

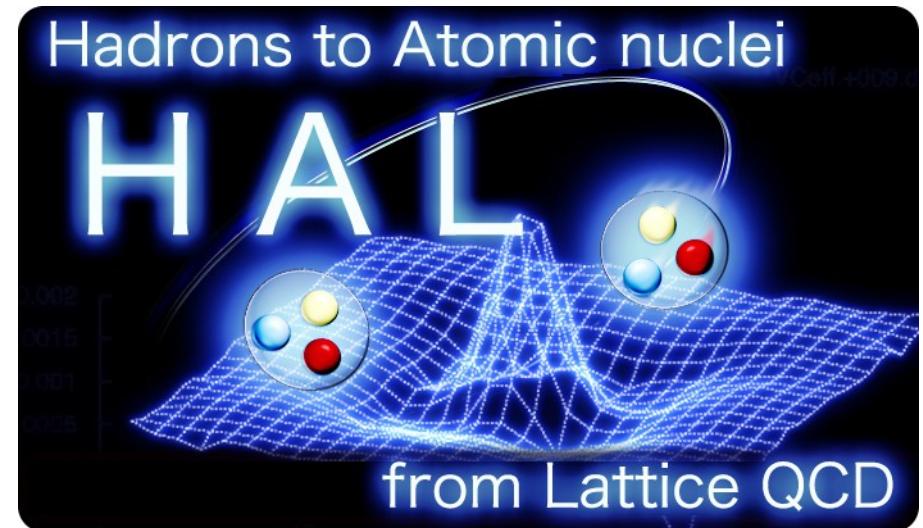
中性子星と格子QCD

井上貴史 @日本大學生物資源科學部

for

HAL QCD Collaboration

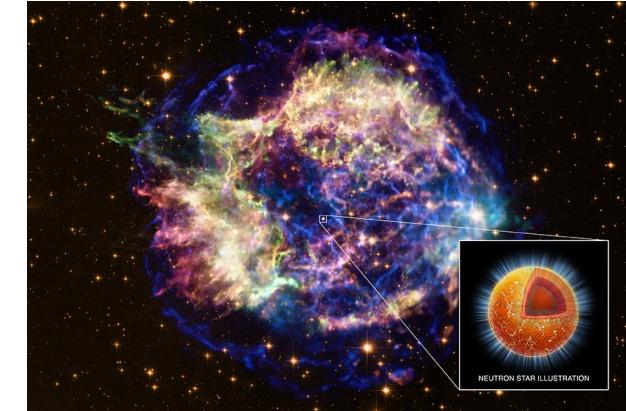
S. Aoki	YITP Kyoto Univ.
T. Doi	RIKEN Nishina
T. Hatsuda	RIKEN Nishina
Y. Ikeda	RIKEN Nishina
T. I.	Nihon Univ.
N. Ishii	RCNP Osaka Univ.
K. Murano	RCNP Osaka Univ.
H. Nemura	Univ. Tsukuba
K. Sasaki	Univ. Tsukuba
F. Etminan	Univ. Birjand
T. Miyamoto	Univ. Tsukuba
T. Iritani	Stony Brook Univ.
S. Gongyo	YITP Kyoto Univ.



Introduction

★ Neutron Star

- is a compact star formed after supernova explosion of massive star.
- Typically, $M = 1.5 M_{\odot}$, $R = 10 \text{ km}$.
- Temperature $T \simeq 10^8 \text{ [K]} \simeq 0.01 \text{ [MeV]} \simeq 0$
- Density in core $\rho = \text{several} \times \rho_0$



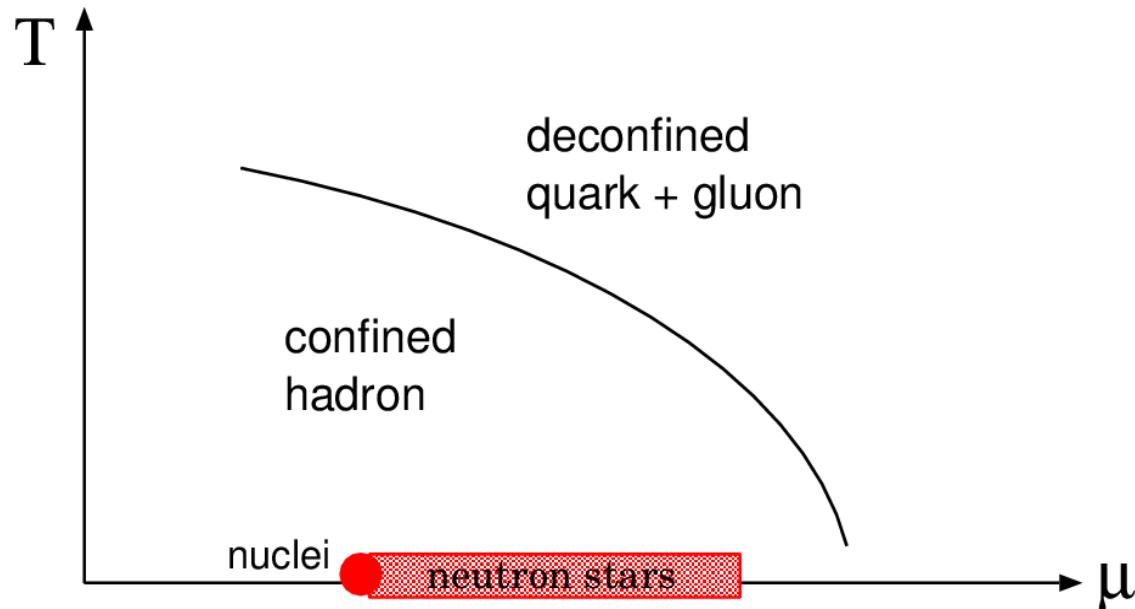
is roughly $10^{15} \text{ [g/cm}^3\text{]}$!
Most dense in Universe!

★ Equation of State

- is a relation between energy and pressure of matter
 $P(E)$ or $E(P)$ or $E(\rho)$ or $E(k_F)$ or ...
- EoS of dense baryonic matter is crucial for NS since it determines NS stable mass and radius, especially maximum NS mass (boundary between NS and BH).

Introduction

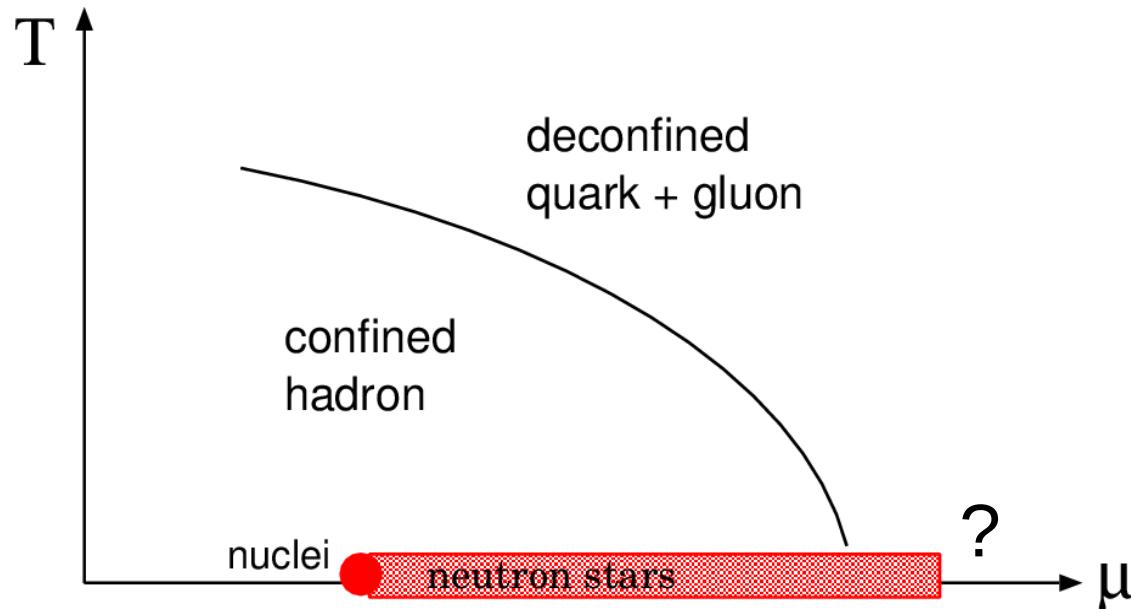
★ QCD phase diagram



- NS matter has $\rho = \text{several} \times \rho_0$ and $T \approx 0$, and corresponds to  on the QCD phase-diagram.

Introduction

★ QCD phase diagram

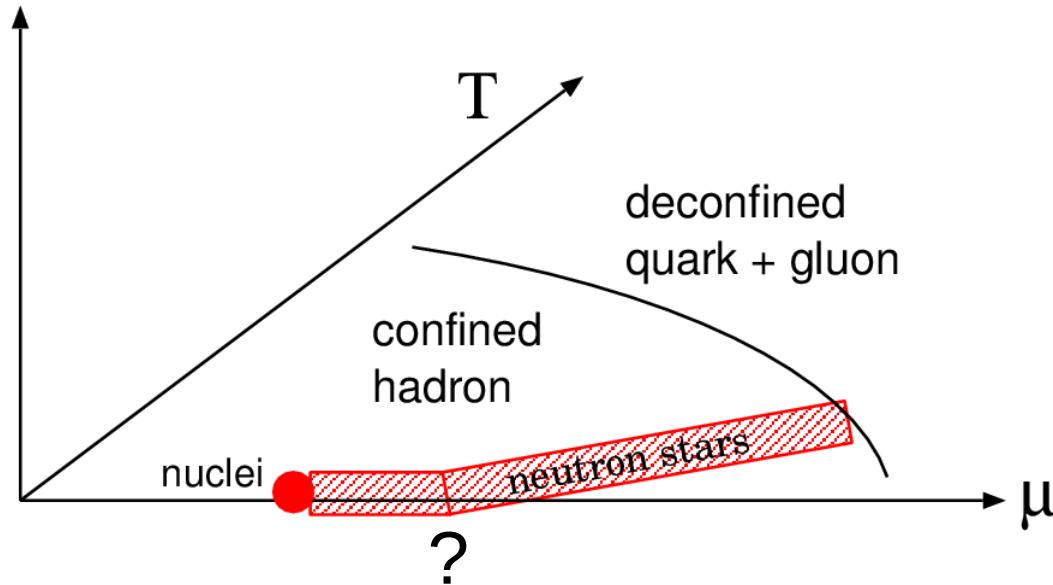


- NS matter has $\rho = \text{several} \times \rho_0$ and $T \approx 0$, and corresponds to  on the QCD phase-diagram.
- Perhaps, it touches the deconfined **QGP** phase.

Introduction

★ QCD phase diagram

Strangeness

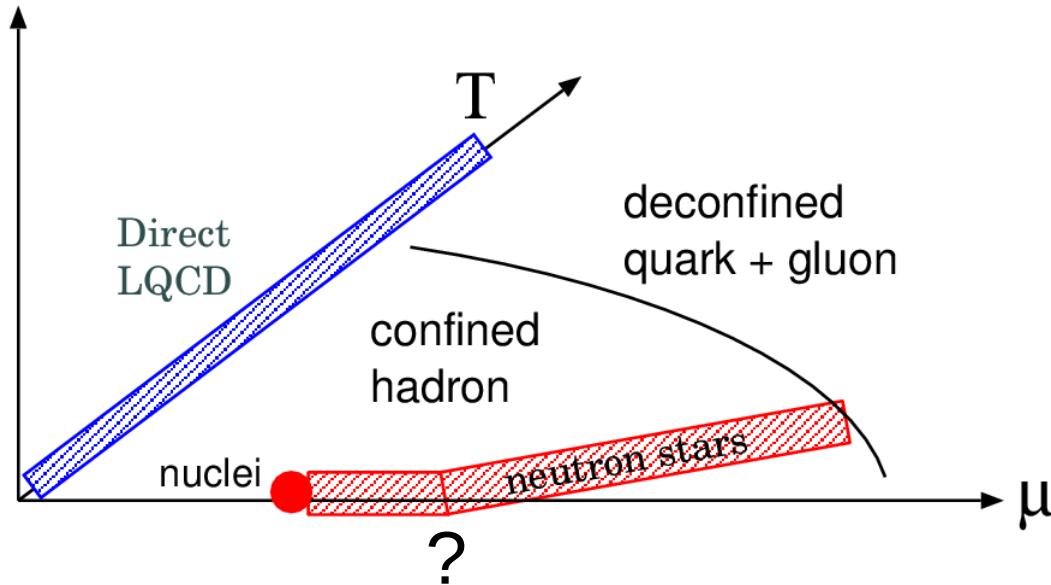


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- Probably, it goes to finite **strangeness** direction.

Introduction

★ QCD phase diagram

Strangeness

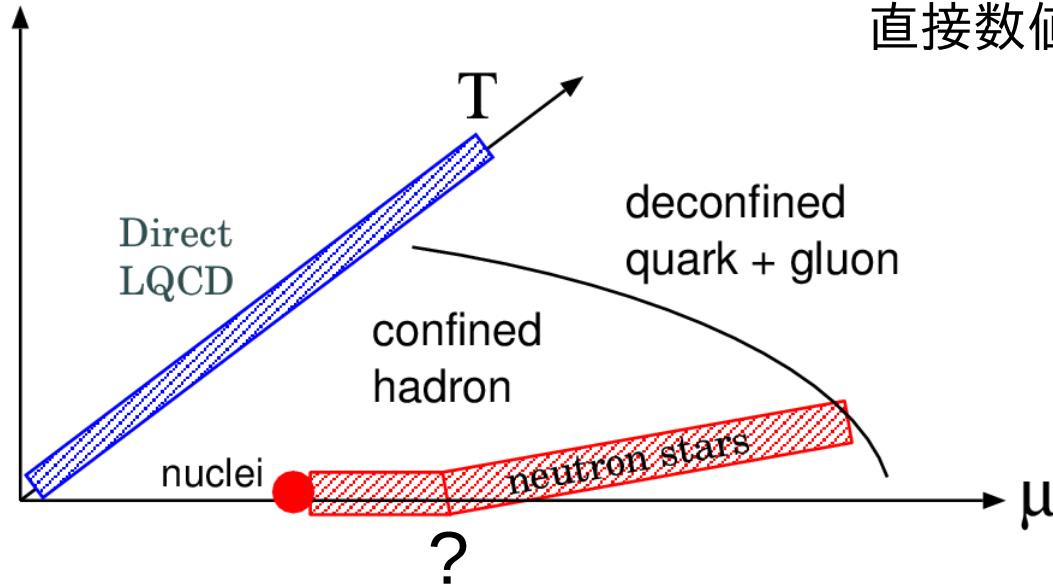


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- Current LQCD simulations are **limited** only for $\mu \approx 0$. 6

Introduction

★ QCD phase diagram

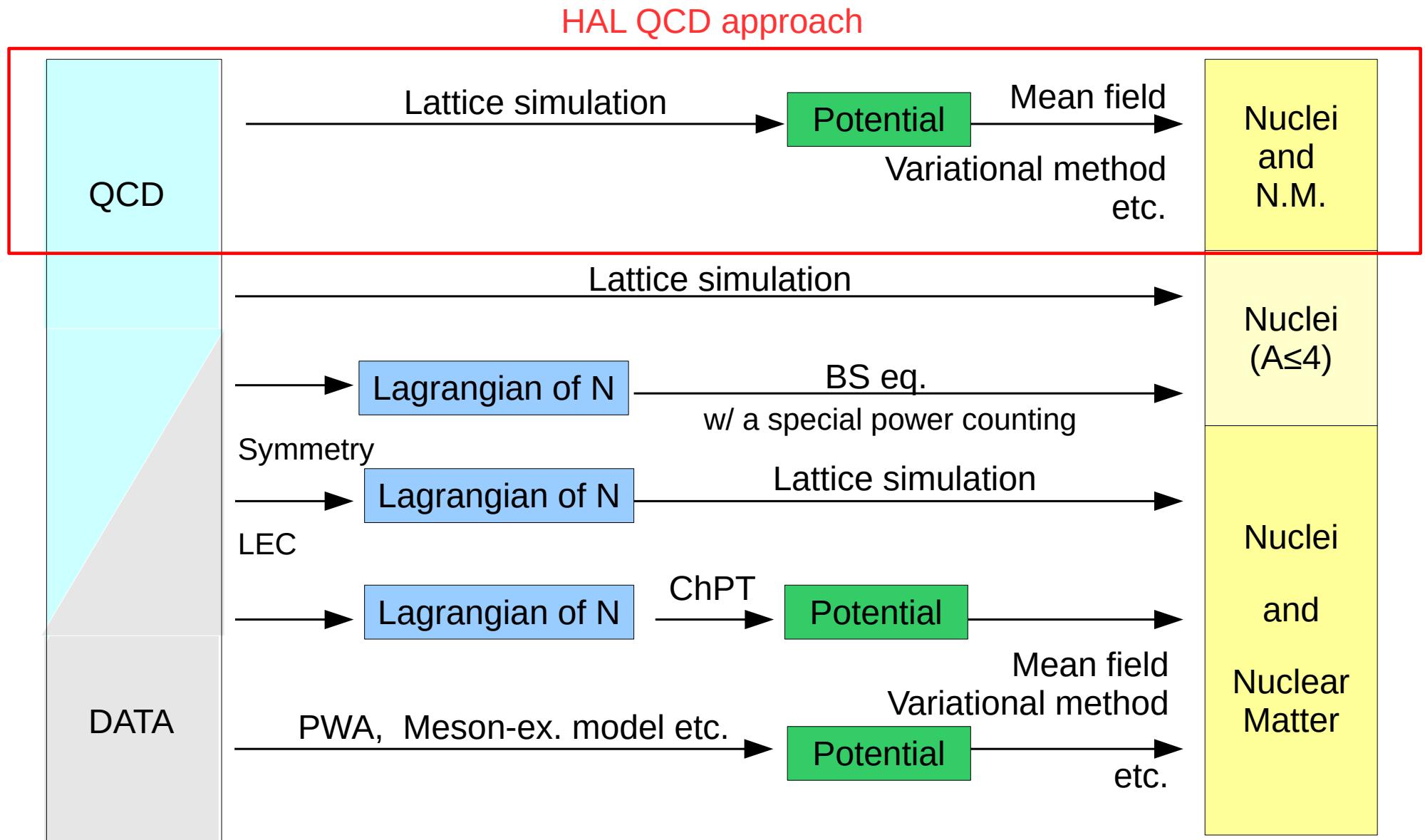
Strangeness



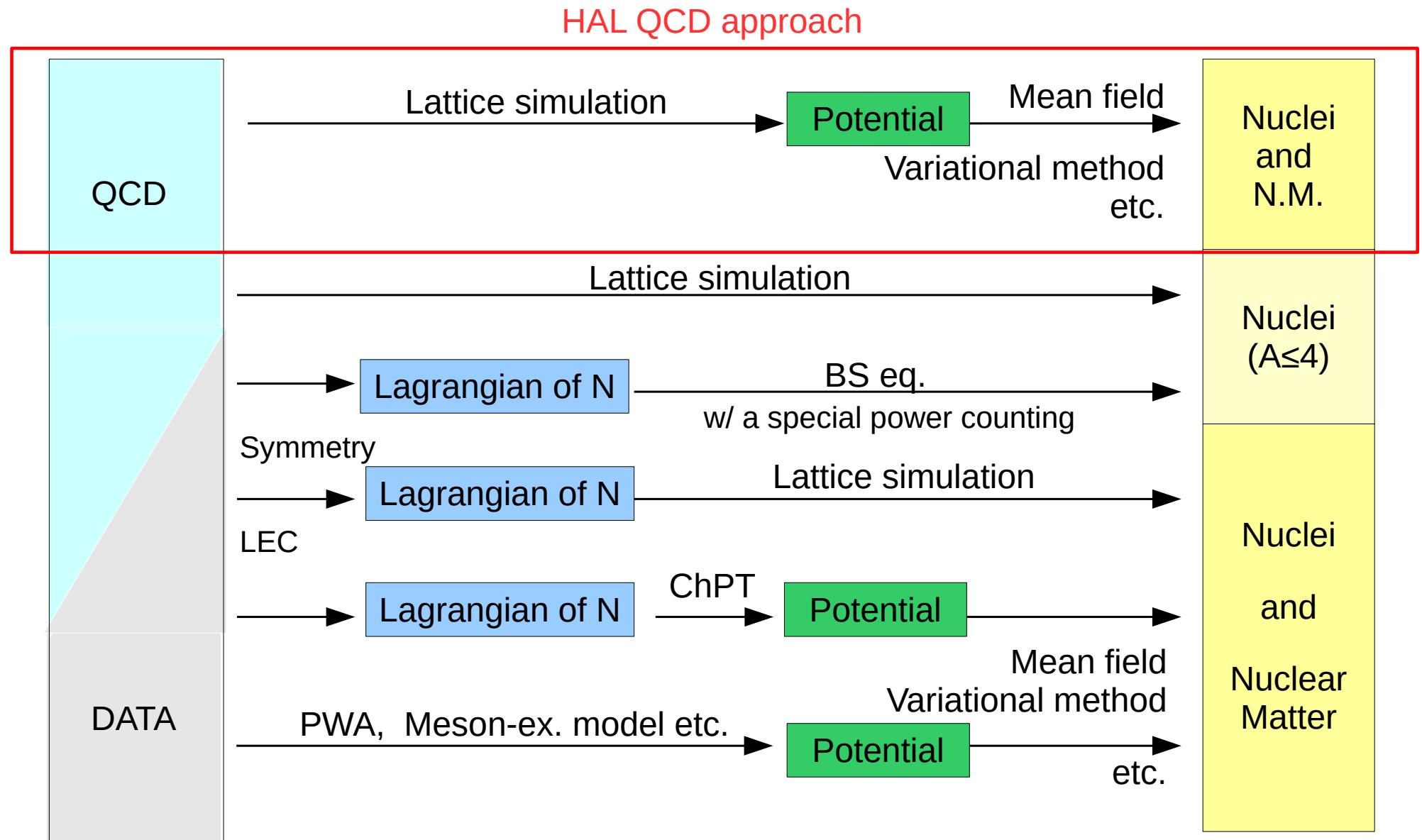
格子QCDから中性子星を攻めるには、直接数値計算とは別のアプローチが必要！

- NS matter has $\rho = \text{several} \times \rho_0$ and $T \approx 0$, and corresponds to [red box] on the QCD phase-diagram.
- Perhaps, it touches the deconfined **QGP** phase.
- Probably, it goes to finite **strangeness** direction.
- Current LQCD simulations are **limited** only for $\mu \approx 0$.

Various approaches in nuclear phys.



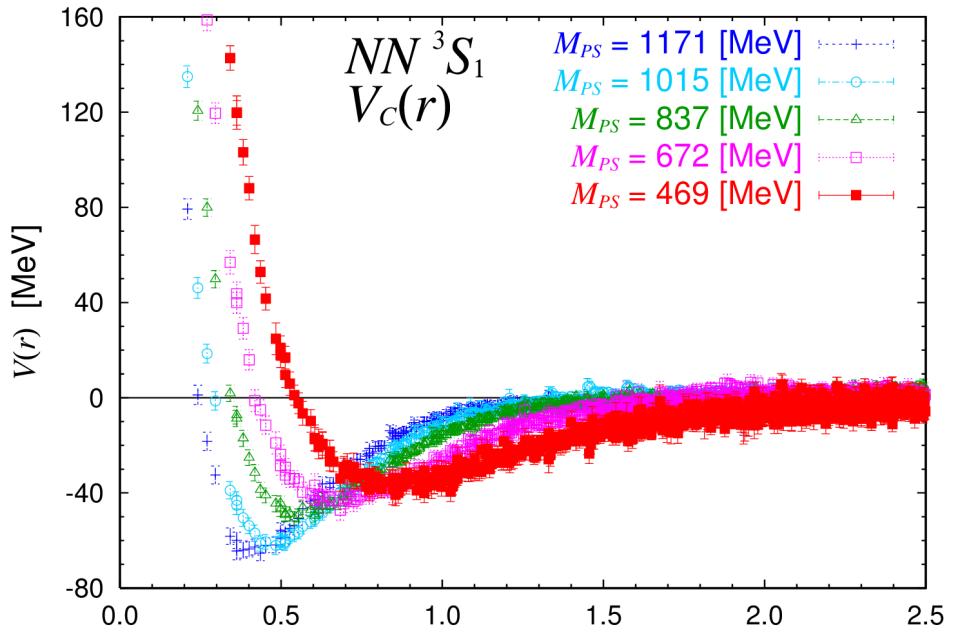
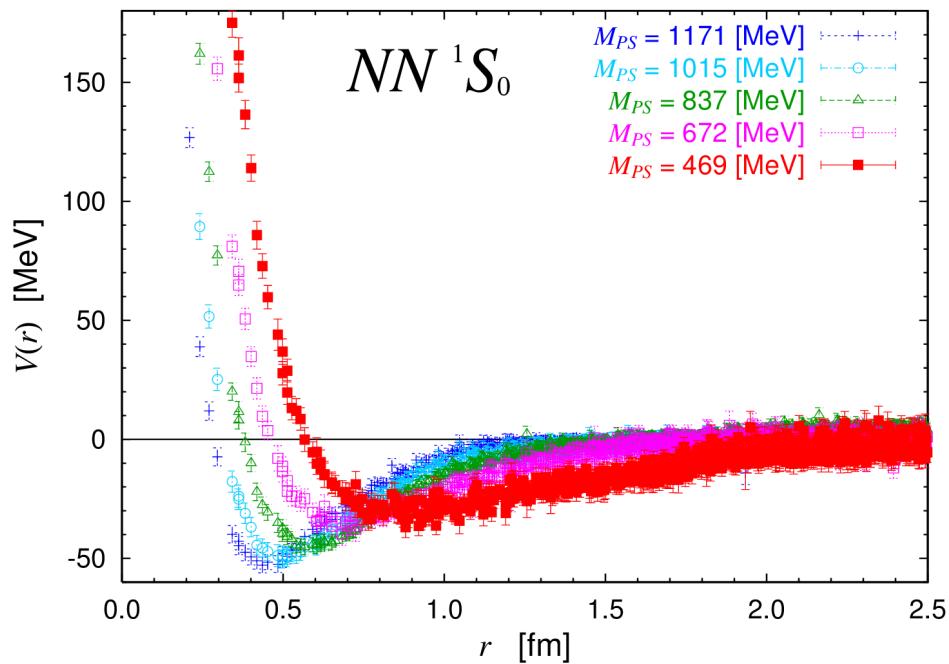
Various approaches in nuclear phys.



今日は、**だいぶ前に**、このアプローチで中性子星を調べた話をします。

Nuclear force from QCD

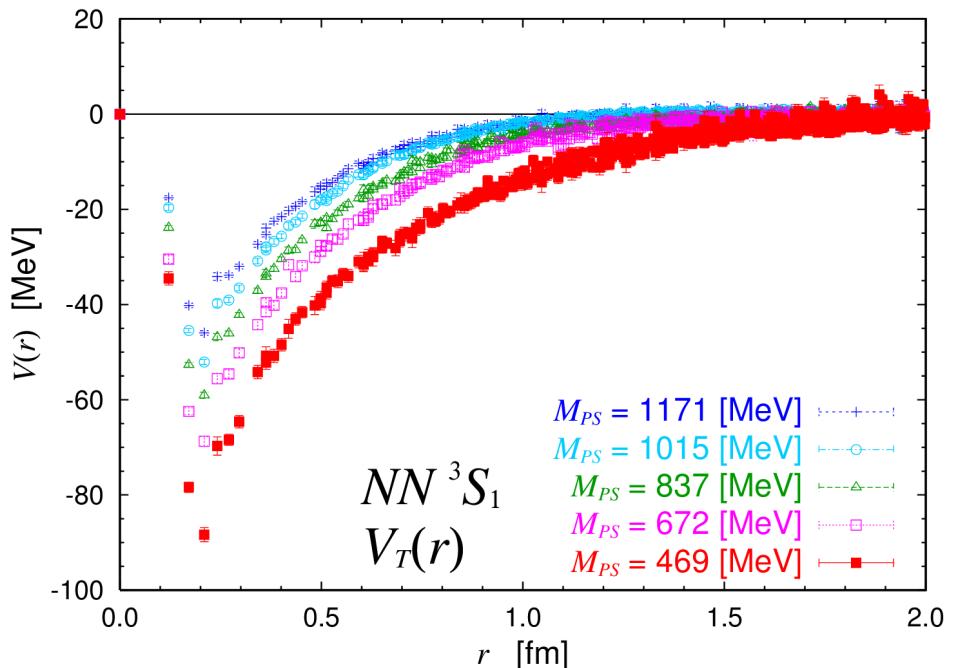
NN potentials from QCD



- At $SU(3)_F$ limit which is useful to capture essential feature of BB int.

size	β	C_{SW}	a [fm]	L [fm]
$32^3 \times 32$	1.83	1.761	0.121(2)	3.87

- Thanks to **PACS-CS** collaboration for their DDHMC/PHMC code.



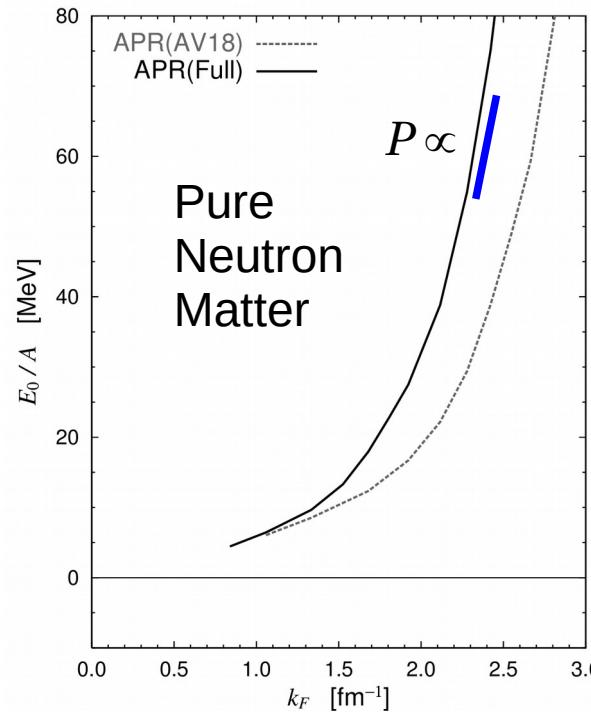
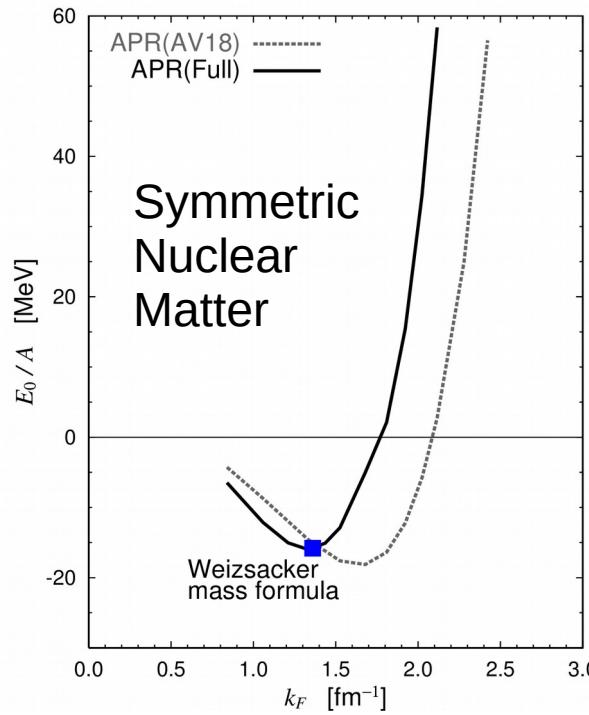
EoS of nuclear matter and Neutron star from QCD

Equation of State

- Ground state of interacting infinite nucleon system
 - Relativistic Mean Field
 - Fermi Hyper-Netted Chain

J. D. Walecka, Ann. Phys. 83 (1974) 491

A. Akmal, V.R. Phandharipande, D.G. Ravenhall
Phys. Rev. C 58 (1998) 1804



They used
phenomenological
Argonne NN force &
“Urbana” NNN force.

- For SNM, most important feature is the **saturation**.
- For PNM or NSM, the **slope** at large k_F is important.

BHF for nuclear matter

K.A. Brueckner and J.L.Gammel
Phys. Rev. 109 (1958) 1023

M.I. Haftel and F. Tabakin,
Nucl. Phys. A158(1970) 1-42

- Ground state energy in **BHF** framework

$$E_0 = \gamma \sum_k^{k_F} \frac{k^2}{2M} + \frac{1}{2} \sum_i^{N_{ch}} \sum_{k, k'}^{k_F} \text{Re} \langle G_i(e(k) + e(k')) \rangle_A$$

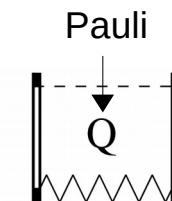
$$\Delta E_0 = \text{---} + \text{---}$$

- G-matrix

$$\langle k_1 k_2 | G(\omega) | k_3 k_4 \rangle = \langle k_1 k_2 | V | k_3 k_4 \rangle + \sum_{k_5 k_6} \frac{\langle k_1 k_2 | V | k_5 k_6 \rangle Q(k_5, k_6) \langle k_5 k_6 | G(\omega) | k_3 k_4 \rangle}{\omega - e(k_5) - e(k_6)}$$

LQCD V_{NN}

$$\text{G-matrix} = \text{---} + \text{---}$$



- Single particle spectrum & potential

$$e(k) = \frac{k^2}{2M} + U(k)$$

$$\parallel = \text{---} + \text{---} + \text{---}$$

$$U(k) = \sum_i \sum_{k' \leq k_F} \text{Re} \langle k k' | G_i(e(k) + e(k')) | k k' \rangle_A$$

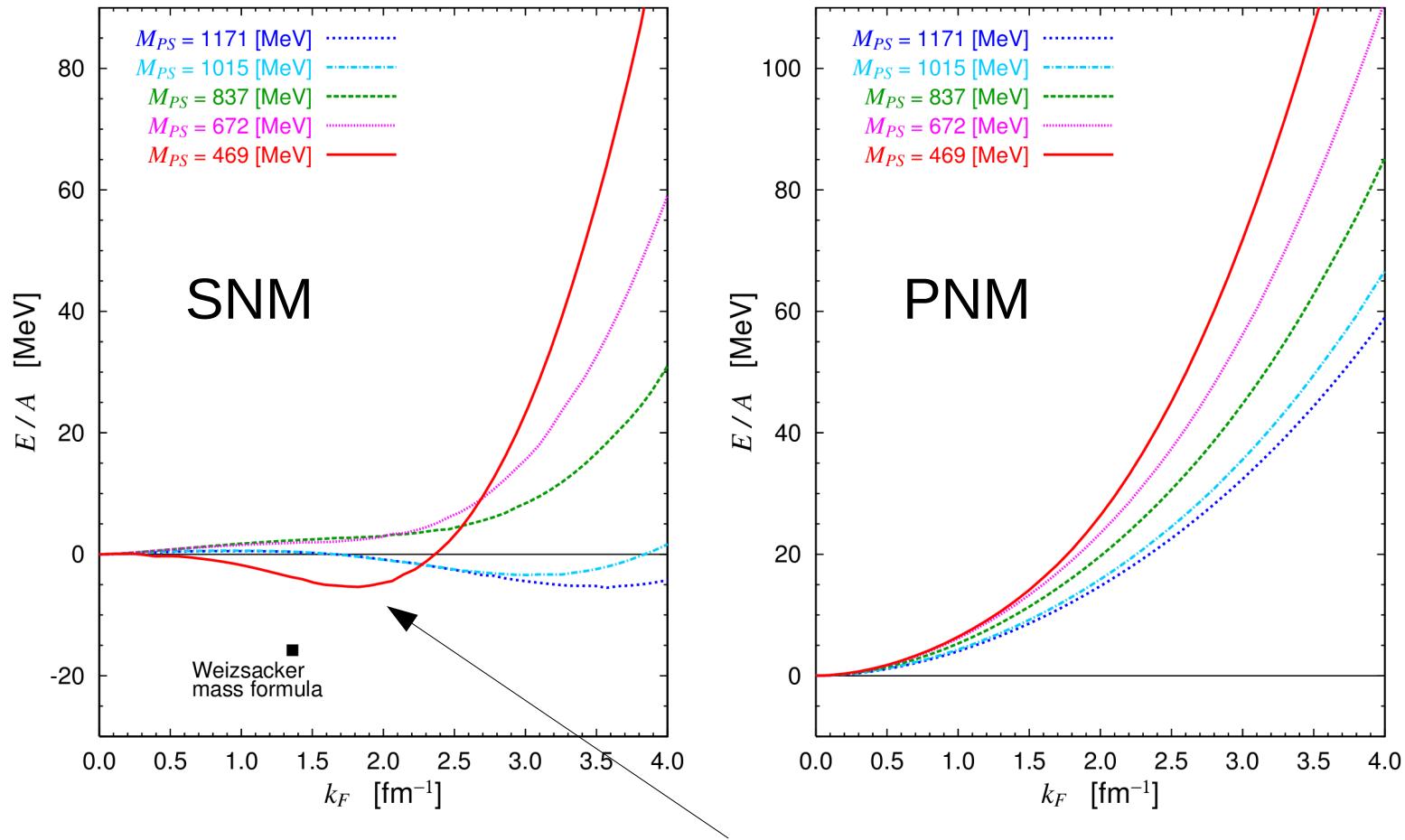
limitation

- p.w. decomposition & truncation $^{2S+1}L_J = {}^1S_0, {}^3S_1, {}^3D_1, {}^1P_1, {}^3P_J \dots$
- Continuous choice w/ parabolic approximation, Angle averaged Q-operator

$\xleftarrow{14}$

Matter EoS from QCD

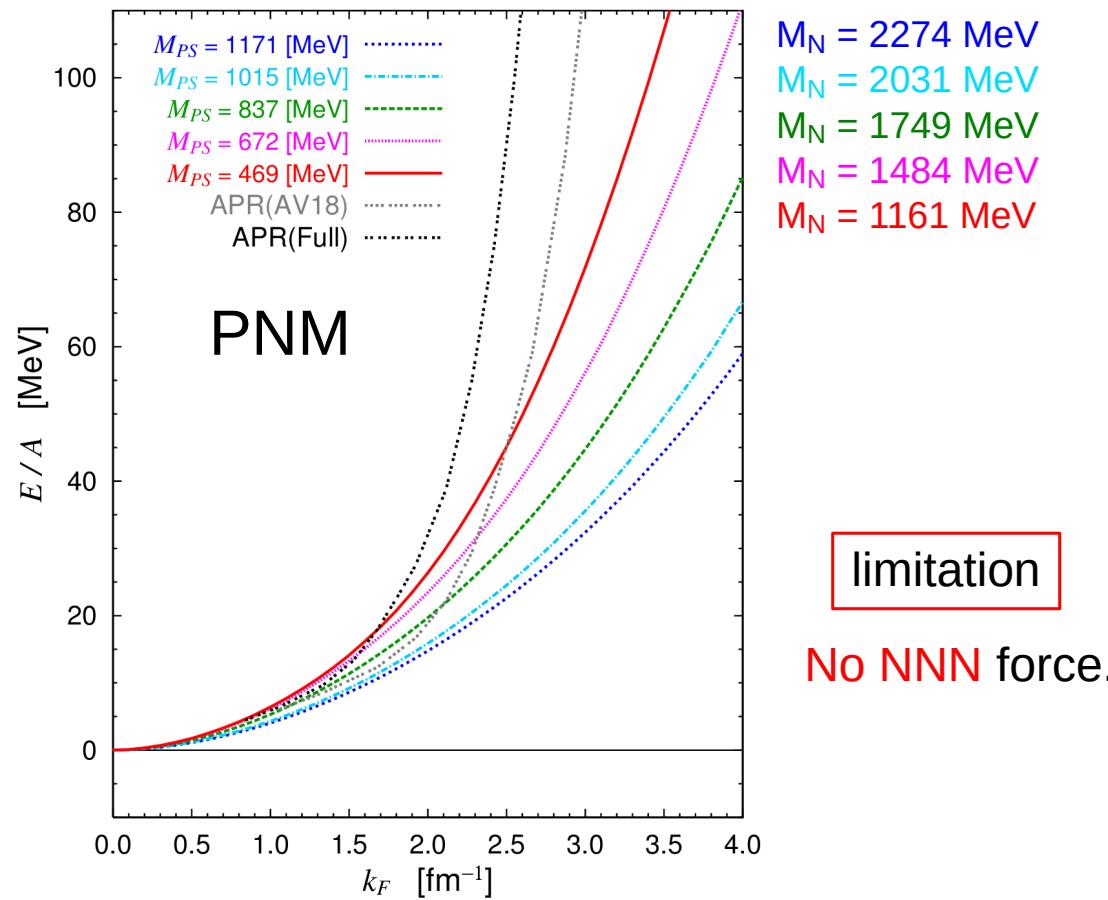
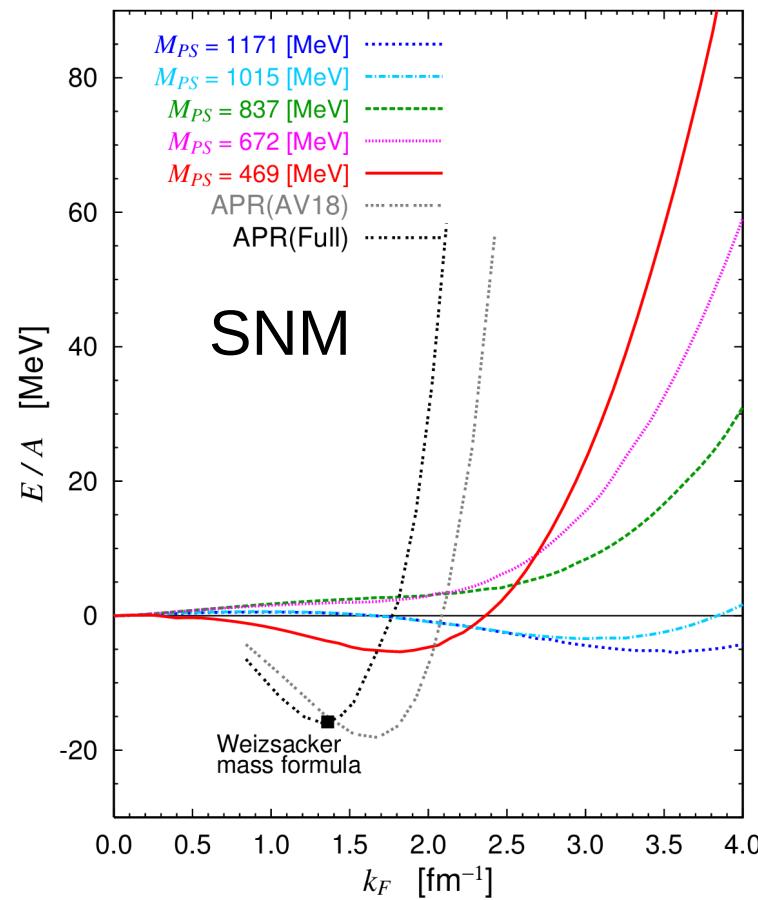
T. Inoue et al. PRL 11, 112503 (2013)



- SNM is bound and the **saturation** occurs at $M_{PS} = 469$ MeV.
 - Saturation is very delicate against change of quark mass.
- PNM is unbound as normal.
 - PNM become **stiff** at high density as quark mass decrease.

Matter EoS from QCD

T. Inoue et al. PRL 11, 112503 (2013)



- “APR” curves are EoS of the matter in the physical world, obtained with a variational method and experimental data.
phenomenological force
- HALQCD EoS largely **deviate** from the empirical ones, primarily due to the **heavy u, d** quark in our calculation.

We expect more compatible results from the physical point LQCD.

Stable Neutron Star (spherical & non-rotating)

- Tolman-Oppenheimer-Volkoff equation

$$\frac{dP(r)}{dr} = -\frac{G(E(r) + P(r))(M(r) + 4\pi r^3 P(r))}{r(r - 2GM(r))}$$

R. C. Tolman, Phys Rev. 55(1939) 364

J. R. Oppenheimer and G. M. Volkoff
Phys. Rev. 55 (1939) 374

$$\frac{dM(r)}{dr} = 4\pi r^2 E(r)$$

$P(r)$: Pressure

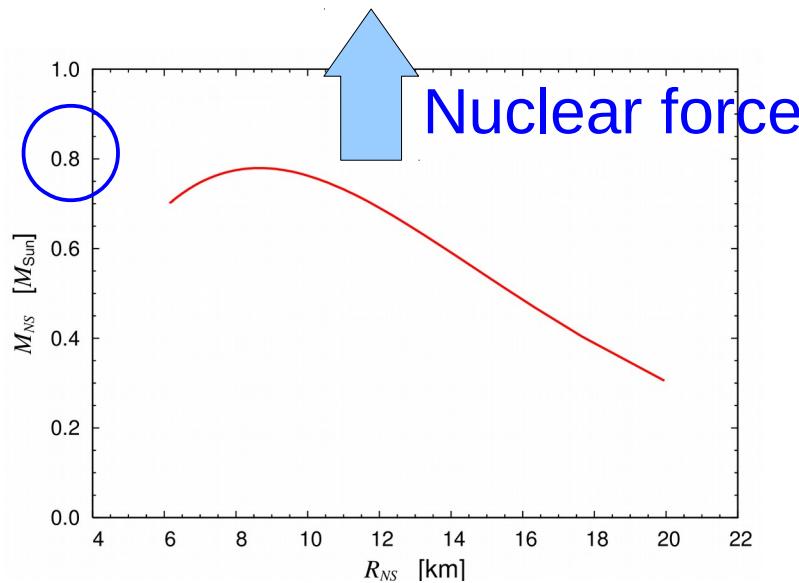
$E(r)$: Mass-energy density

$M(r)$: Enclosed mass

Gravitational constant

$G = 6.6743 \times 10^{-11} [\text{m}^3 \text{ kg}^{-1} \text{ s}^{-2}]$

- with $P(E)$ (EoS) for a cold **Fermi gas** of neutrons.

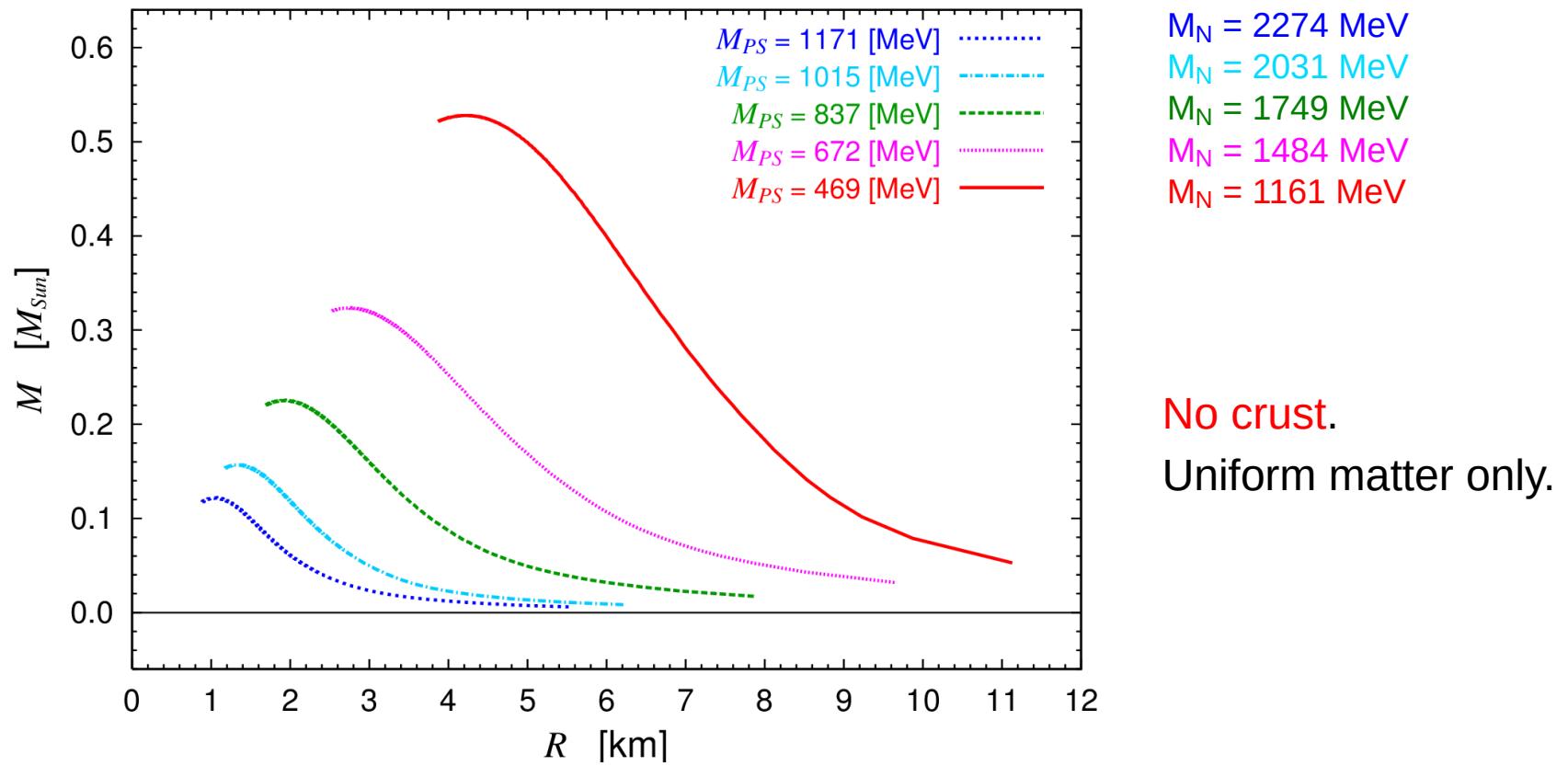


QCD is essential for NS!

Let us apply our LQCD EoS
to neutron stars.

Neutron Star M-R relation

T. Inoue et al. PRL 11, 112503 (2013)



- Mass-radius curve of neutron stars at five value of m_q .
 - $M^{\max} = 0.12 - 0.52 [M_{\odot}]$ for $M_{ps} = 1171 - 469 \text{ [MeV]}$.
 - due to **heavy** nucleon and **weaker** repulsion at short distance.
 - M^{\max} will be much bigger with lighter u,d quark.

We expect more compatible results from the physical point LQCD.

More on Neutron star and QCD

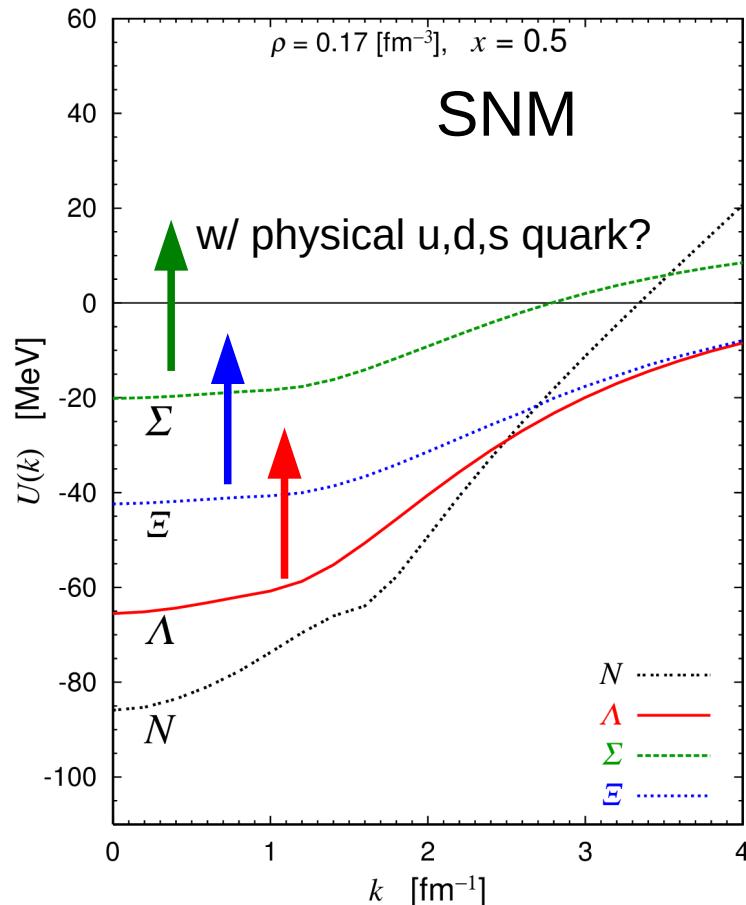
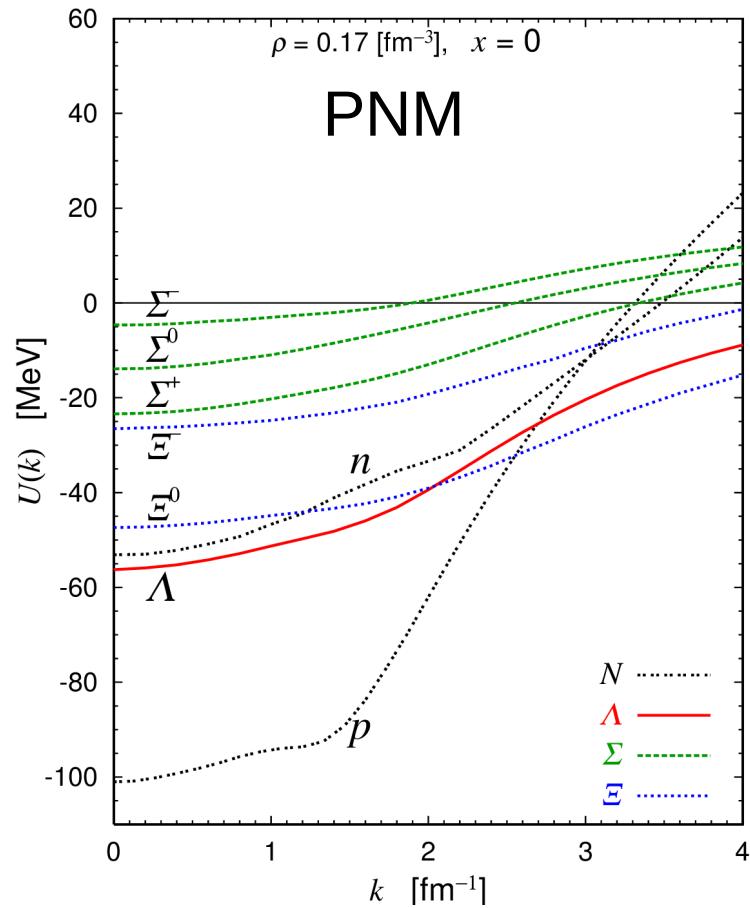
Strangeness in neutron star

- ★ Probably, hyperons exist in core of NS.
- ★ How EoS of NS matter can be stiff with hyperon?
- ★ Tough problem due to ambiguity of YN, YY force.
 - ambiguity due to shortage of experimental data.
- ★ But, we can study hyperon in nuclear medium by basing on YN, YY force extracted from QCD.
- ★ Hyperon chemical potential $\mu_Y(\rho)$ in matter and onset density are given by single-particle potential

Hyperon spectrum
in nuclear medium

$$e_Y(k) = \frac{k^2}{2M_Y} + \underline{U_Y(k)}$$

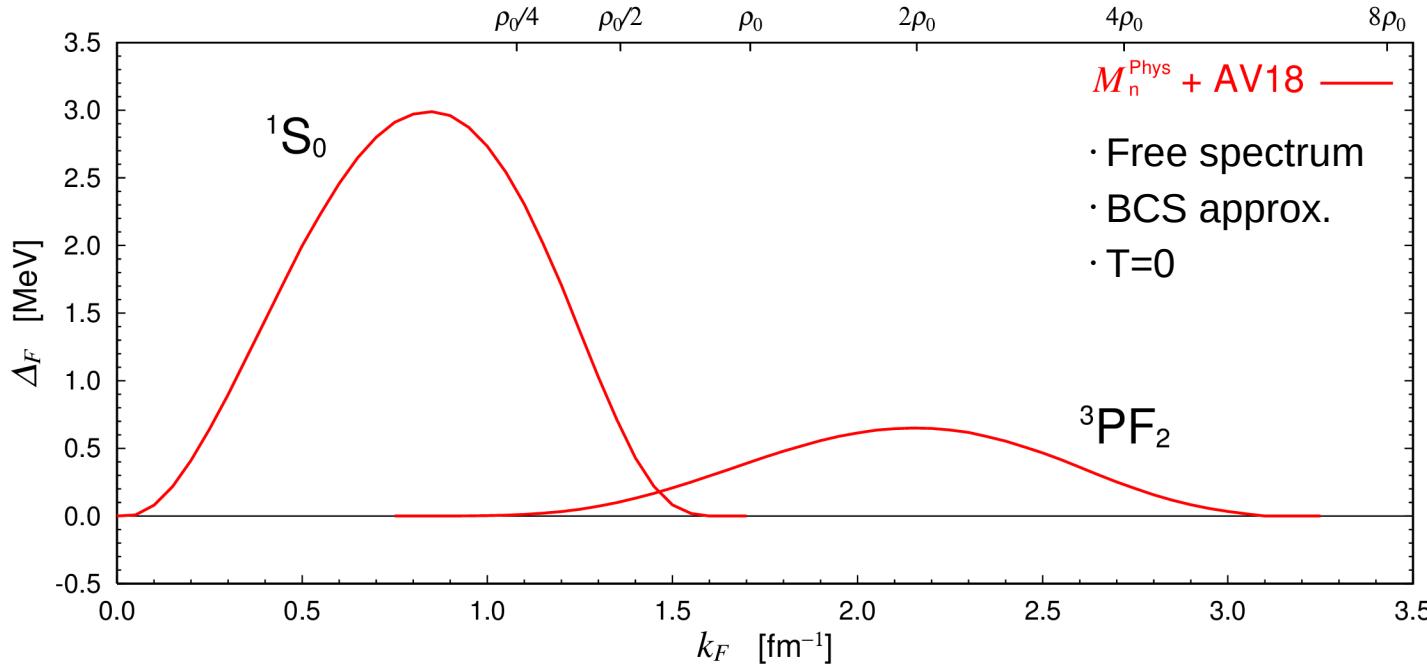
M_B Phys + AV18 NN + LQCD YN, YY



at the normal nuclear density

- LQCD result $U_\Lambda(k) < U_{\Xi}(k) < U_\Sigma(k)$ is **consistent** to data.
- LQCD $U_Y(k)$ are **deeper** than data and model predictions.
- Due to **unphysically** heavy u,d quark and light s quark. (?)

Neutron pairing gap in PNM

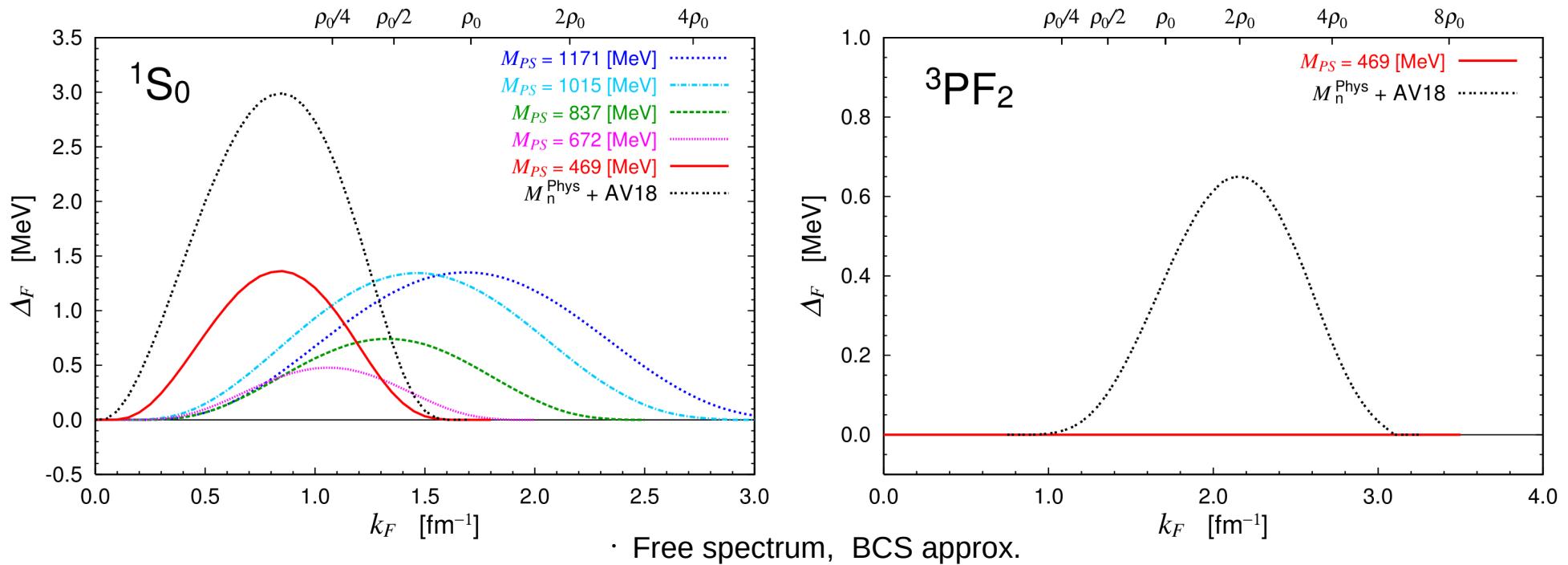


$$\Delta_F = \Delta(k_F) \quad \text{where}$$
$$E(p) = \sqrt{\epsilon(p)^2 + \Delta(p)^2}$$

Elementary excitation (Bogolon) spectrum

- Neutron **superfluid** may exist in crust and core of NS due to paring gap in ${}^1\text{S}_0$ and ${}^3\text{PF}_2$ channel, respectively.
T. Takatsuka and R. Tamagaki, Prog. Theo. Phys. 46 (1971) 114, Suppl. 112 (1993) 27
- Surface superfluid may be origin of the **glitch** phenomenon.
- Core superfluid affects ν production rate and **cooling rate**.
 - It is already observed in NS in Cassiopeia A (?)

Neutron pairing gap from QCD



- Left: $^1\text{S}_0$ pairing gap in PNM at T=0.
 - QCD derive **finite gap** at all the five m_q . → **Super**
 - Nontrivial m_q dependence. Peak moves to lower density.
- Right $^3\text{P}_F$ pairing gap in PNM at T=0.
 - QCD derive **no gap** at that quark mass. → **Normal**

Summary and Outlook

まとめと展望

- ★ 中性子星とバリオン物質と格子QCDの関係
 - ・バリオン物質の高密度での状態方程式の必要性
 - ・実験データが不足しているハイペロン力の必要性
 - ・格子QCDの直接数値計算の困難
- ★ HALQCDアプローチで中性子星への例
 - ・クオークが重い世界で格子QCD数値計算 \Rightarrow 核力の導出。
 - ・BHF で EoS の計算。SNMの飽和性を再現。
 - ・TOV方程式 \Rightarrow M-R 曲線。最大質量のクオーク質量依存性。
 - ・ハイペロンの出現や超流動の有無の研究にも有力。
- ★ 今日紹介した例は第一歩に過ぎない(要改善な点が多くある)。今後このアプローチを発展させる事によって、より確かな基礎を基に中性子星の理論研究が可能になる時代が来ると信じている。
 重いクオーク、足りない部分波、平均場 etc.