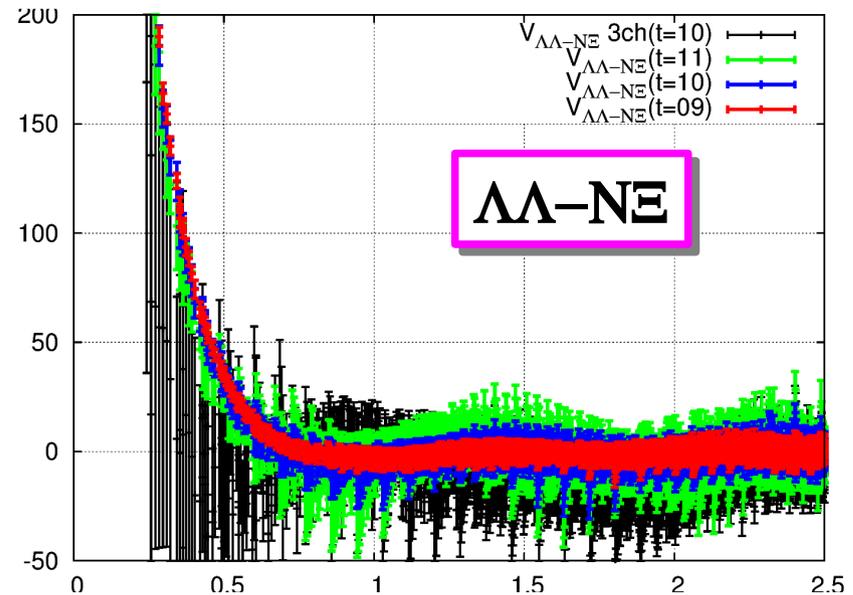
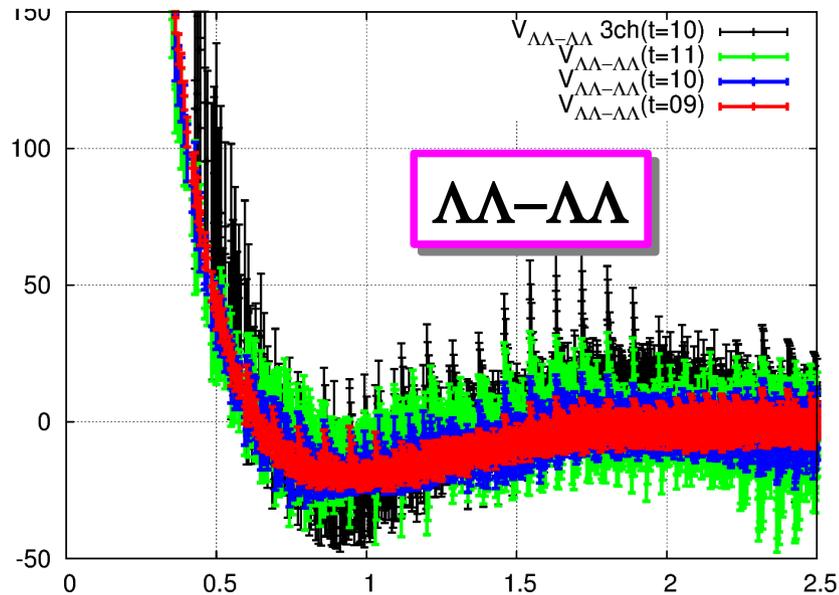
- All diagonal elements have a repulsive core.  $\Sigma\Sigma$ - $\Sigma\Sigma$  potential is strongly repulsive.
- **Diagonal  $N\Xi$  potential is more attractive than the  $\Lambda\Lambda$  potential.**
- We need more statistics to discuss physical observables through this potential.

*H-dibaryon channel (2-ch calculation)*

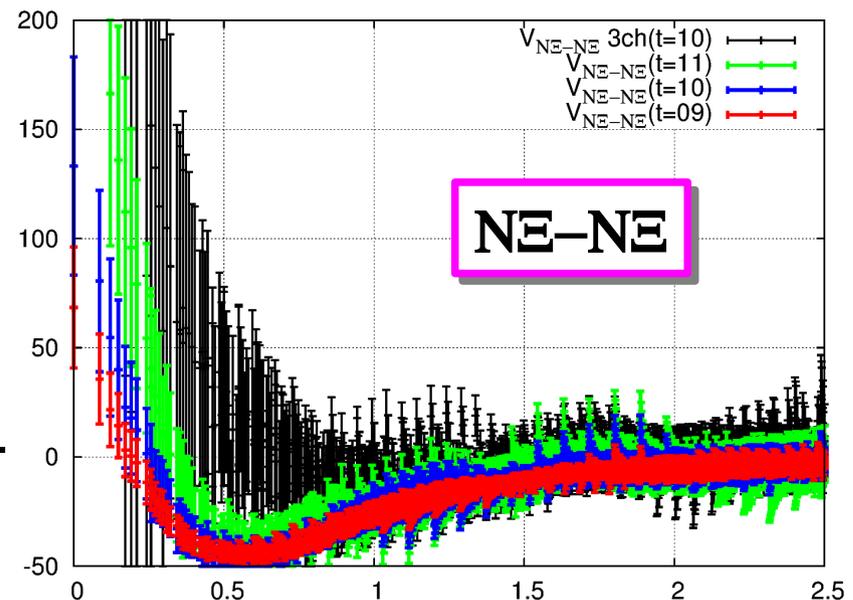
# $\Lambda\Lambda, N\Xi (I=0) ^1S_0$ potential (2ch calc.)

►  $N_f = 2+1$  full QCD with  $L = 8\text{fm}$ ,  $m_\pi = 145\text{ MeV}$

Preliminary!



- Potential calculated by only using  $\Lambda\Lambda$  and  $N\Xi$  channels
- Deviation from potential in 3ch calc. can be seen mainly in  $r < 1\text{fm}$ .
- The same scattering phase shift would be expected in low energy region.

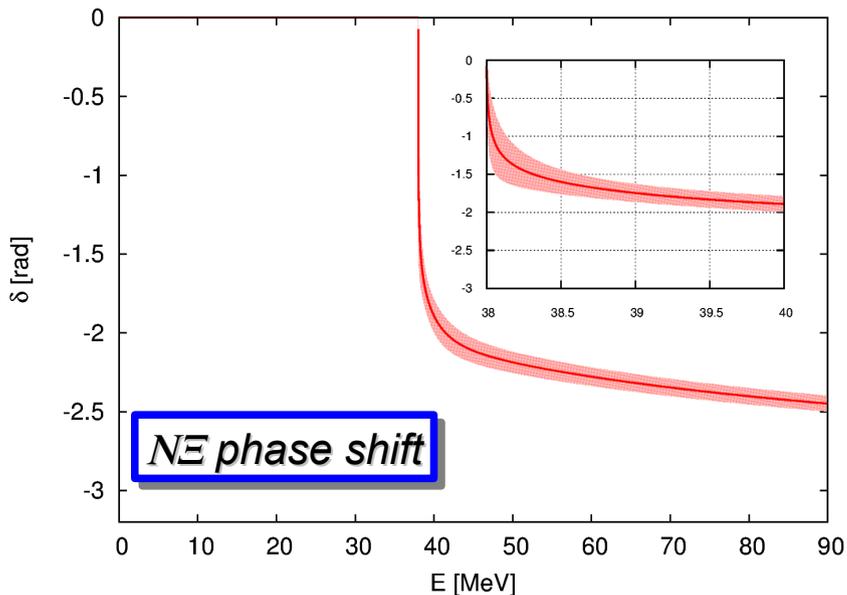
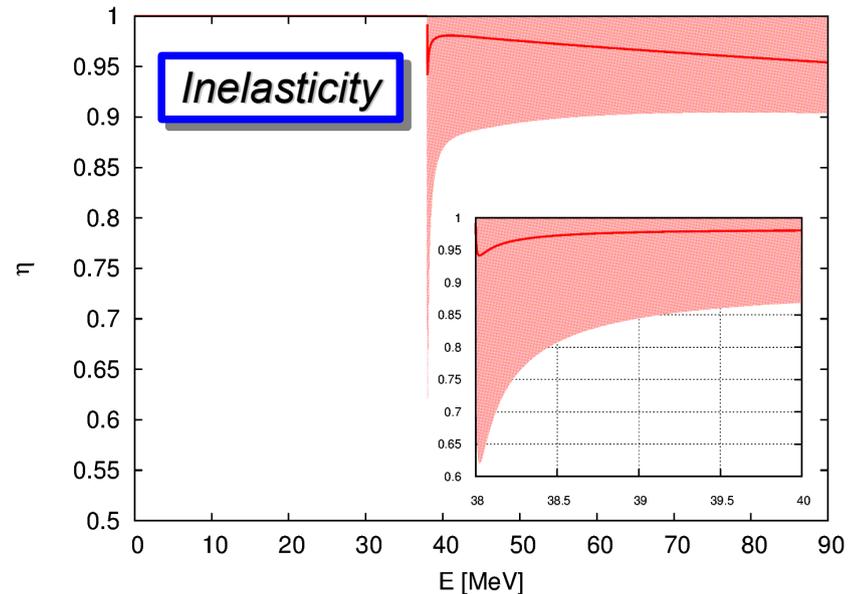
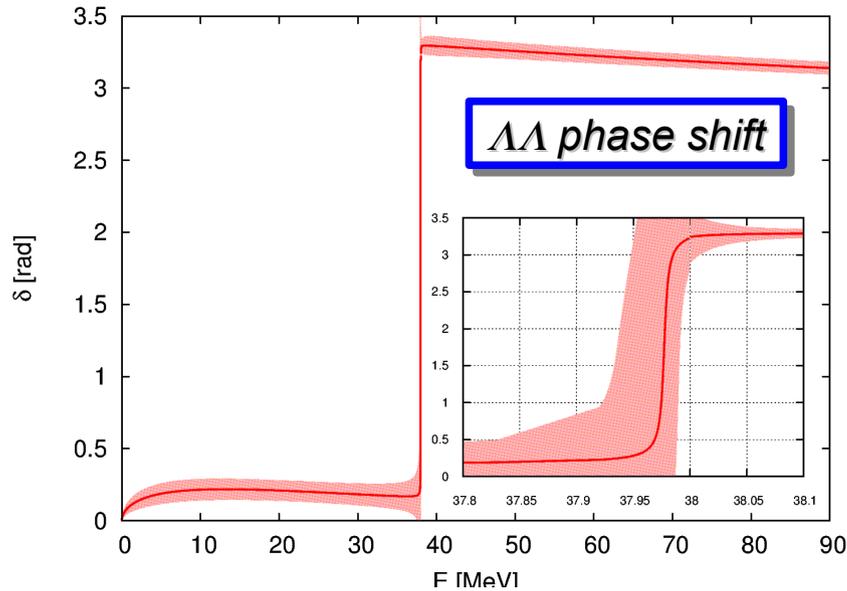


# $\Lambda\Lambda$ and $N\Xi$ phase shift and inelasticity

t=10

►  $N_f = 2+1$  full QCD with  $L = 8\text{fm}$ ,  $m_\pi = 145\text{ MeV}$

Preliminary!



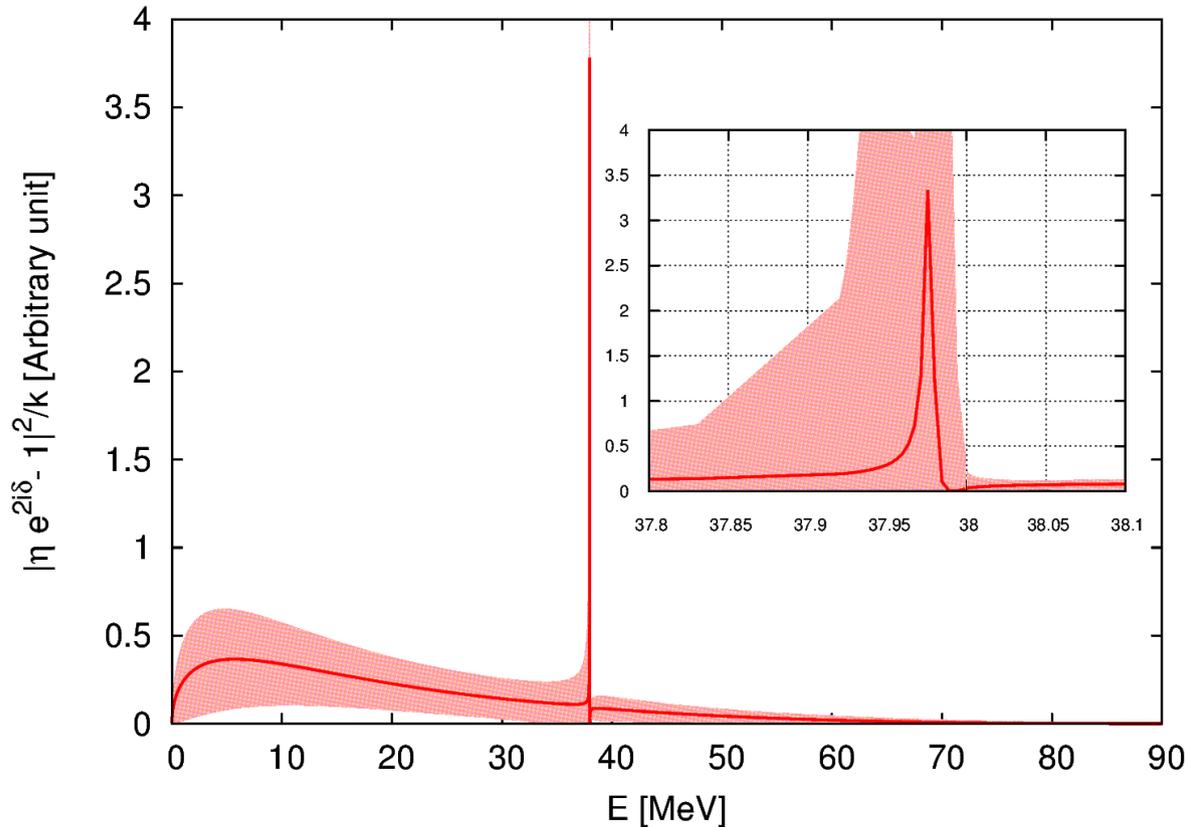
- $\Lambda\Lambda$  and  $N\Xi$  phase shift is calculated by using 2ch effective potential.
- A sharp resonance below the  $N\Xi$  threshold
- Inelasticity is small.

Breit-Wigner mass and width

$$E_R = 37.977 \pm 0.092 \text{ [MeV]}$$

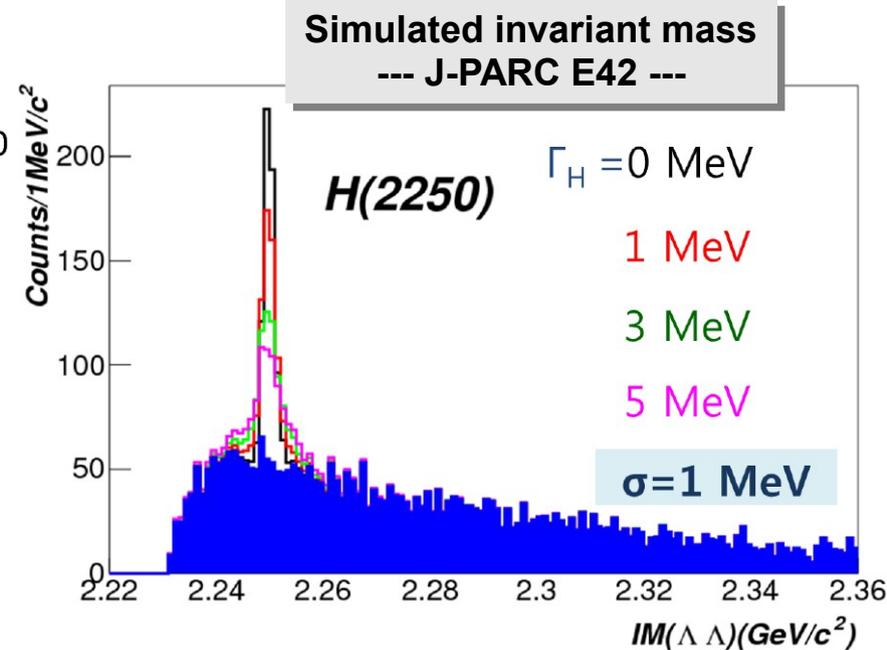
$$\Gamma = 0.0054 \pm 0.0576 \text{ [MeV]}$$

# Invariant mass spectrum of $\Lambda\Lambda$ channel



● Sharp peak below  $N\Xi$  threshold

- Time slice saturation should be checked.
- 3ch calculation (need more statistics)



# *Interactions of decuplet baryons*

# $SU(3)$ aspects of $BB$ interaction

We have succeeded to evaluate potentials  
between ground state baryons directly from QCD.

$$8 \otimes 8 = 1 \oplus 8_s \oplus 27 \oplus 8_a \oplus 10 \oplus \bar{10}$$

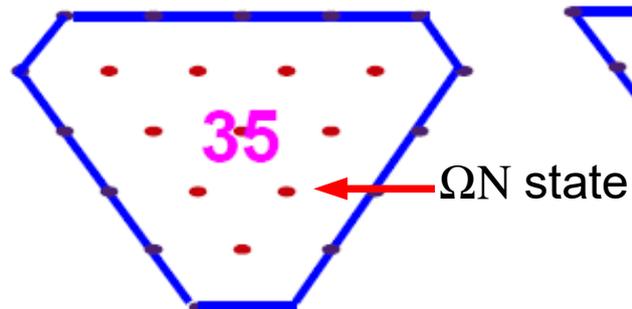
H-dibaryon ←  $1$ 
←  $27$ 
←  $\bar{10}$ 
←  $10$ 
←  $8_a$ 
←  $8_s$ 
←  $1$

Nuclear force

## ► Inclusion of decuplet baryons

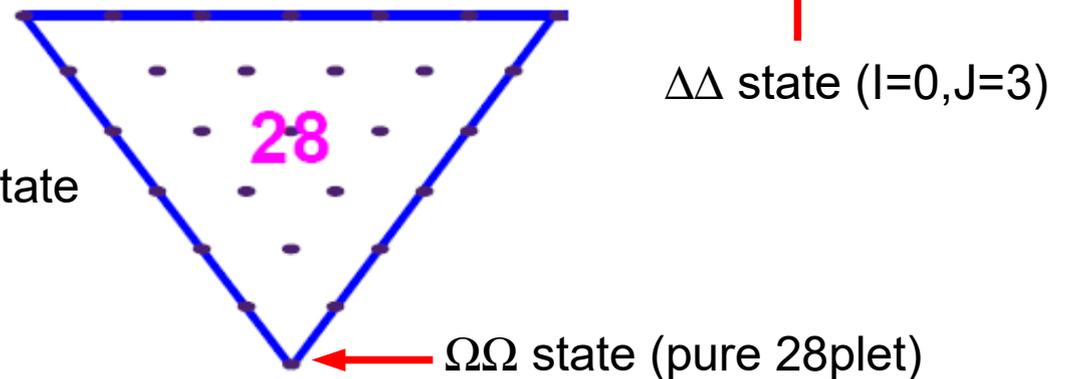
### ● For decuplet-octet system

$$10 \otimes 8 = 35 \oplus 8 \oplus 10 \oplus 27$$



### ● For decuplet-decuplet system

$$10 \otimes 10 = 28 \oplus 27 \oplus 35 \oplus \bar{10}$$



**Alternative source of generalized baryon-baryon interactions**

*$N\Omega$  interaction*

# $N\Omega$ system from quark model

- ▶ One of **di-baryon candidate**

T.Goldman et al PRL59(1987)627

- ▶ (Quasi-)Bound state is reported with  $J=2, I=1/2$

- Constituent quark model

M.Oka PRD38(1988)298

- CMI does not contribute for this system because of no quark exchange between baryons.
- **Coupled channel effect is important.**

- Chiral quark model

Q.B.Li, P.N.Shen, EPJA8(2000)

- Strong attraction yielded by scalar exchange

$N\Omega$   $J^P(I) = 2^+(1/2)$  is considered

- **Easy to tackle it by lattice QCD simulation**

- Lowest state in  $J=2$  coupled channel

- $N\Omega - \Lambda E^* - \Sigma E^* - E\Sigma^*$

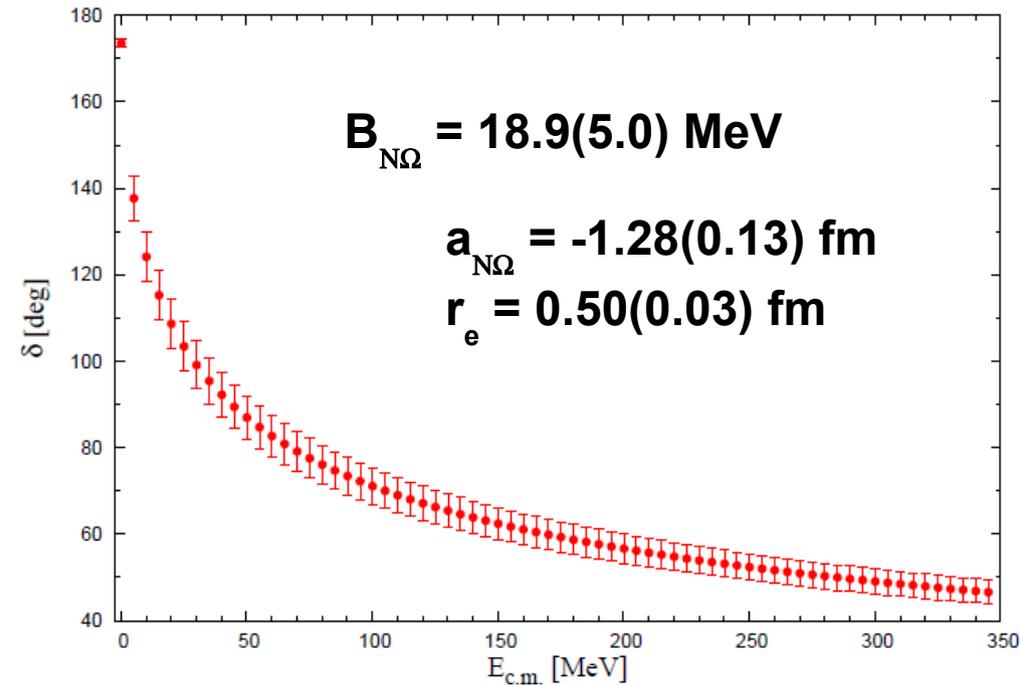
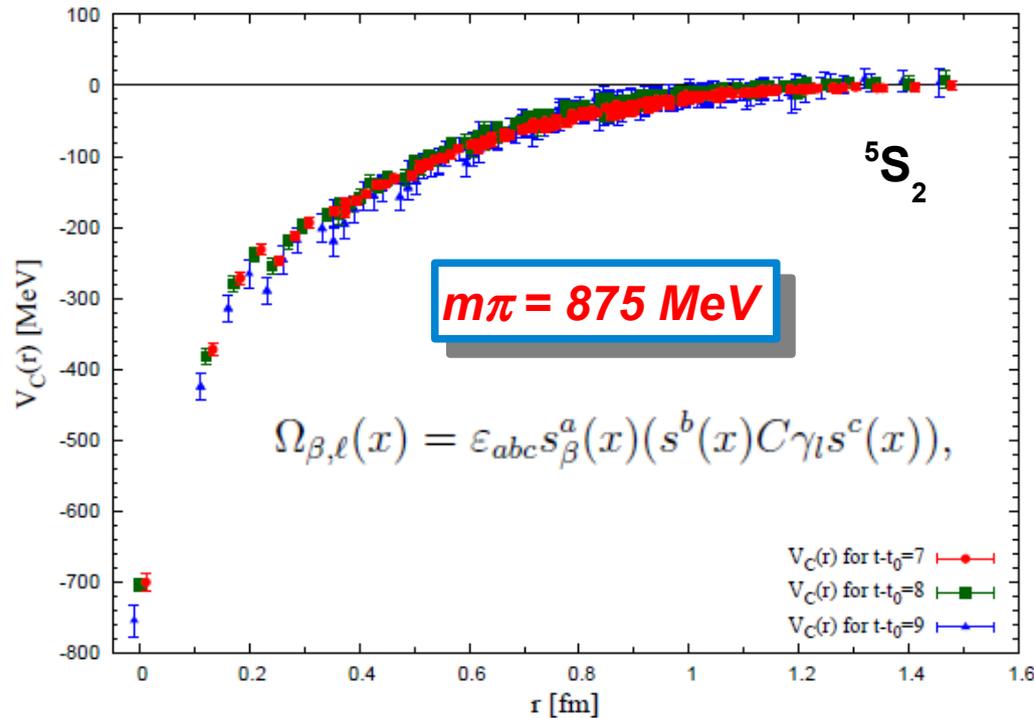
- Multi-strangeness reduces a statistical noise

- Wick contraction is very simple

# $N\Omega$ system $J^P(I) = 2^+(1/2)$

►  $N_f = 2+1$  full QCD with  $L = 1.9\text{fm}$

F.Etminan(HAL QCD), NPA928(2014)89



**$N\Omega$  state cannot decay into  $\Lambda\Xi$  (D-wave) state in this setup**

- Strongly attractive S-wave effective potential in  $J^P(I) = 2^+(1/2)$
- Good baseline to explore  $S=-3$  baryonic system

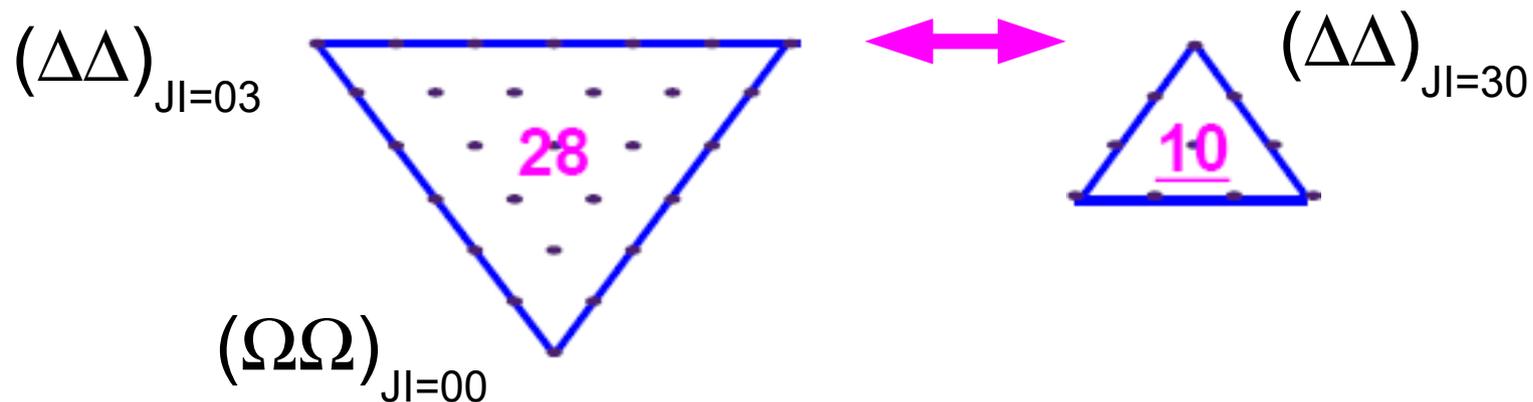
# *Decuplet-Decuplet interactions*

# Decuplet-Decuplet interaction

## ● Flavor symmetry aspect

Decuplet-Decuplet interaction can be classified as

$$10 \otimes 10 = 28 \oplus \cancel{27} \oplus \cancel{35} \oplus \bar{10}$$



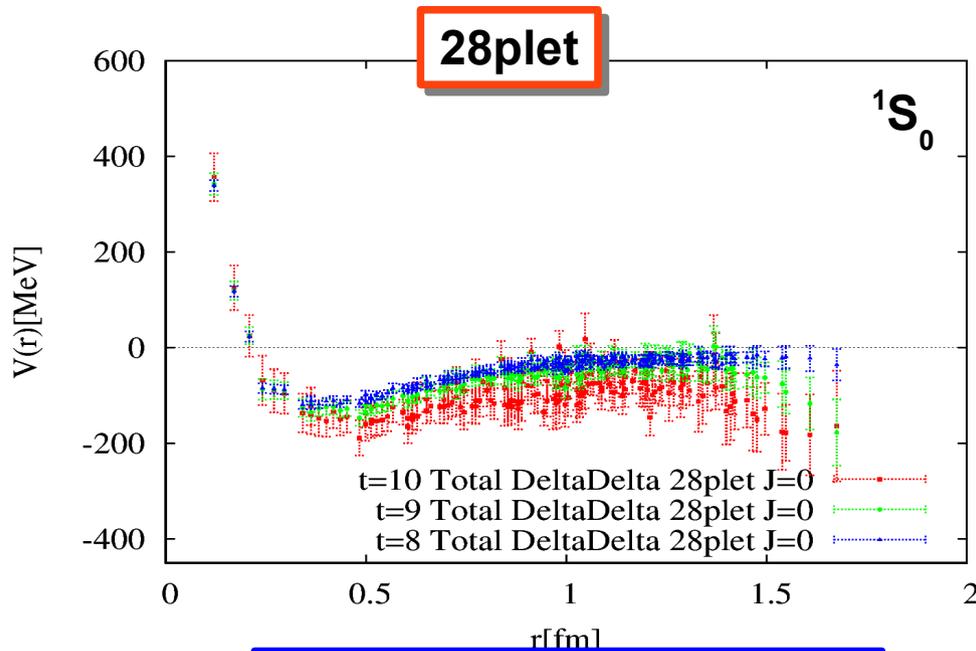
	28plet (0 <sup>+</sup> )	<del>28plet (2<sup>+</sup>)</del>	<del>10*plet (1<sup>+</sup>)</del>	10*plet (3 <sup>+</sup> )
Pauli	<b>allowed</b>	<b>forbidden</b>	---	<b>allowed</b>
CMI	<b>repulsive</b>	---	---	<b>Not attractive</b>

- $\Delta-\Delta(J=3)$  : **Bound (resonance) state was found in experiment.**
- $\Delta-\Delta(J=0)$  [and  $\Omega-\Omega(J=0)$ ] : **Mirror of  $\Delta-\Delta(J=3)$  state**

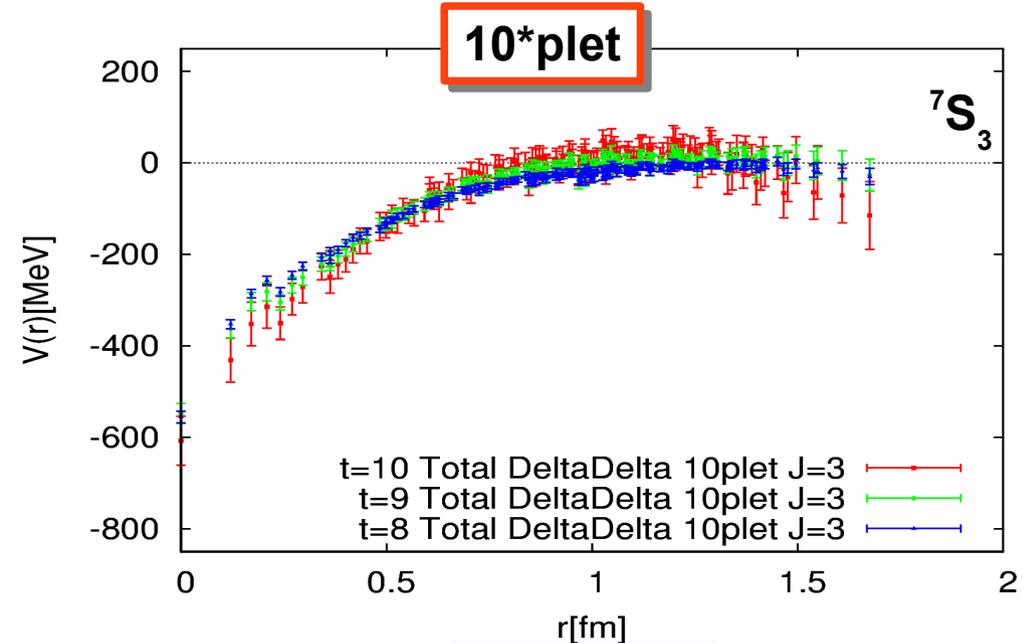
# Decuplet-Decuplet interaction in $SU(3)$ limit

►  $N_f = 2+1$  full QCD with  $L = 1.93\text{fm}$ ,  $m_\pi = 1015\text{ MeV}$

Preliminary!



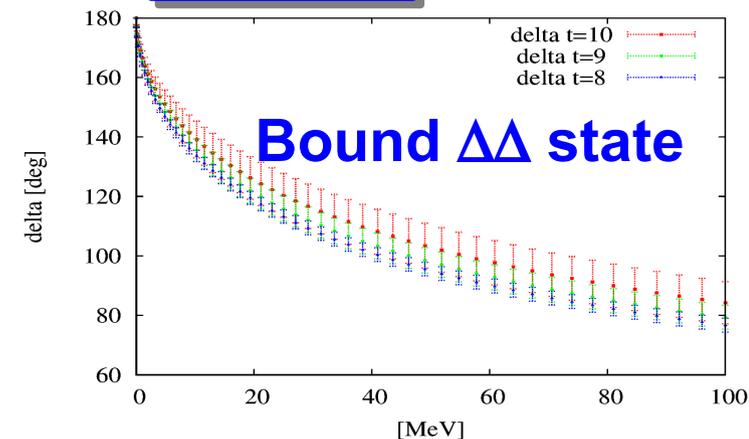
$\Delta-\Delta(J=0)$  and  $\Omega-\Omega(J=0)$



$\Delta-\Delta(J=3)$

- Short range repulsion and attractive pocket are found in 28plet.

- **10\*plet [ $J^P(I)=3^+(0)$ ] is strongly attractive.**



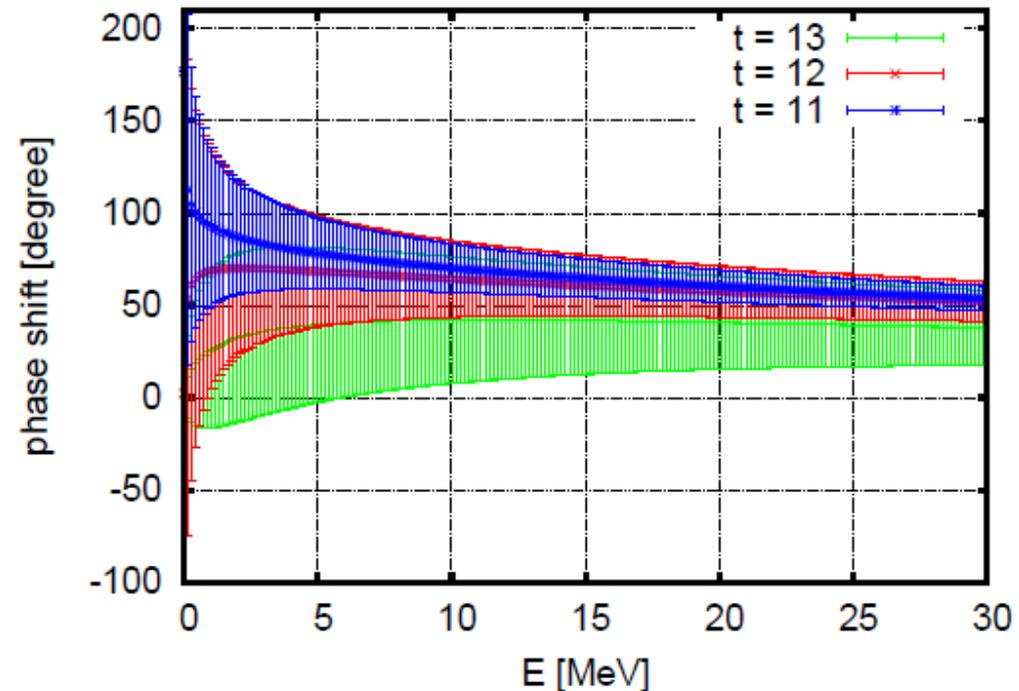
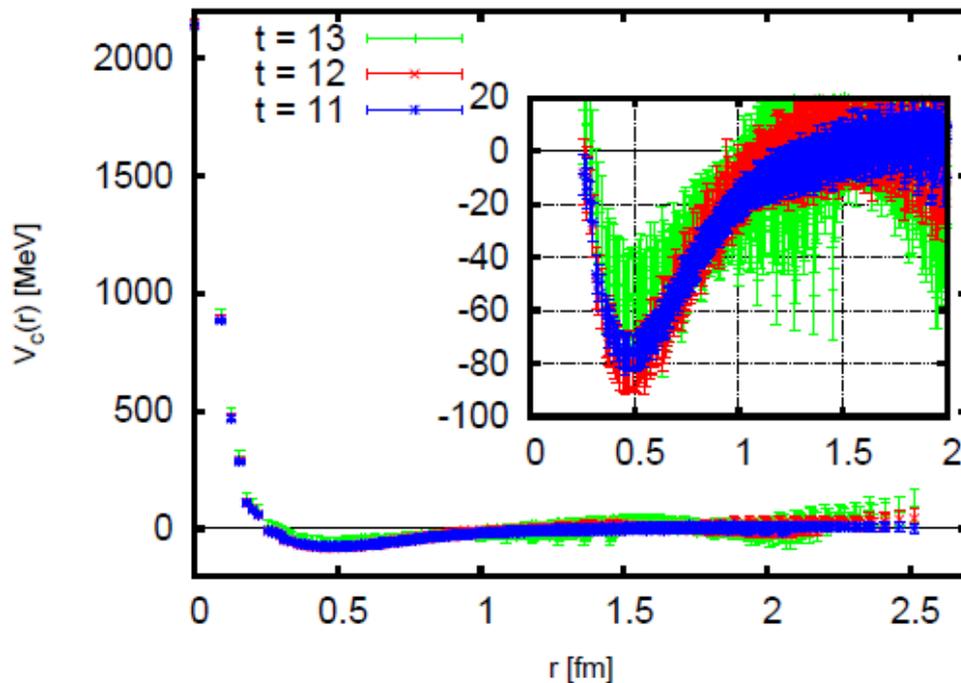
# $\Omega\Omega J^P(I) = 0^+(0)$ state in unphysical region

►  $N_f = 2+1$  full QCD with  $L = 3\text{fm}$ ,  $m_\pi = 700\text{ MeV}$

The  $\Omega\Omega$  state is stable against the strong interaction.

## Potential

## Phase shift

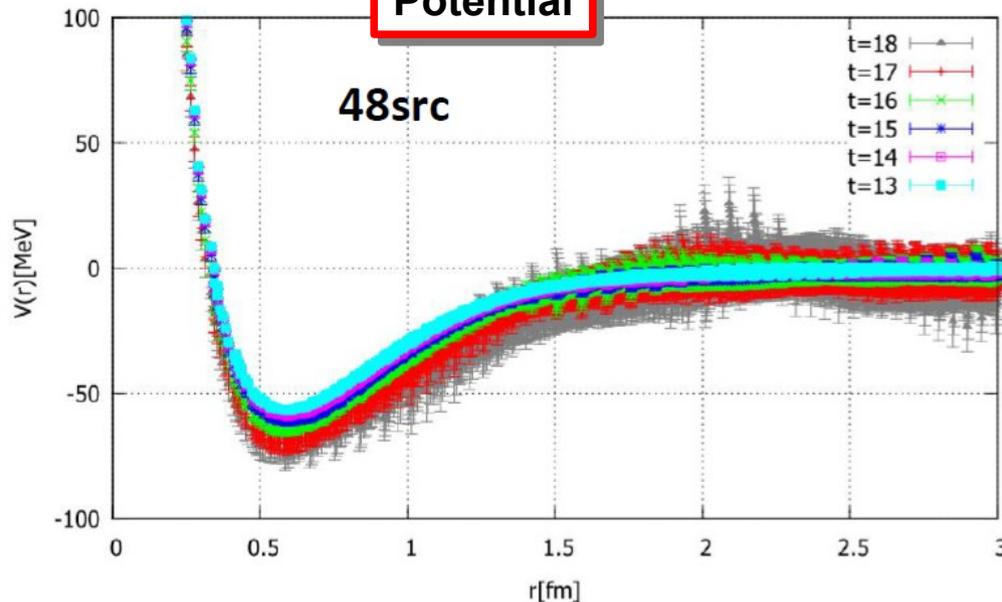


- Short range repulsion and attractive pocket are found.
- Potential is nearly independent on “t” within statistical error.
- **The system may appear close to the unitary limit.**

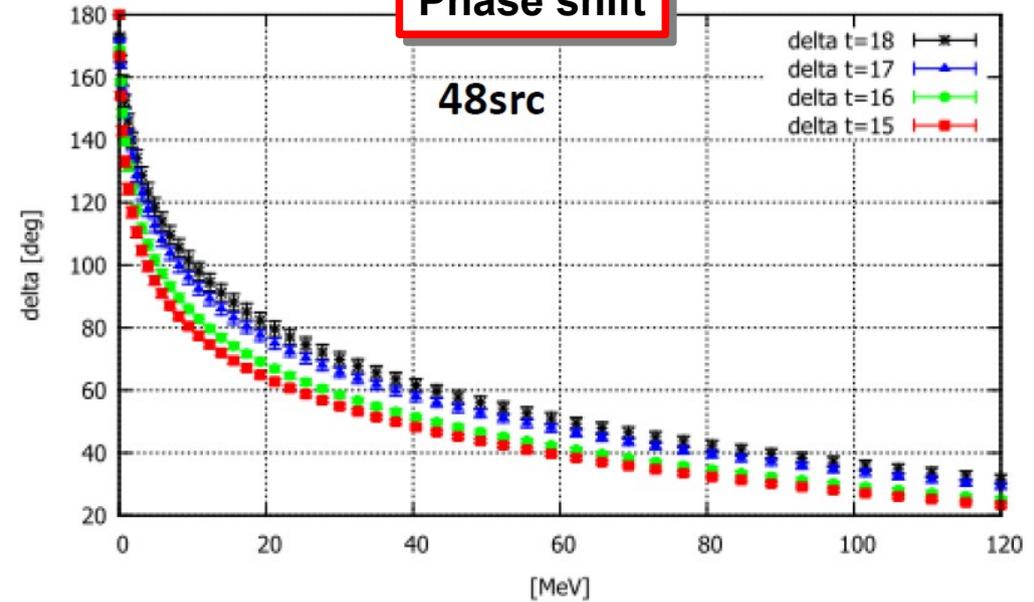
# $\Omega\Omega J^p(I) = 0^+(0)$ state near the physical point

►  $N_f = 2+1$  full QCD with  $L = 8\text{fm}$ ,  $m_\pi = 145\text{ MeV}$

Potential



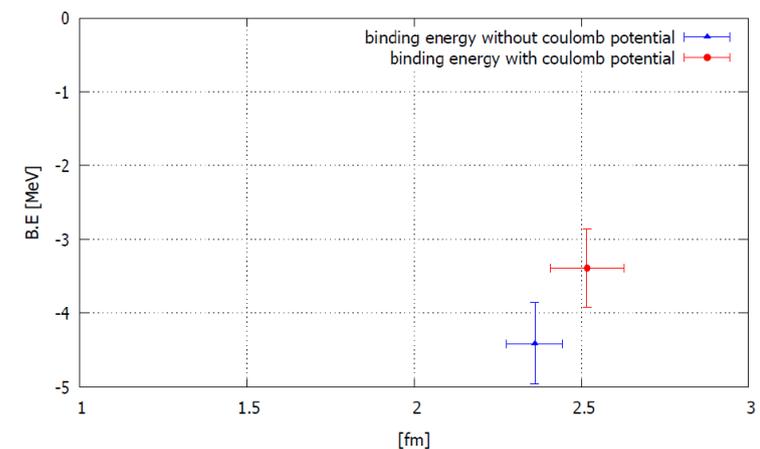
Phase shift



The  $\Omega\Omega$  state is stable against the strong interaction.

- Short range repulsion and attractive pocket are found.
- Physical  $\Omega\Omega$  state would form a bound state.
- Coulomb repulsion
  - reduces binding energy.
  - is not enough to untie two- $\Omega$ s.

Binding energy and rms



# Summary and outlook

## ▶ We have studied exotic candidate states

### ● H-dibaryon channel

- Sharp resonance just below the  $N\Xi$  threshold was found.
- Breit-Wigner mass and width are

$$E_R = 37.977 \pm 0.092 \text{ [MeV]} \quad \textbf{Preliminary!!}$$

$$\Gamma = 0.0054 \pm 0.0576 \text{ [MeV]}$$

### ● $N\Omega$ state with $J^P=2^+$

- It is strongly attractive without short range repulsion.
- It forms a bound state with about 20MeV B.E..
- $\Omega N - \Xi^* \Sigma - \Xi^* \Lambda - \Sigma^* \Xi$  coupled channel calculation is necessary.

### ● $\Delta\Delta$ and $\Omega\Omega$ states

- $\Delta\Delta(l=0)$  have strongly attractive potential.
- $\Delta\Delta(l=3)$  and  $\Omega\Omega$  potential have repulsive core and attractive pocket.
- Both channels form (quasi-)bound state???

## ▶ BB-BD-DD coupling channel treatment

## ▶ Dibaryon search at the physical point