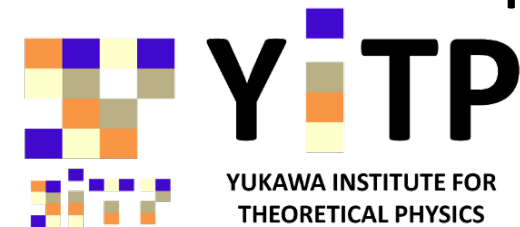


# ブラックホール・中性子星 連星からの重力波と 状態方程式の影響

Yukawa Institute of Theoretical Physics,  
Kyoto University D3



[Koutarou Kyutoku \(久徳 浩太郎\)](#)

Kyutoku, Shibata, Taniguchi PRD 82 (2010) 044049

Kyutoku, Okawa, Shibata, Taniguchi PRD 84 (2011) 064018

# Black hole-neutron star binaries

- Ones of **the most promising GW sources**
  - emit 1-a few kHz GWs just before the merger
  - fairly promising for ground-based detectors
  - a robust test of GR / **a new prove for the NS**
- Possible candidates of **the short GRB engine**
  - merger scenario  $\leftrightarrow$  accretion disk formation
- A candidate of **the r-process environment**

(do not go into detail today)

# Gravitational-wave detectors



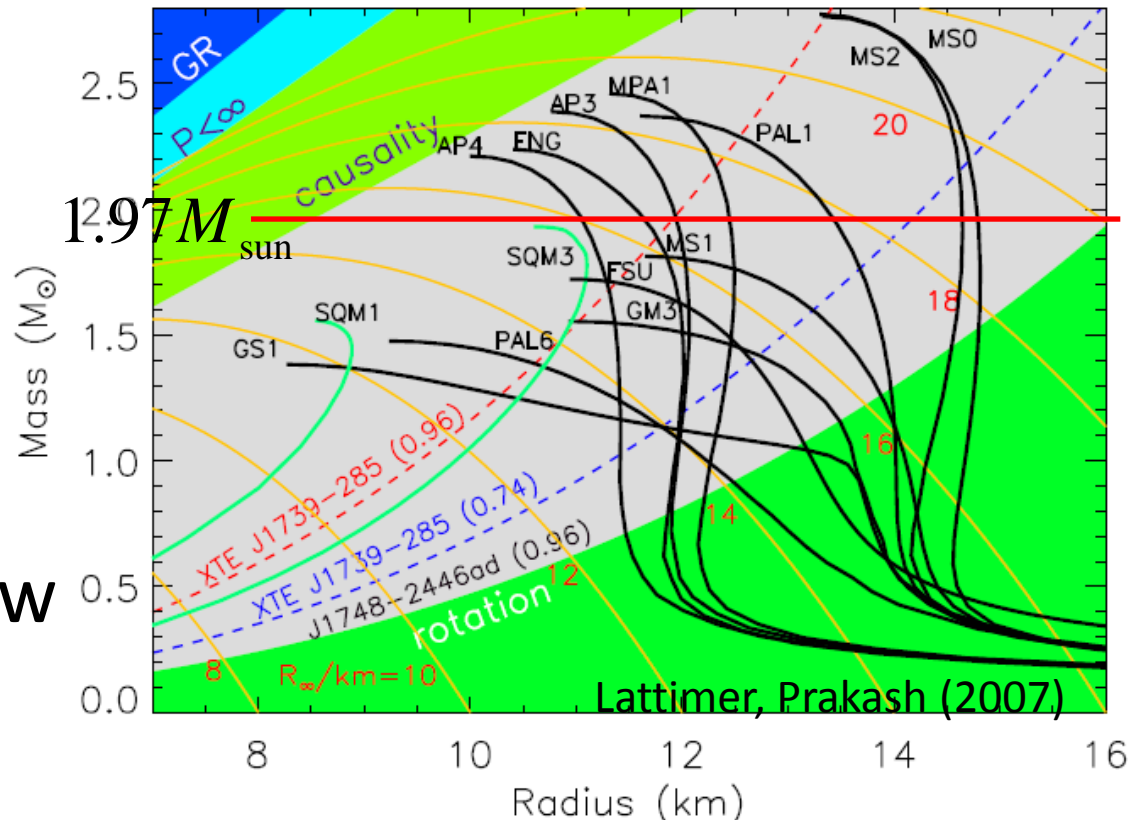
Sensitive in 10-1000Hz  
... astrophysical sources



# Neutron star equations of state

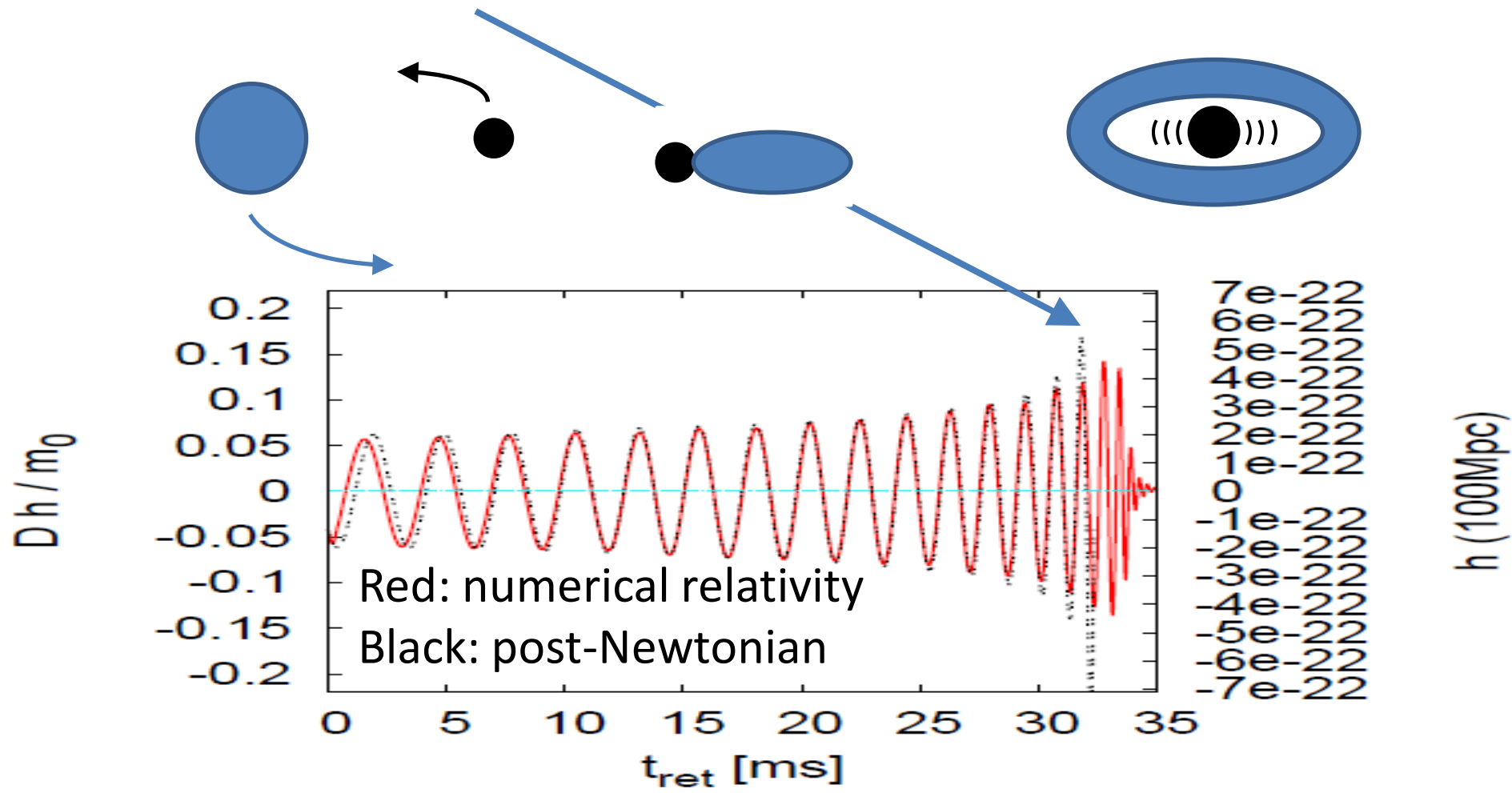
- The EOS at high density is not confirmed yet
- NS radii are determined by the cold ( $T=0$ ) EOS, but not constrained accurately by (X-ray) observ.

- Can we determine the NS radius by GW observation?
- We can obtain the EOS if we know the M-R relation



# Typical GWs from BH-NS binaries

- Classified as inspiral-**merger**-ringdown (if any)



# Importance of numerical relativity

- Appropriate methods differ among the three phases
  1. inspiral phase ... post-Newtonian approx.
  2. merger phase ... numerical relativity  
strong (=nonlinear) gravity, hydrodynamics
  3. ringdown phase ... BH perturbation technique
- Numerical relativity is the unique approach for the merger phase of compact binary coalescences
- **Tidal disruption of the NS** determines the GWs and properties of the remnant disk, such as the mass

# Advantages of binary GW observation

- Less systematic errors than EM observation
  - the largest model is the EOS and GR itself
- The dynamics **before** the merger is nearly free of the finite-temperature effects, magnetic fields...
  - **in BH-NS, all GWs are determined by T=0 EOSs**
  - (- in NS-NS, hypermassive NSs also emits GWs)
- The early inspiral gives us different information
  - masses of each component, the BH spin

# When the tidal disruption occurs?

- Two nondimensional parameters are important
  - Mass ratio of BH/NS  $Q = M_{\text{BH}} / M_{\text{NS}} \geq 1$
  - NS compactness  $C = M_{\text{NS}} / R_{\text{NS}} \sim 0.15 - 0.2$

tidal disruption occurs outside the ISCO if the mass ratio  $Q$  and/or compactness  $C$  are small

**= the small BH mass and/or the large NS radius**

∴ tidal effect is a finite size effect of the NS

- **The large BH spin  $a \equiv S_{\text{BH}} / M_{\text{BH}}^2$  is also favored**

∴ The ISCO radius is small for a large BH spin



# The formulation and methods

- Solve  $G_{ab} = 8\pi T_{ab}, \nabla_b T^b_a = 0, \nabla_a(\rho u^a) = 0$
- Compute initial conditions
  - the spectral method library LORENE  
<http://www.lorene.obspm.fr/>
  - developed new code for the BH spin / NS EOS
- Perform simulations of time evolution
  - AMR code SACRA developed in our group  
Yamamoto, Shibata, Taniguchi PRD (2008) 78 064054
- EOSs closes the system of equations

# The piecewise polytrope (PWP)

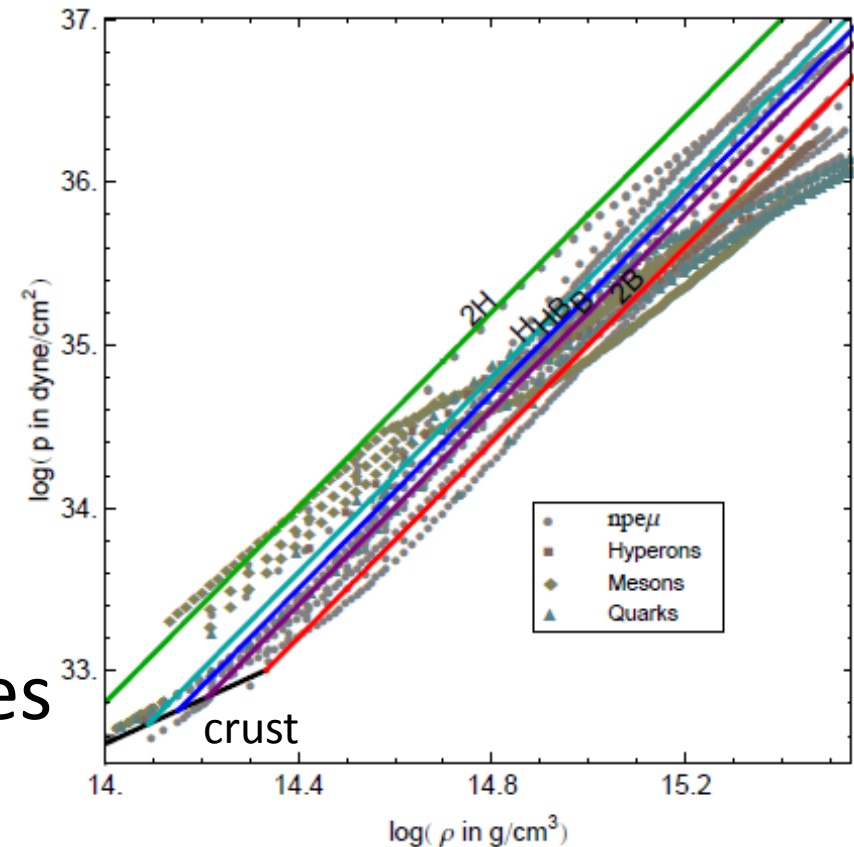
- T=0, nuclear-theory based EOSs are approximated by analytic broken-polytropes

$$P = \begin{cases} \kappa_1 \rho^{\Gamma_1} & (\rho < \rho_1) \sim \text{crust} \\ \kappa_2 \rho^{\Gamma_2} & (\rho > \rho_1) \sim \text{core} \end{cases}$$

- less computational costs
- only a few parameters

- Thermal effects are incorporated by ideal gases

$$P_{\text{th}} = (\Gamma_{\text{th}} - 1) \rho \varepsilon_{\text{th}}$$



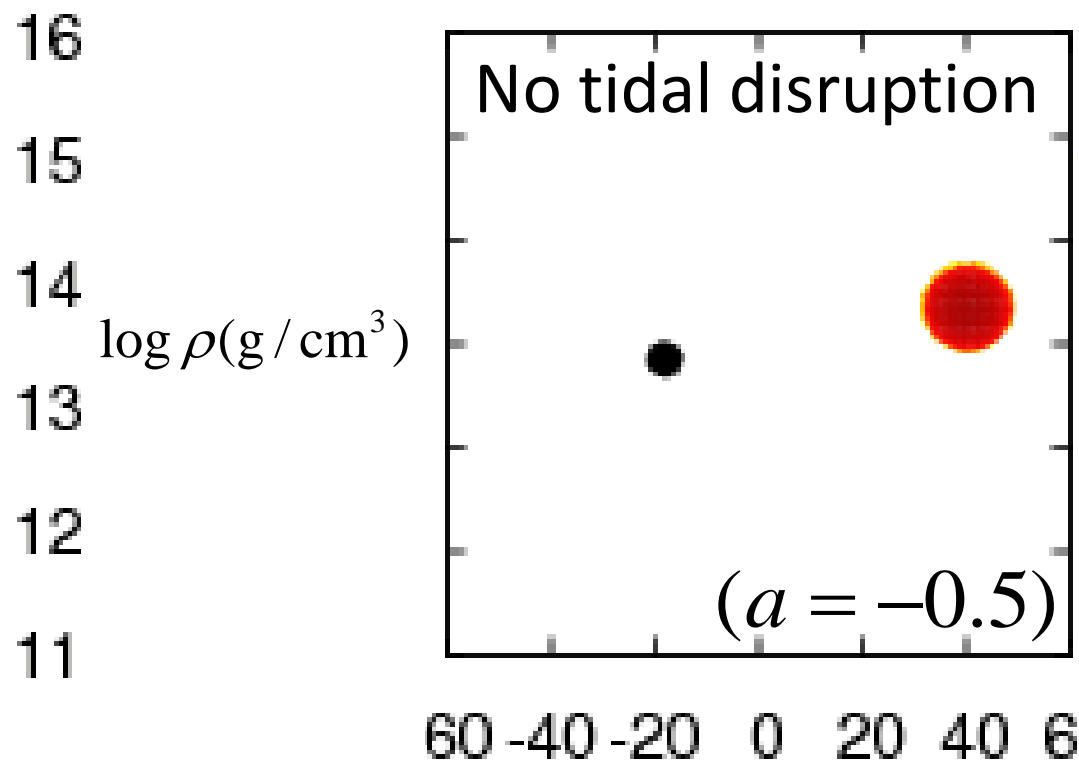
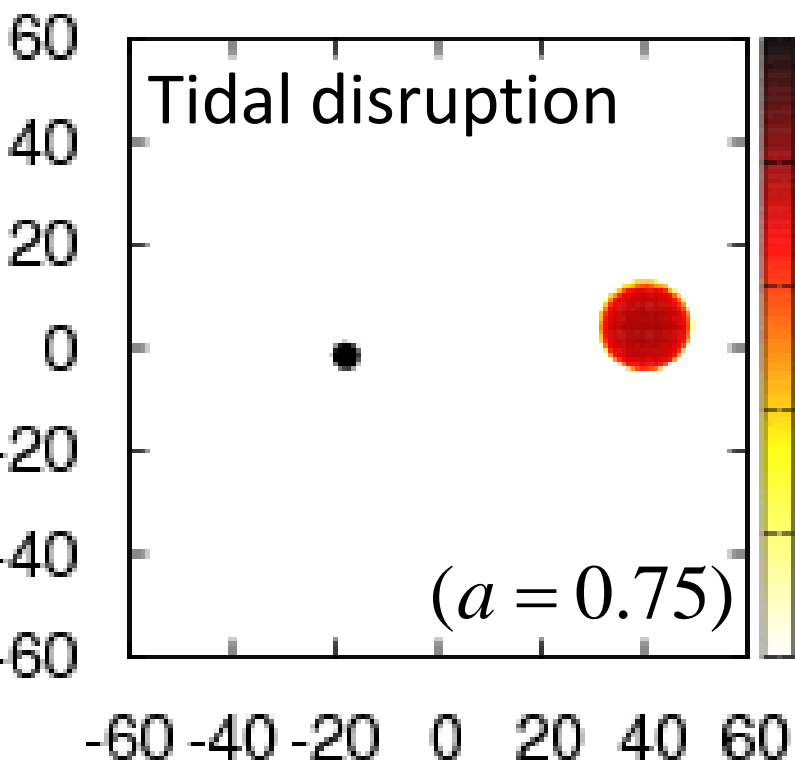
# Comparison of tidal disruption

- (only the BH is different in this example)

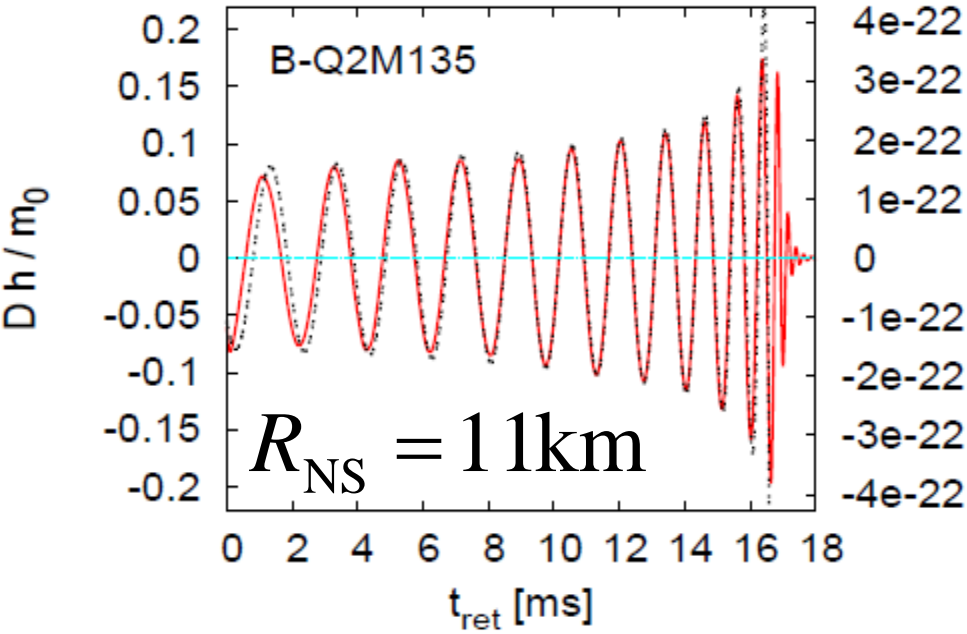
$$M_{\text{NS}} = 1.35M_{\text{sol}}, M_{\text{BH}} = 2.7M_{\text{sol}} \quad (Q = 2)$$

$t = 109.7051 \mu\text{s}$

$t = 164.5577 \mu\text{s}$

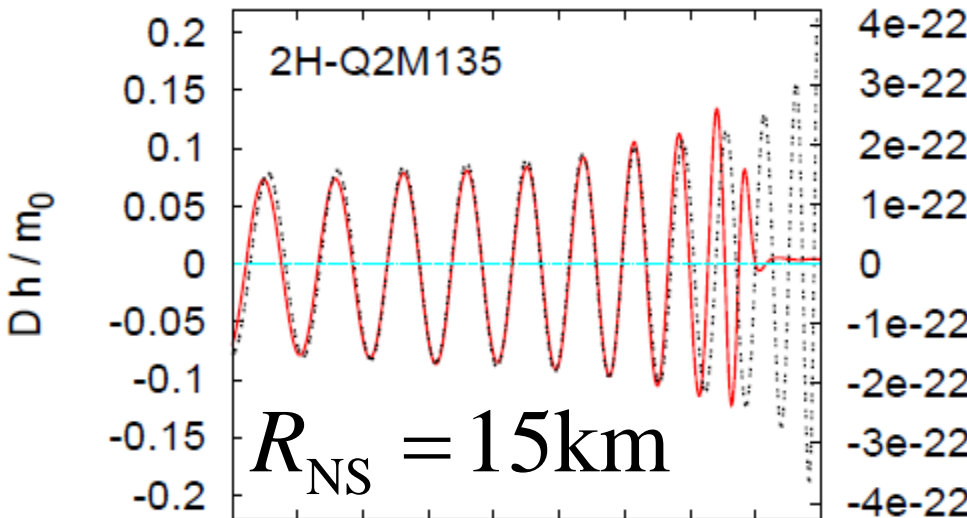


# GWs: differences due to the EOS



$M_{\text{BH}} = 2.7 M_{\text{sol}}$   
 $M_{\text{NS}} = 1.35 M_{\text{sol}}$   
 $a = 0$

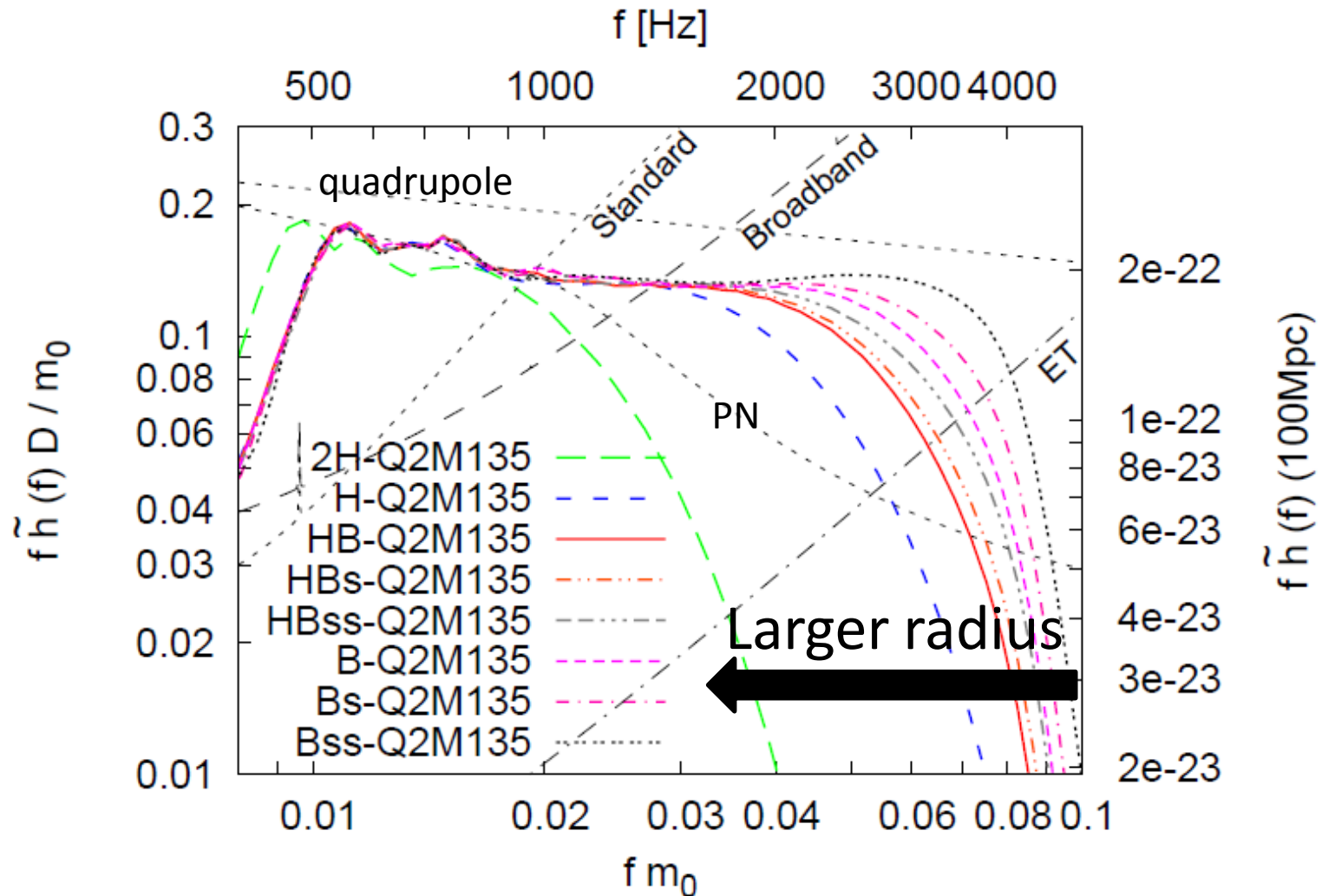
Top: soft EOS  
the small NS radius  
weak disruption



Bottom: stiff EOS  
the large NS radius  
strong disruption

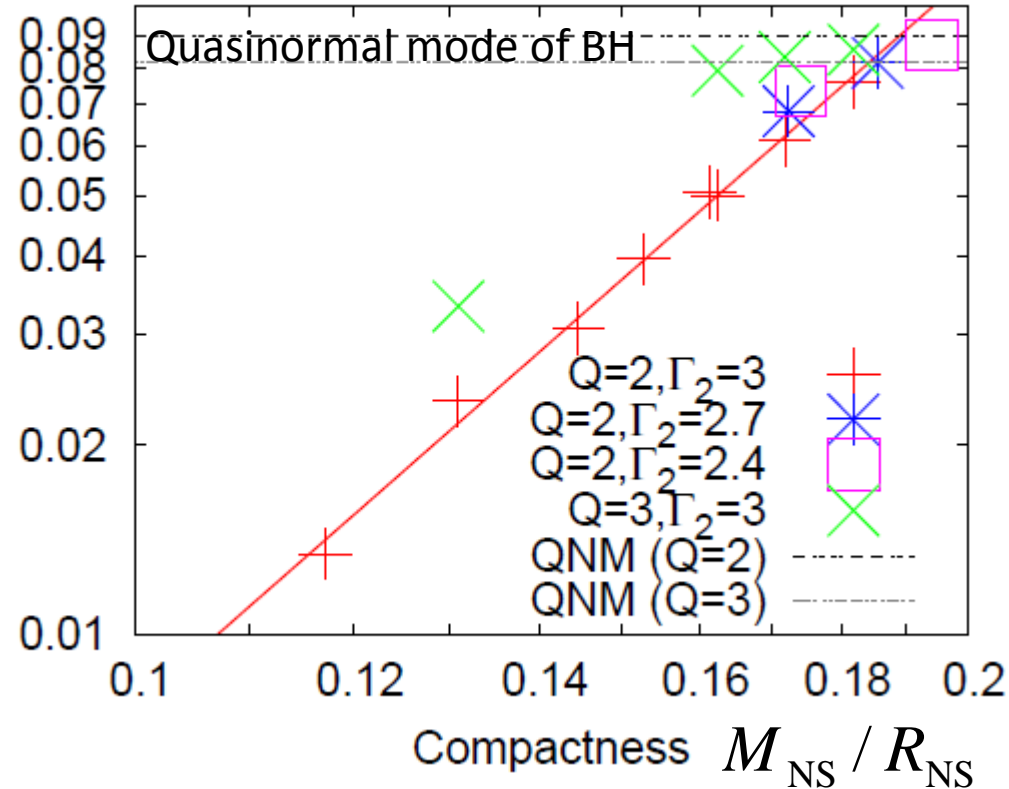
# The GW spectrum

- $M_{\text{NS}} = 1.35 M_{\text{sol}}, M_{\text{BH}} = 2.7 M_{\text{sol}} (Q = 2), a = 0$



# Compactness vs cutoff frequency

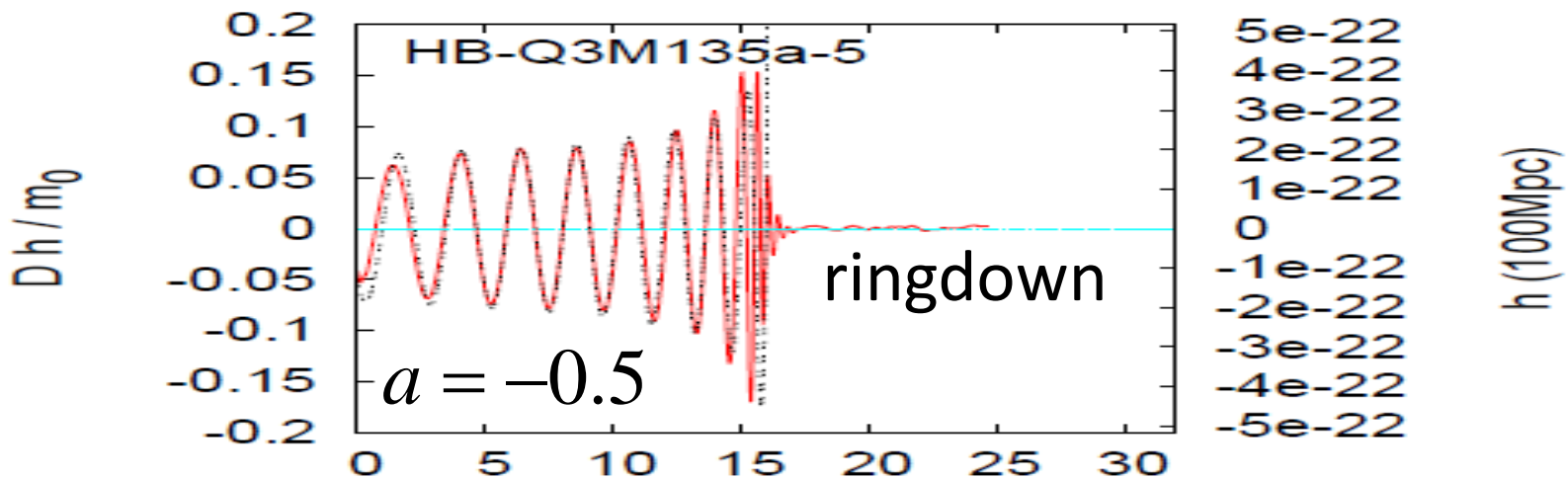
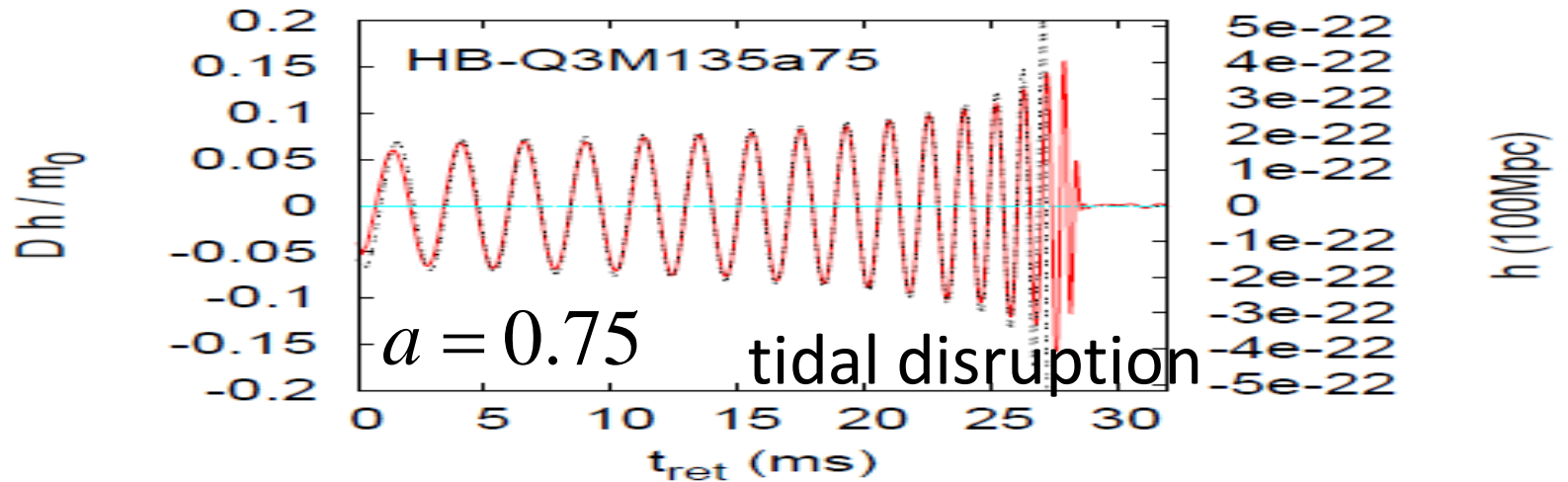
- $a = 0$  cases
- Strong correlations  
= **The NS radius**  
**can be read off**  
**from GW observ.**



- $f_{cut} m_0 \propto C^4$  when tidal disruption occurs
- $Q \geq 3$  ( $M_{BH} \geq 4.05 M_{sol}$ ) seems to bring no tidal disruption -> an unrealistically story?

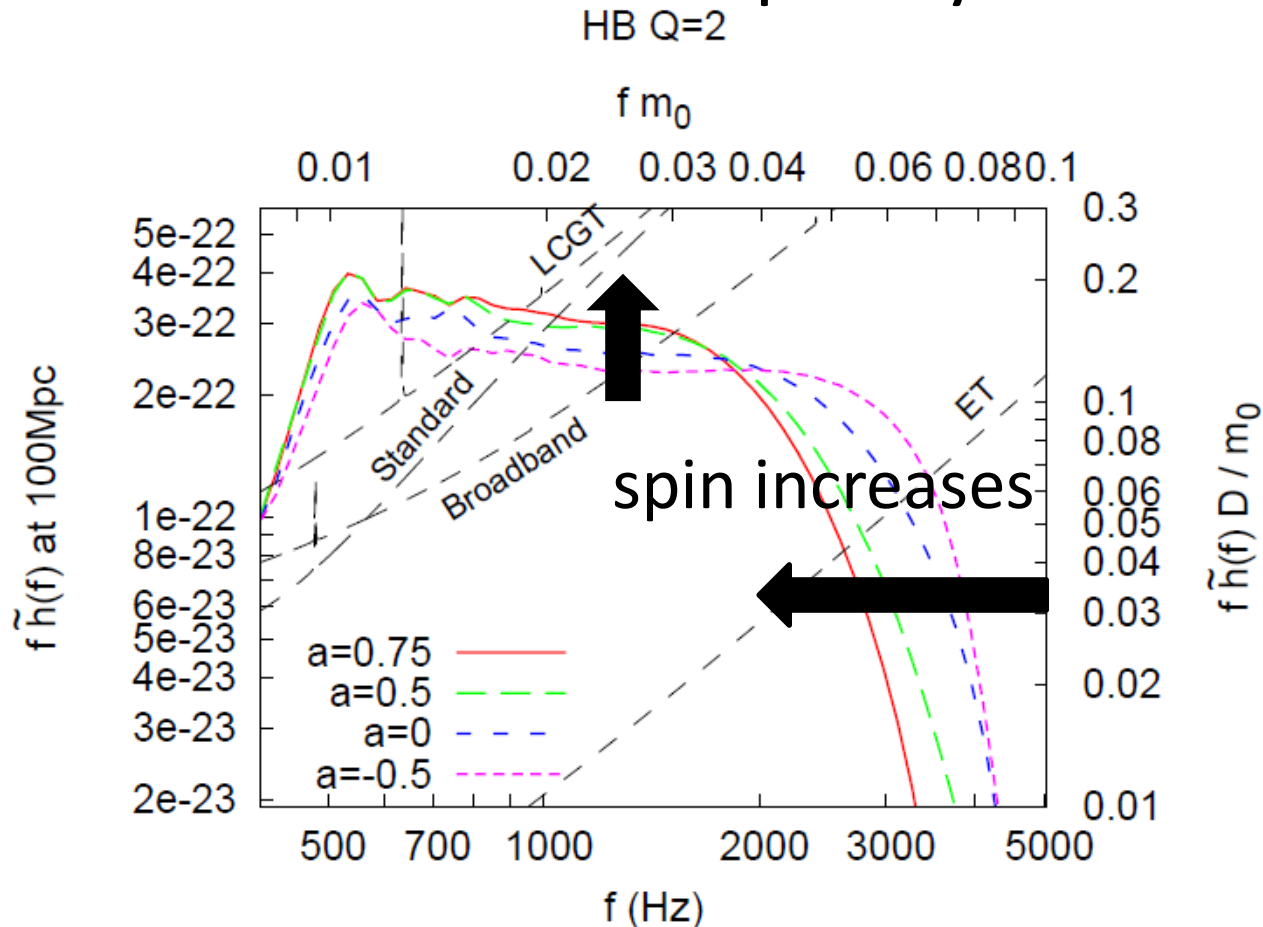
# GWs: difference due to the BH spin

- Strong if the BH spin is parallel to orbit.ang.mom.



# Changes of spectra due to the spin

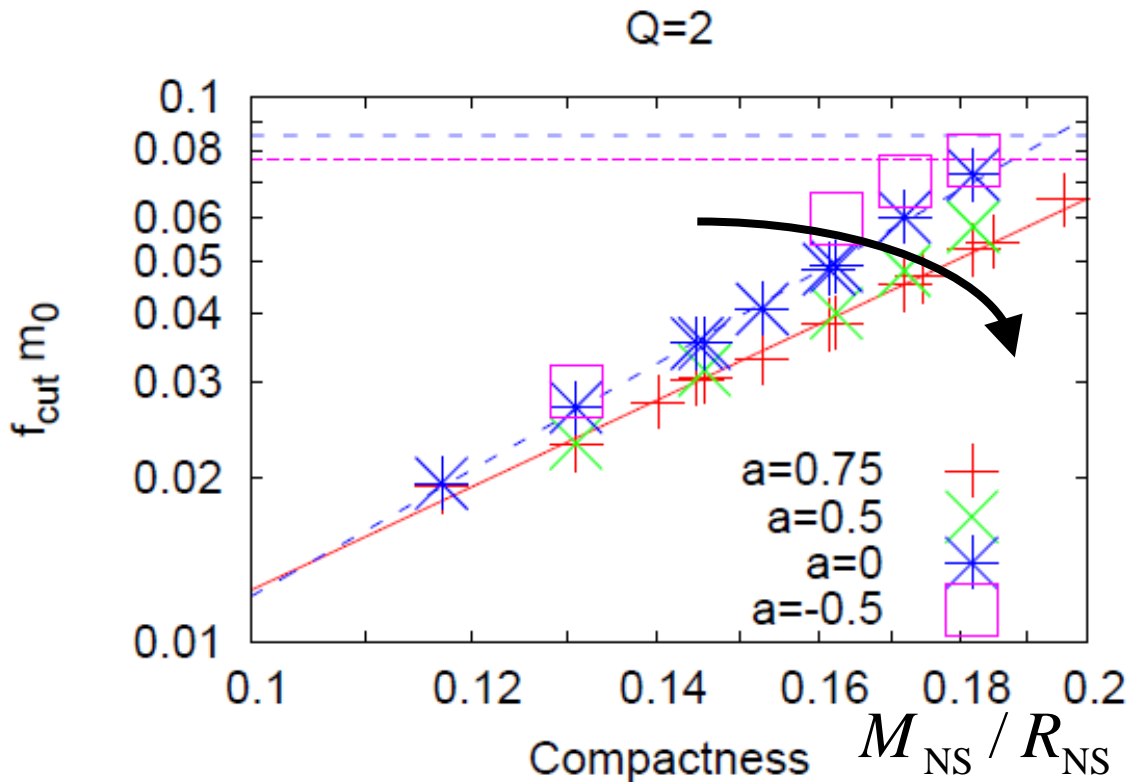
- The large amplitude at low frequency
- Cutoff occurs at lower frequency





# Compactness – cutoff frequency

- **BH spins lower the cutoff frequency**
  - the low frequency is preferred from observ.

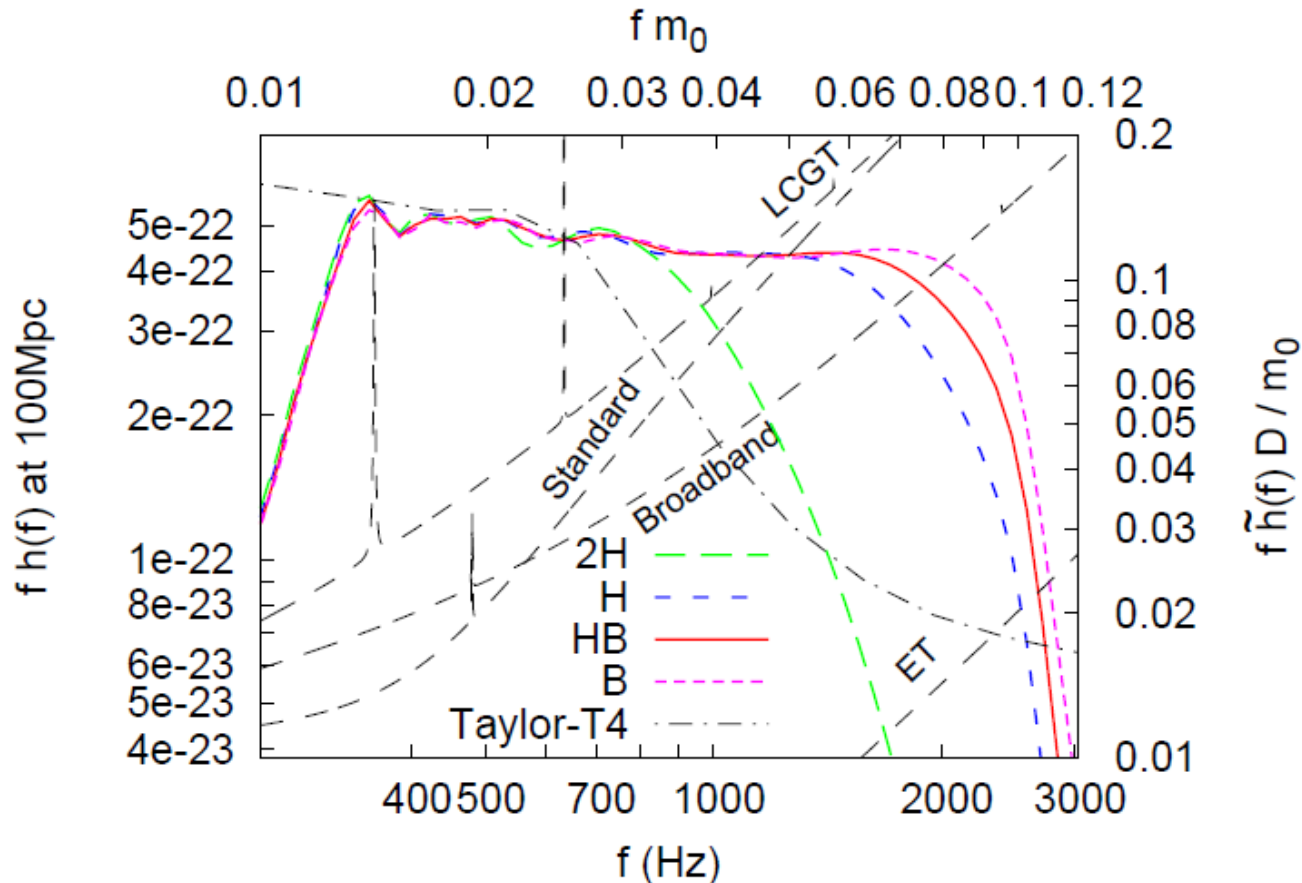


quasinormal modes  
for different BH spins

we have to know  
the BH spin using  
inspiral GWs

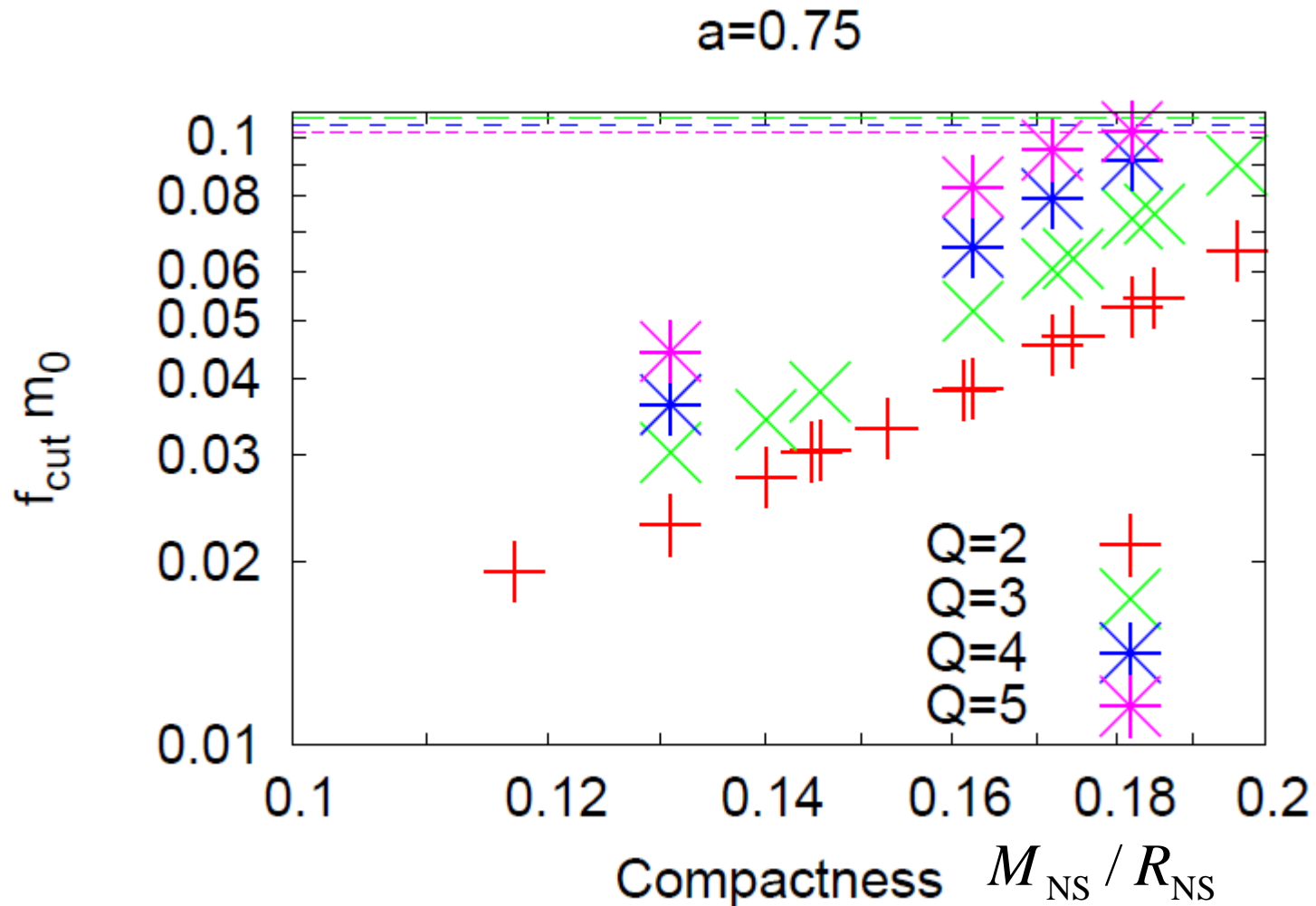
# The GW spectrum for Q=5

- In this case,  $M_{\text{BH}} = 6.75 M_{\text{sol}}$  -> maybe realistic
- Adv. LIGO/LCGT will observe the spectrum cutoff



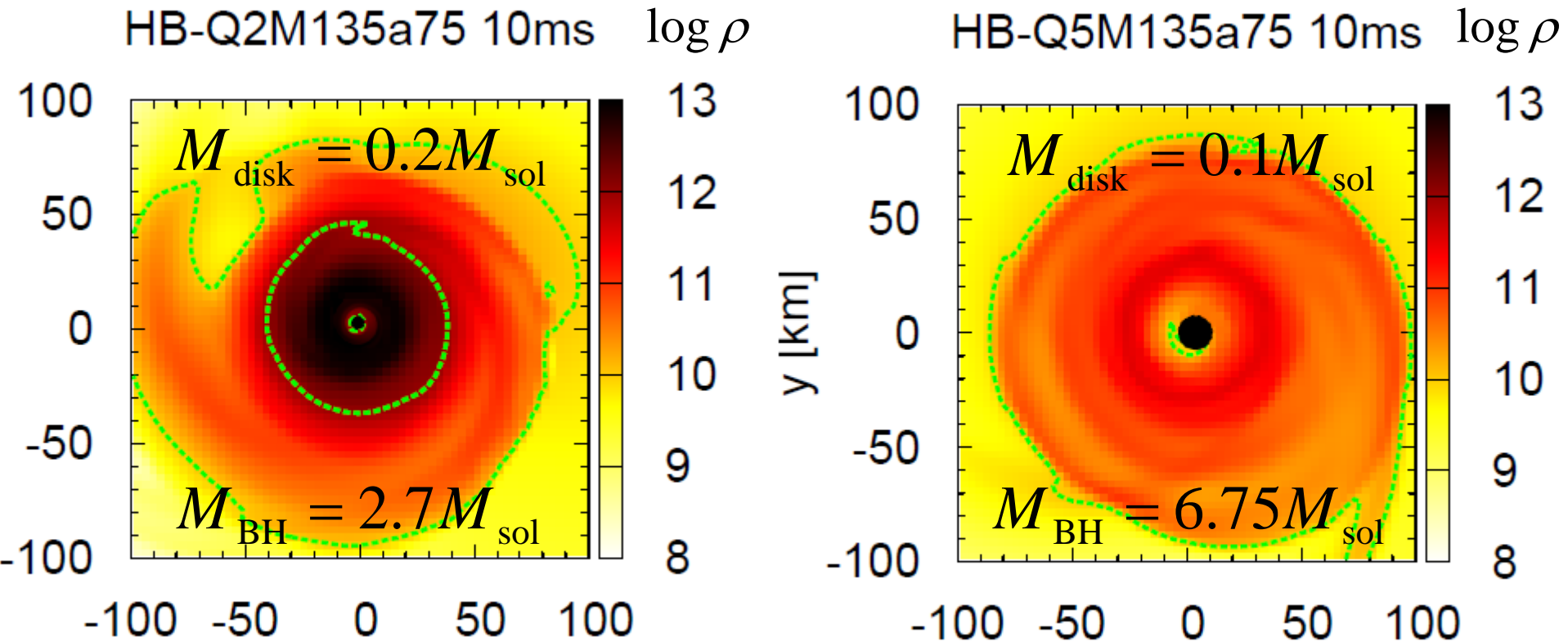
# Cutoff frequencies for $a=0.75$

- Massive (realistic) BH-NS will tell us the NS EOS



# Formed accretion disks

- The mass of the disk can exceed  $0.1M_{\text{sol}}$  when the tidal disruption is strong



# Summary

- We computed gravitational waves from black hole-neutron star binaries by numerical relativity.
- Gravitational waves from black hole-neutron star binaries will tell us the equation of state of neutron star matter, especially when tidal disruption occurs.
- Astrophysically realistic black hole-neutron star binaries will also tell us the equation of state if the BH spin is moderately strong.
- The mass of the accretion disk can be sufficiently high to bring the short-hard gamma-ray burst.

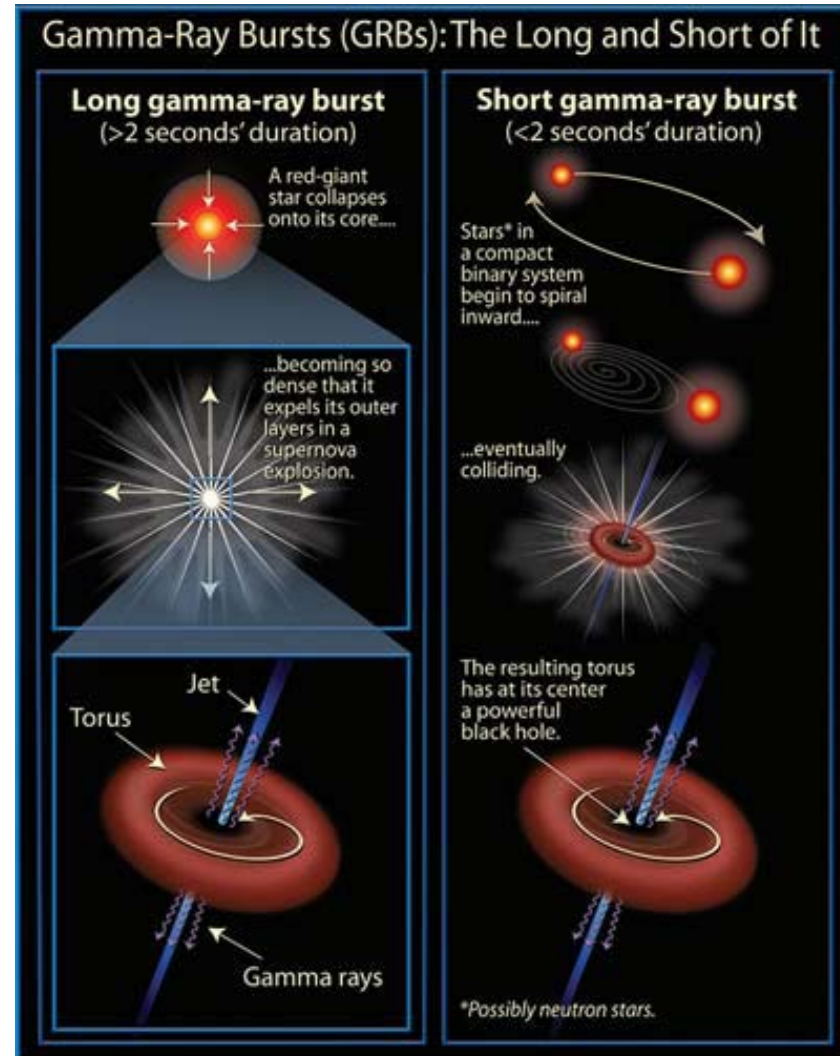
# Future work

- More waveforms for generic configurations
  - an urgent task for the GW astronomy
- Incorporate neutrinos and magnetic fields
  - essential for GRBs, multi-messenger astron.
- Analyze how accurately we can know the EOS
  - the Fisher analysis using numerical relativity
    - Lackey, KK, Shibata, Brady, Friedman PRD submitted

appendix

# Short-hard gamma-ray burst

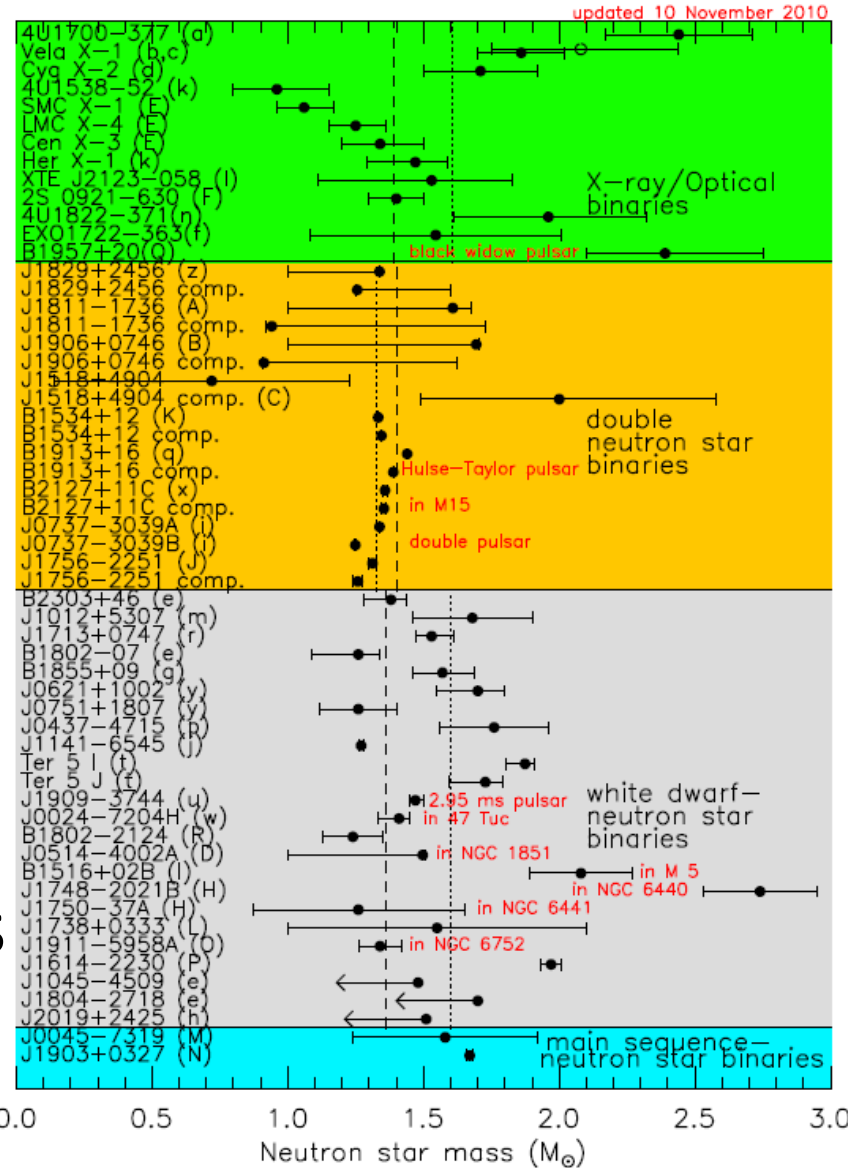
- Release  $10^{49-51}$  erg within  $\sim 2$  s
    - jet opening angle  $\rightarrow ?$
  - BH-accretion disks?
    - LGRB: “collapsar” model
    - **SGRB: merger scenario?**
      - BH-NS or NS-NS**
- Is a massive disk formed?





# The mass of the neutron star

- EOSs are constrained by the NS maximum mass, recently  $1.97M_{\odot}$  found
- Radius measurement is fairly difficult
  - degeneracy w/ distance
  - rad./atmosphere models



# Lattimer & Prakash (2007)

If the observed peak flux is approximately the Eddington flux, if the opacity and color correction factor are well-understood, if the quiescent flux observed in-between bursts is thermal emission with a measurable temperature  $T_\infty$ , and if spectral features are observed which permit a determination of the object's redshift, these multiple observations then contain the information needed to identify uniquely the mass and the radius of a single star. To make this clear, combine Eqs. (62), (64) and (66):

$$M = \frac{c^5}{4G\kappa} \frac{\alpha}{F_{edd,\infty}} [1 - (1+z)^{-2}]^2 (1+z)^{-3},$$

$$R = \frac{c^3}{2\kappa} \frac{\alpha}{F_{edd,\infty}} [1 - (1+z)^{-2}] (1+z)^{-3},$$

$$z = \left(1 - \frac{2GM}{Rc^2}\right)^{-1/2} - 1 \quad (62) \quad F_{edd,\infty} = \frac{cGM}{\kappa d^2} \sqrt{1 - 2GM/Rc^2} \quad (64)$$

$$F_\infty / (\sigma T_\infty^4) = (T_{eff}/T_\infty)^4 R^2 d^{-2} (1 - 2GM/Rc^2)^{-1} \quad (66)$$

$$\alpha = (T_\infty/T_{eff})^4 F_\infty / (\sigma T_\infty^4) = (R_\infty/d)^2$$