

# Calculation of Transition Strength of Nuclei

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2. Density functional theory and QRPA
3. Spherical nuclei
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Dec. 5, 2011  
Shima

# 1. Motivation and purpose

One of the goals of nuclear physics :

to establish theoretical methods to describe all properties of  
all nuclei



To establish capability to supply other fields including  
nuclear astrophysics with the nuclear data they need.

My basic idea : application is very important.

The purpose of my research :

to calculate as many transition strengths and energies of  
nuclei as possible using density functional theory and  
Search reliable nuclear density functional

## 2. Density functional theory (DFT)

Energy density functional

$$\langle \hat{H} \rangle = \int d^3\vec{r} \mathcal{H}(\rho(\vec{r})) = E[\rho]$$

Dynamical equation

$$\frac{\delta}{\delta\rho} E[\rho] = 0 \rightarrow \text{technically mean-field eq.}$$

The density functional which I use: Skyrme-type

Most parts are contact interaction  $\delta(\vec{r}_1 - \vec{r}_2)$ .

- volume term  $\propto \delta(\vec{r}_1 - \vec{r}_2)$
- momentum<sup>2</sup>  $\delta(\vec{r}_1 - \vec{r}_2)$  (gradient approximation)
- spin-orbit term  $\propto \delta(\vec{r}_1 - \vec{r}_2)$
- density-dependent term  $\rho(\vec{r}_1)^\alpha \delta(\vec{r}_1 - \vec{r}_2)$
- Coulomb term (exchange term in Slater approximation)

The previous dynamical equation → ground state

Derivation of dynamical eq. for excited states:

- Extend to time-dependent formulation. Introduce fluctuation around the ground state.
- Assume the time dependence of the fluctuation as  $e^{i\omega t}$ .
- Neglect many-body many-hole correlations



Dynamical eq. of random-phase approximation (RPA).

Solutions are stationary states.

Add pairing energy density (contact interaction, volume type)



Quasiparticle RPA (QRPA)

### 3 . Spherical Nuclei

#### Strength function

$$S_J(E) = \sum_k \sum_{M=-J}^J \left| \langle \Psi_k | \hat{F}_{JM} | \Psi_0 \rangle \right|^2 L_k(E)$$

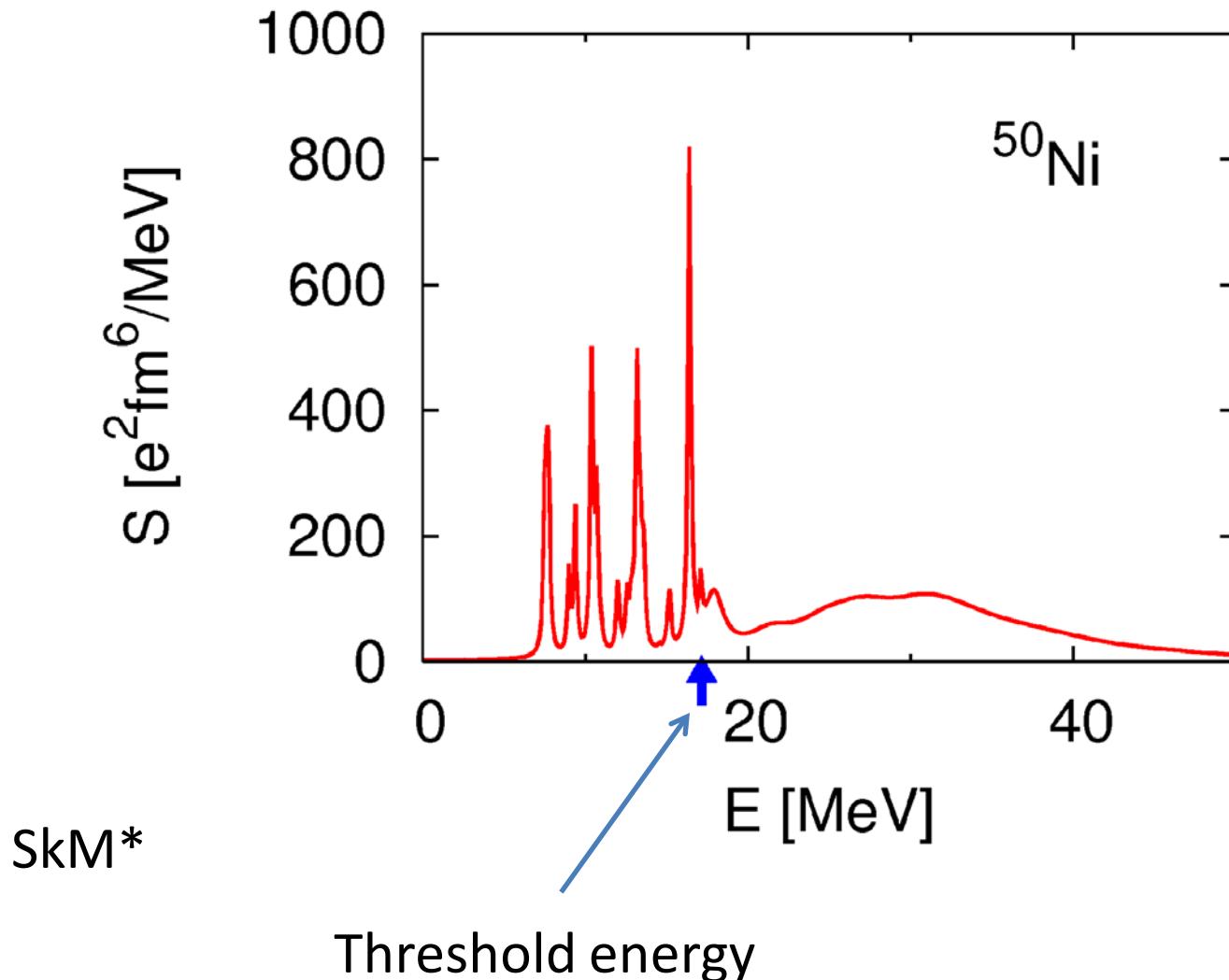
#### Transition operator

Isoscalar     $e \frac{Z}{A} \sum_{i:\text{nucleons}} f_J(r_i) Y_{JM}(\Omega_i)$

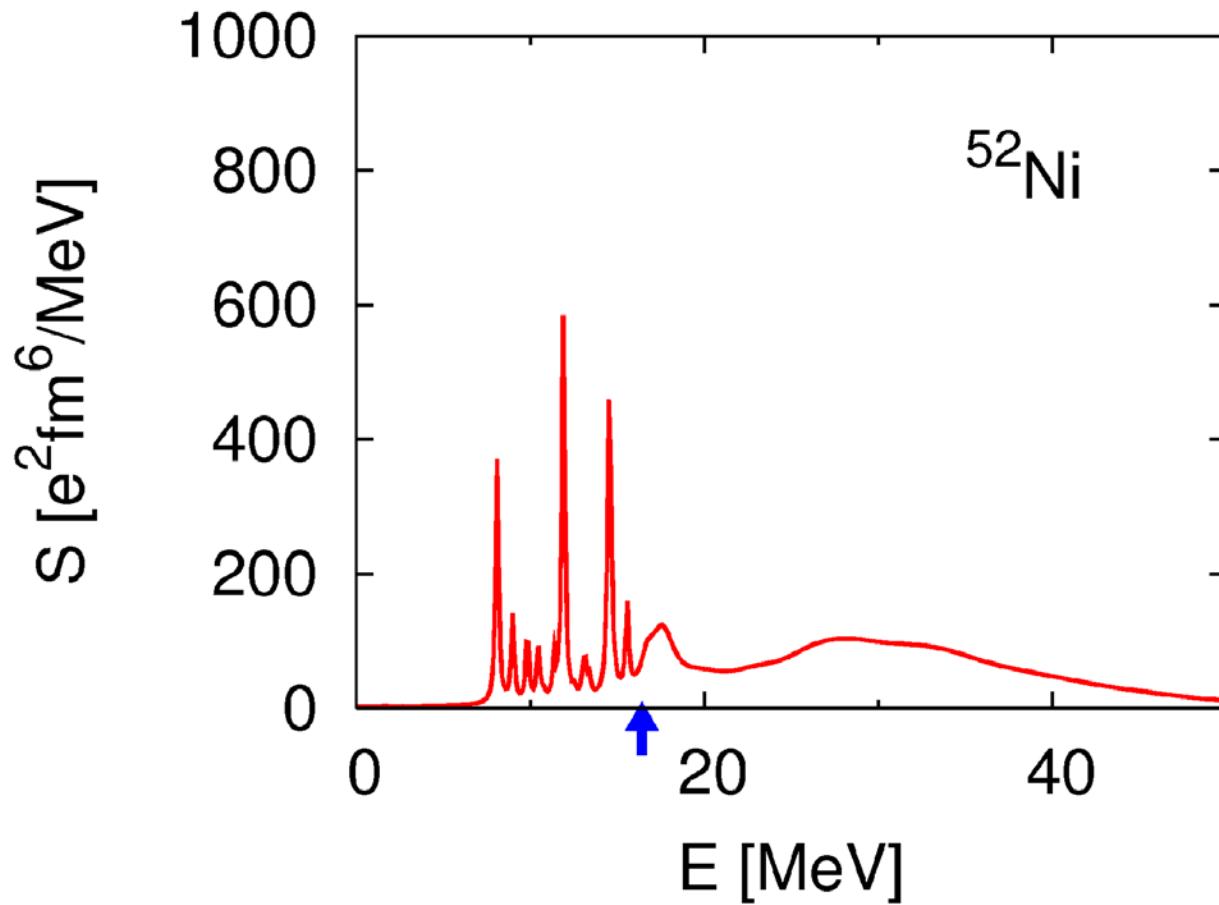
Isovector     $e \frac{N}{A} \sum_{i:\text{proton}} f_J(r_i) Y_{JM}(\Omega_i) - e \frac{Z}{A} \sum_{i:\text{neutron}} f_J(r_i) Y_{JM}(\Omega_i)$

$$f_J(r_i) \propto r_i^n$$

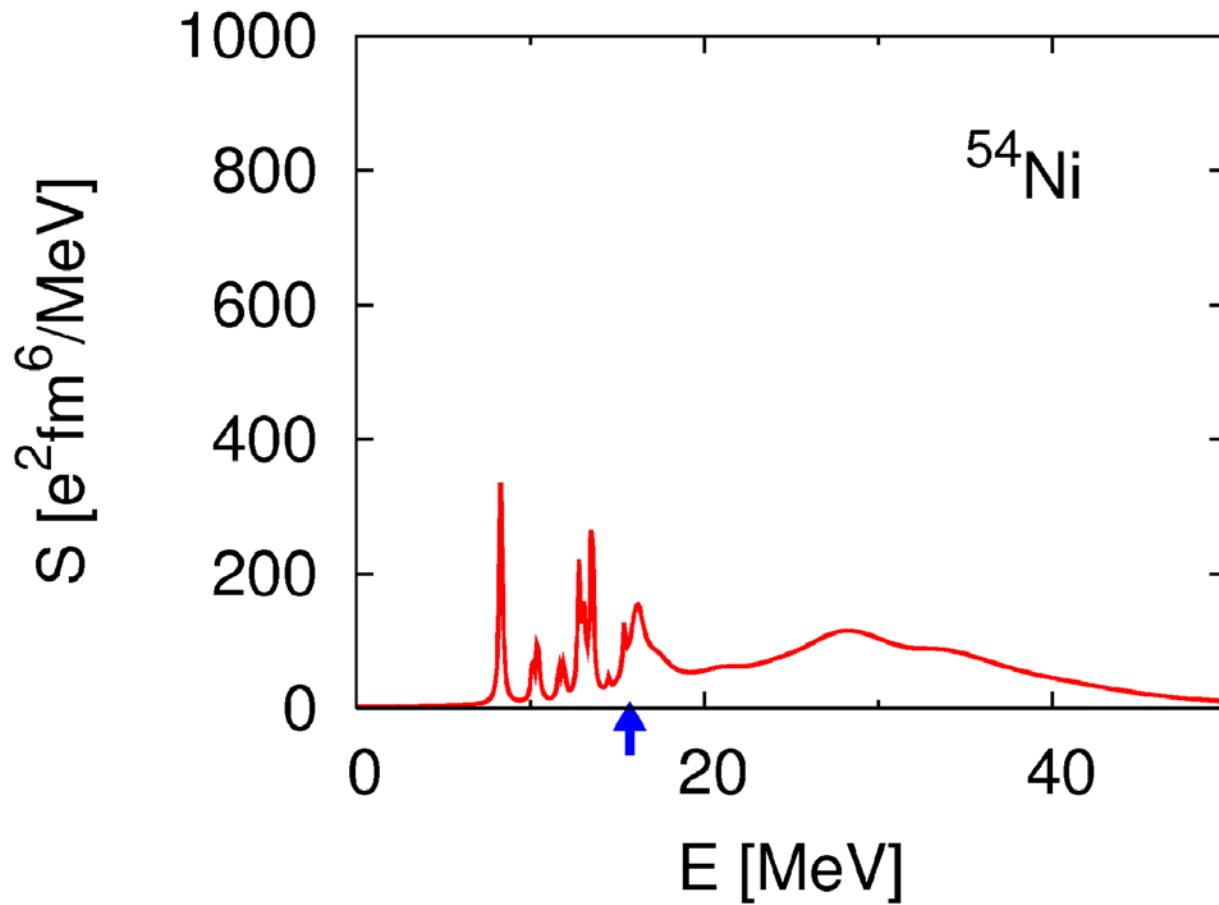
# Isoscalar $1^-$ strength functions



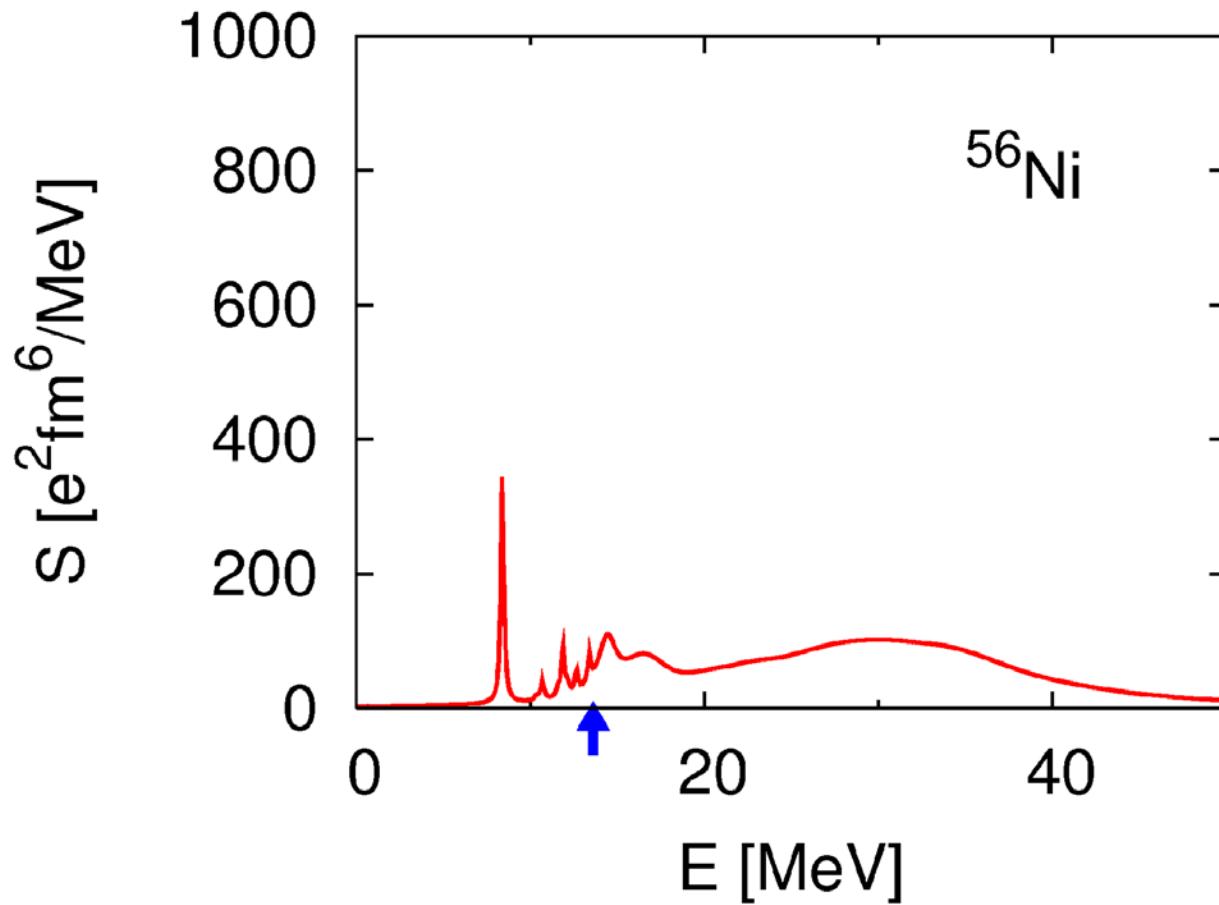
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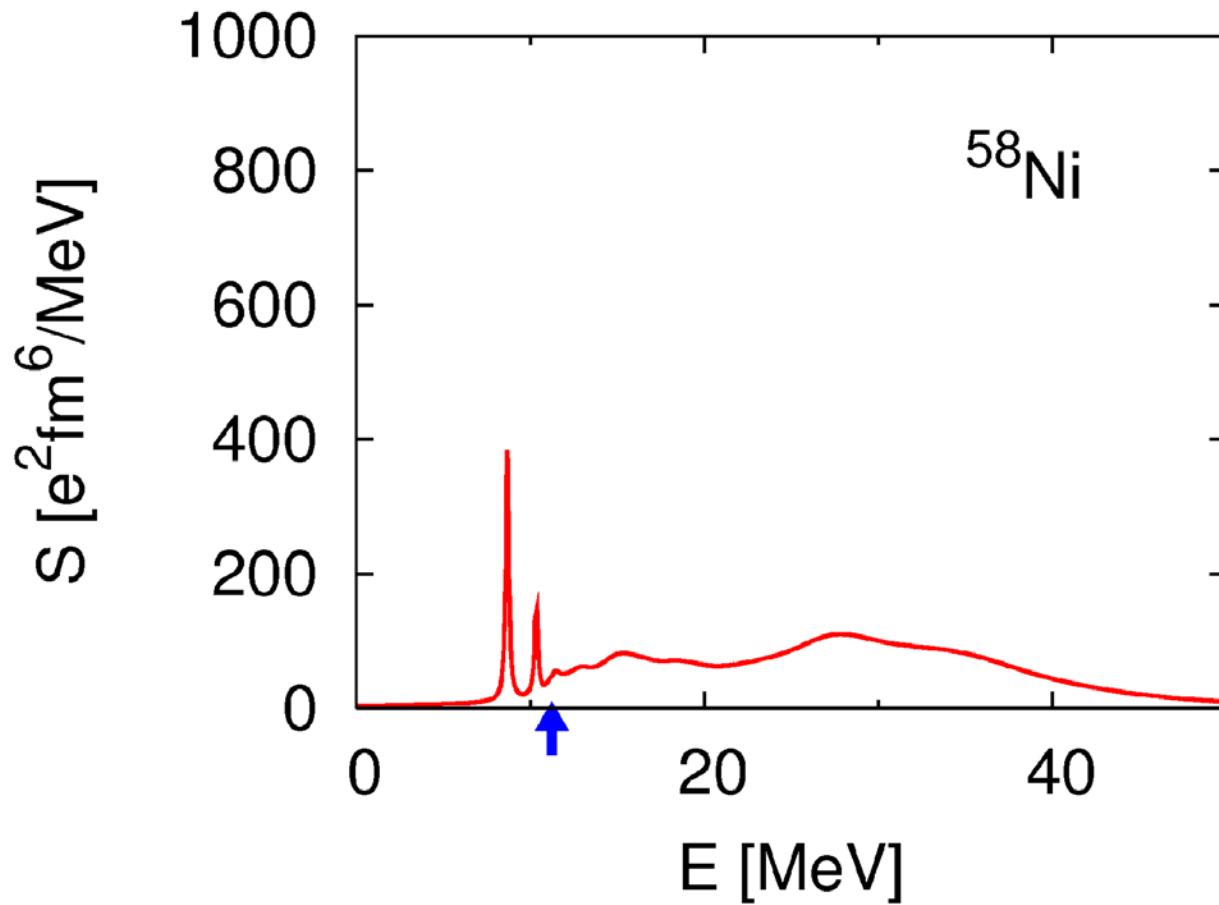
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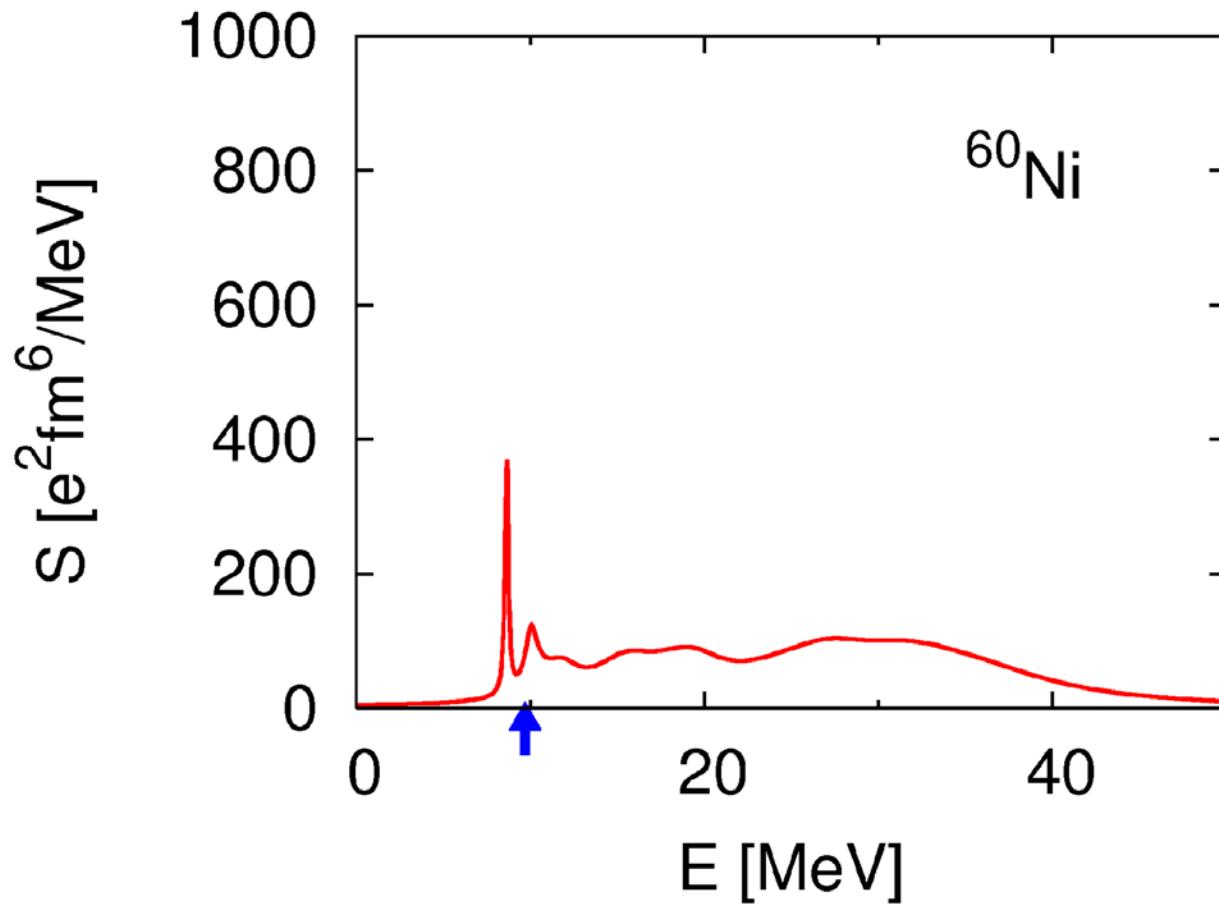
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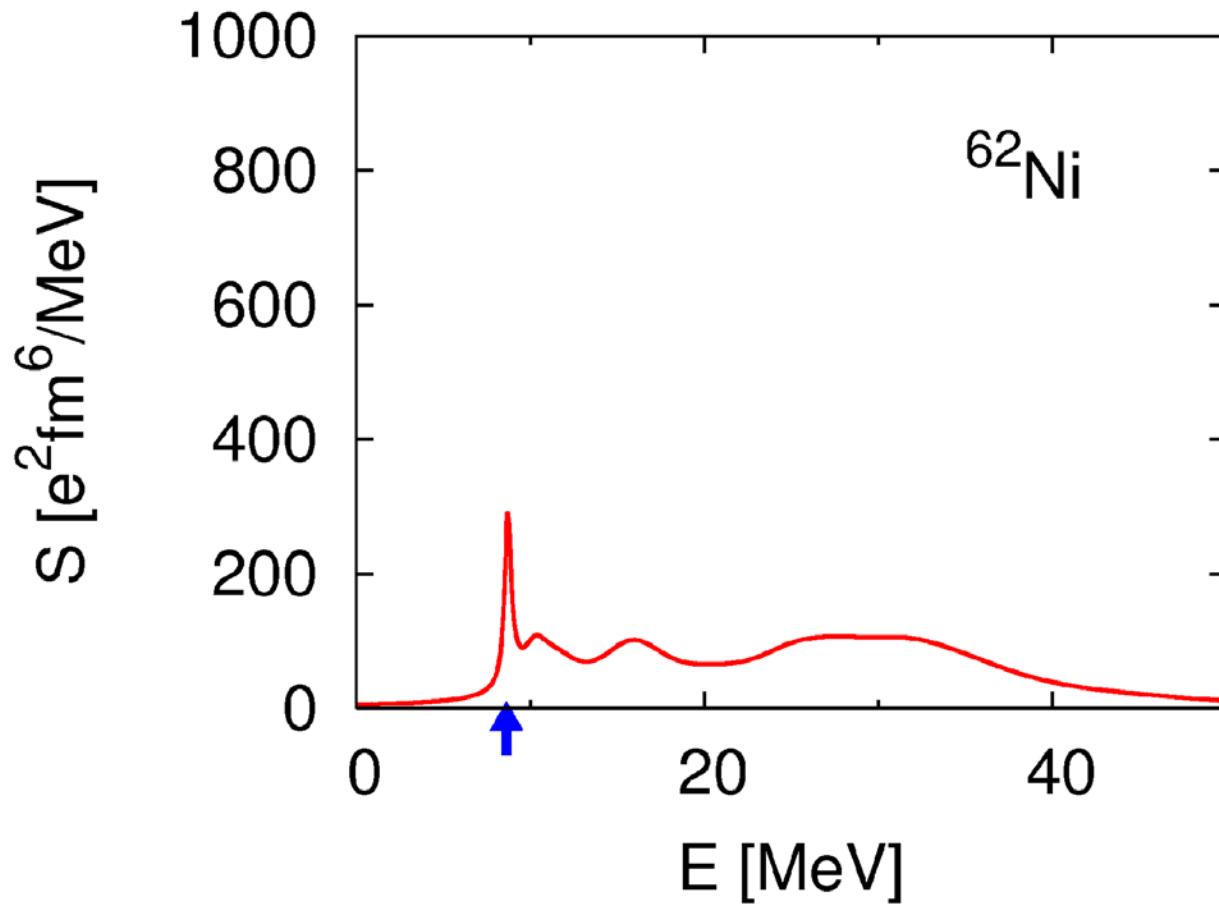
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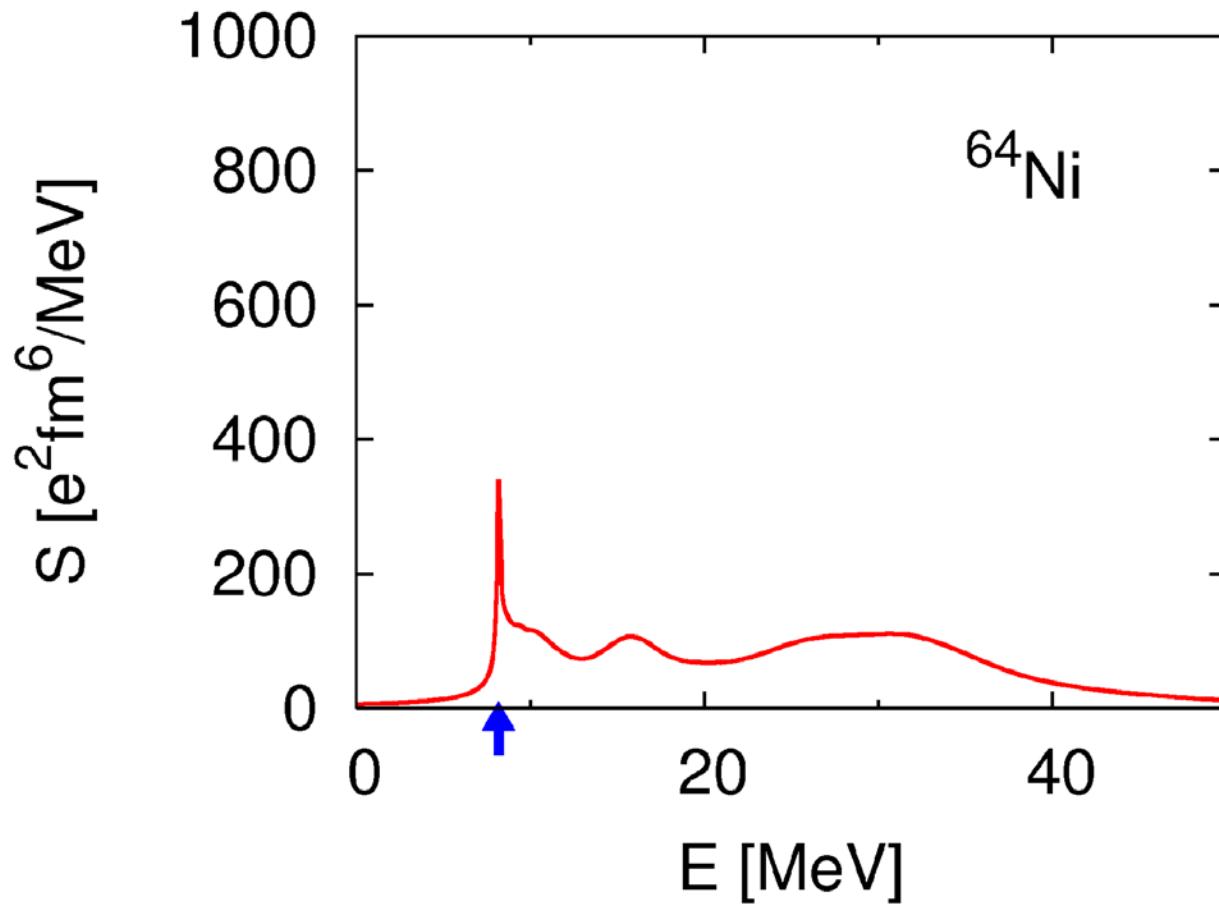
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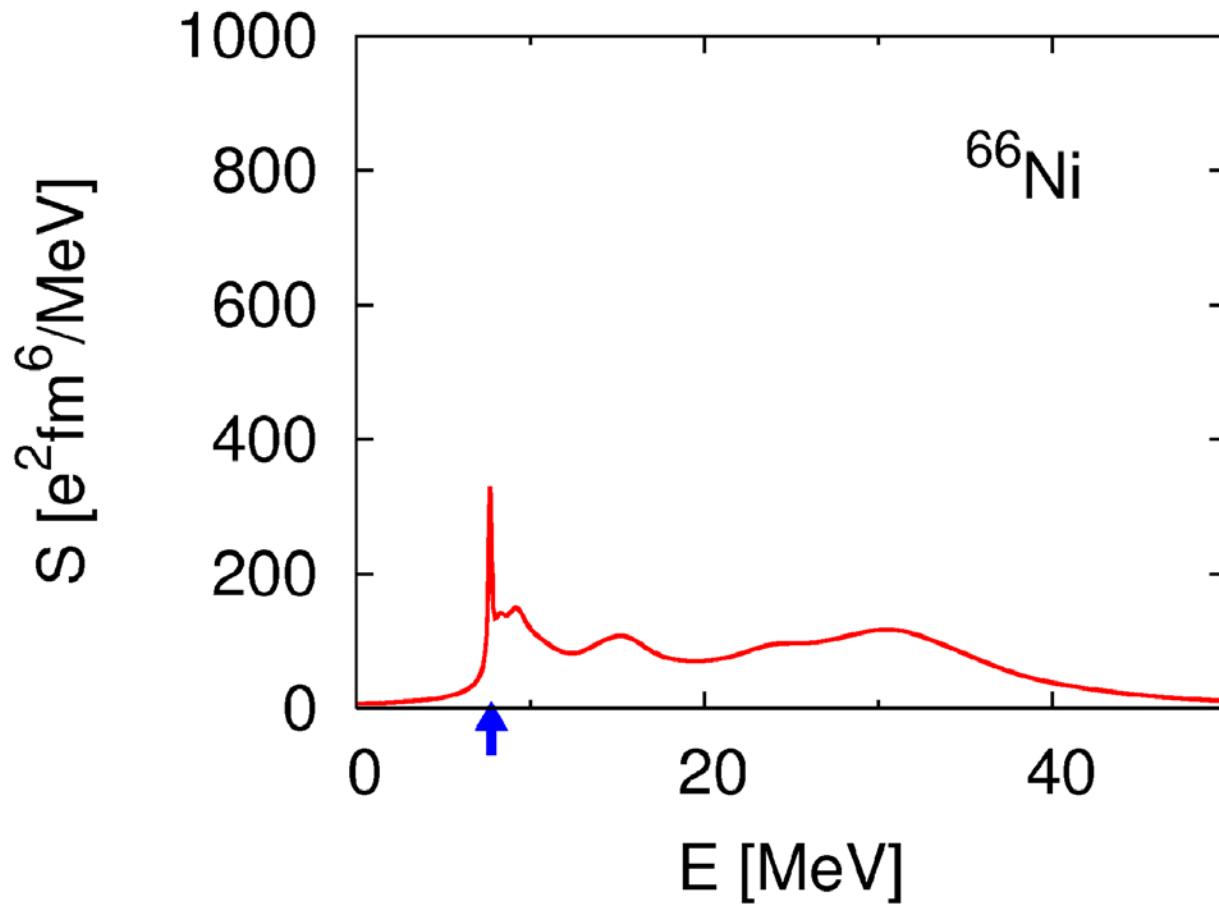
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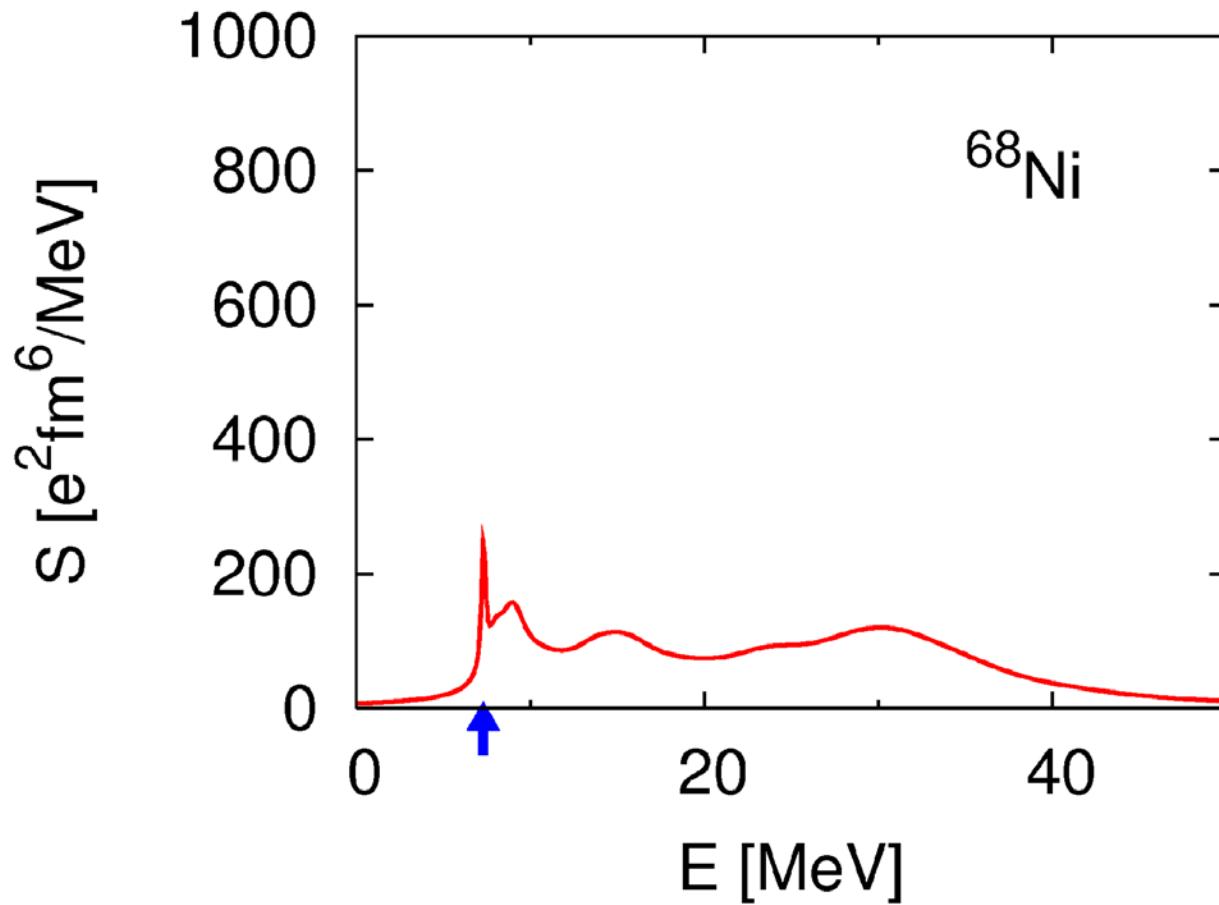
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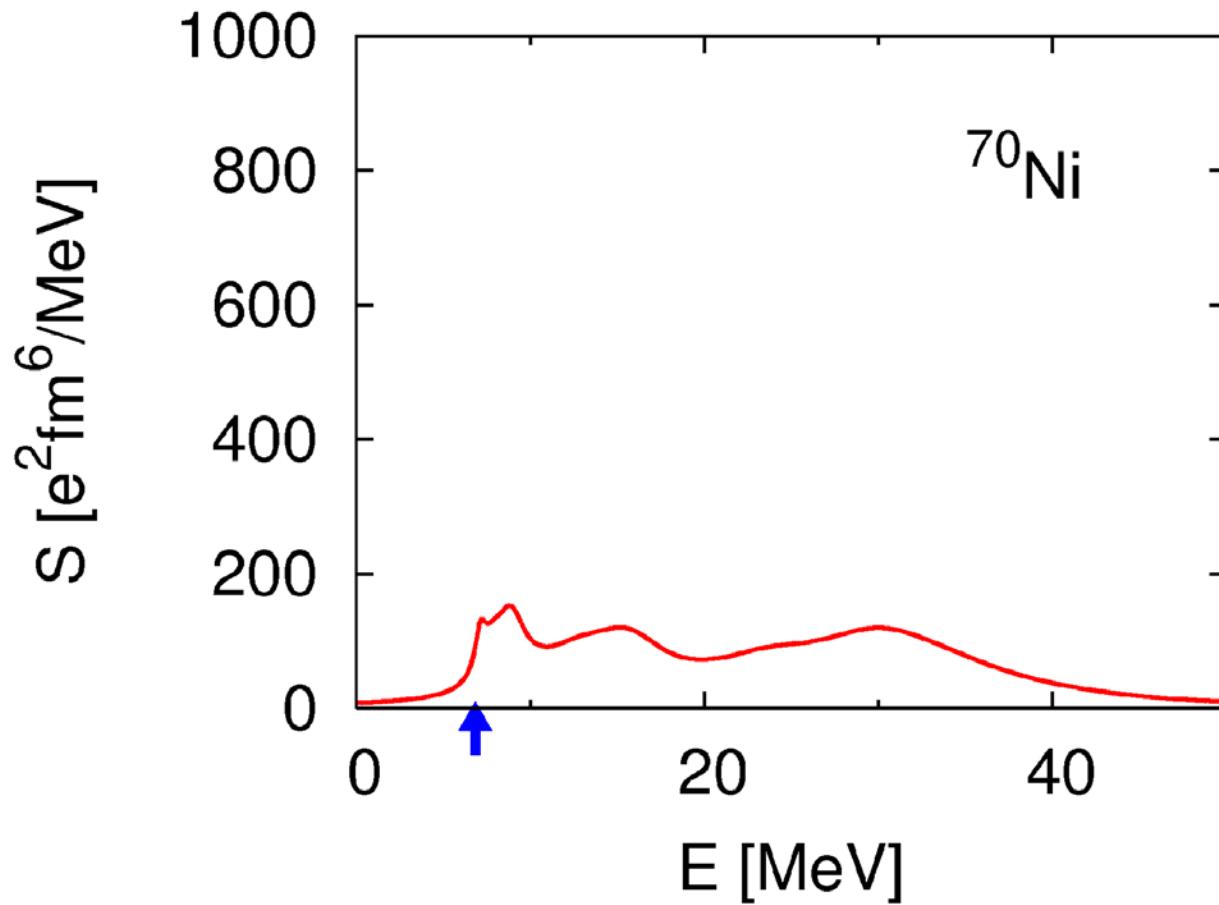
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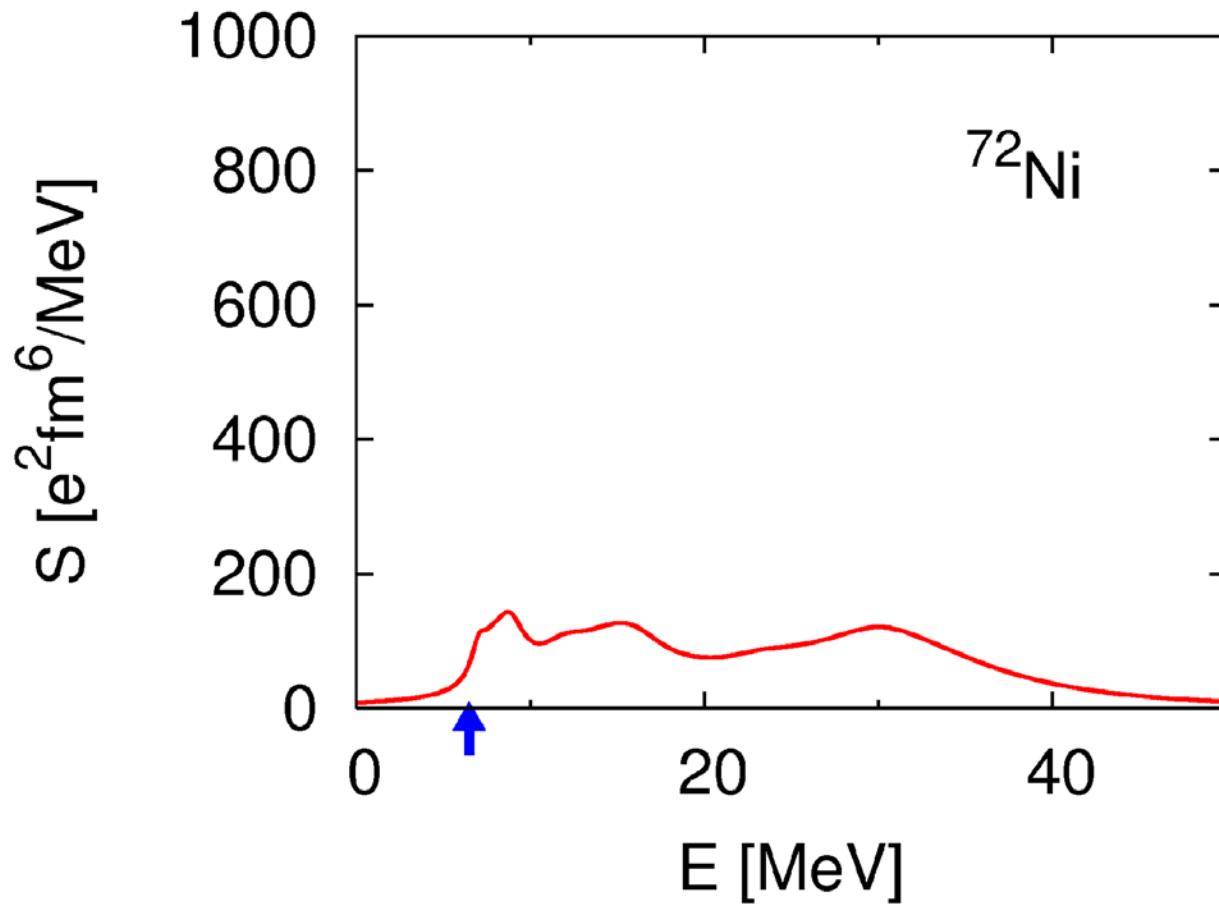
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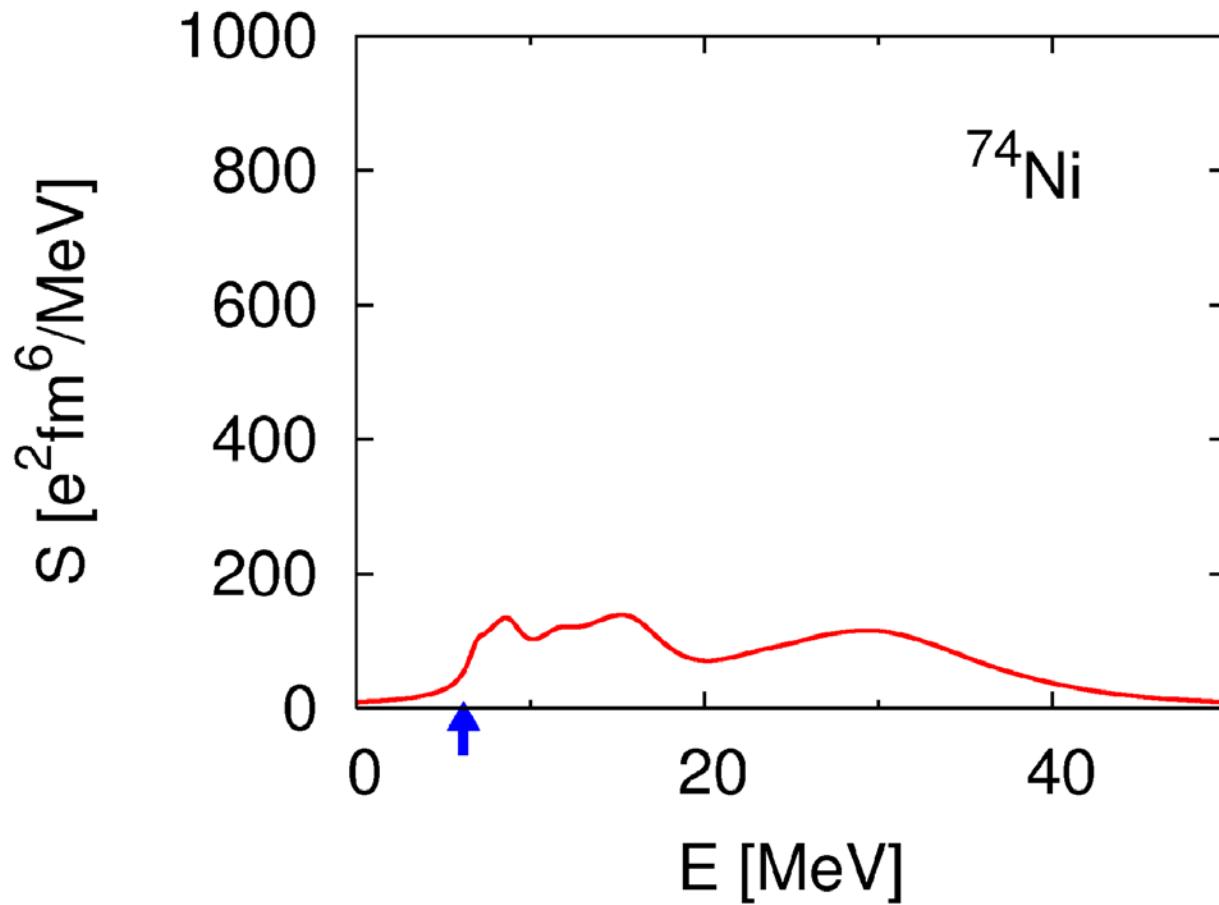
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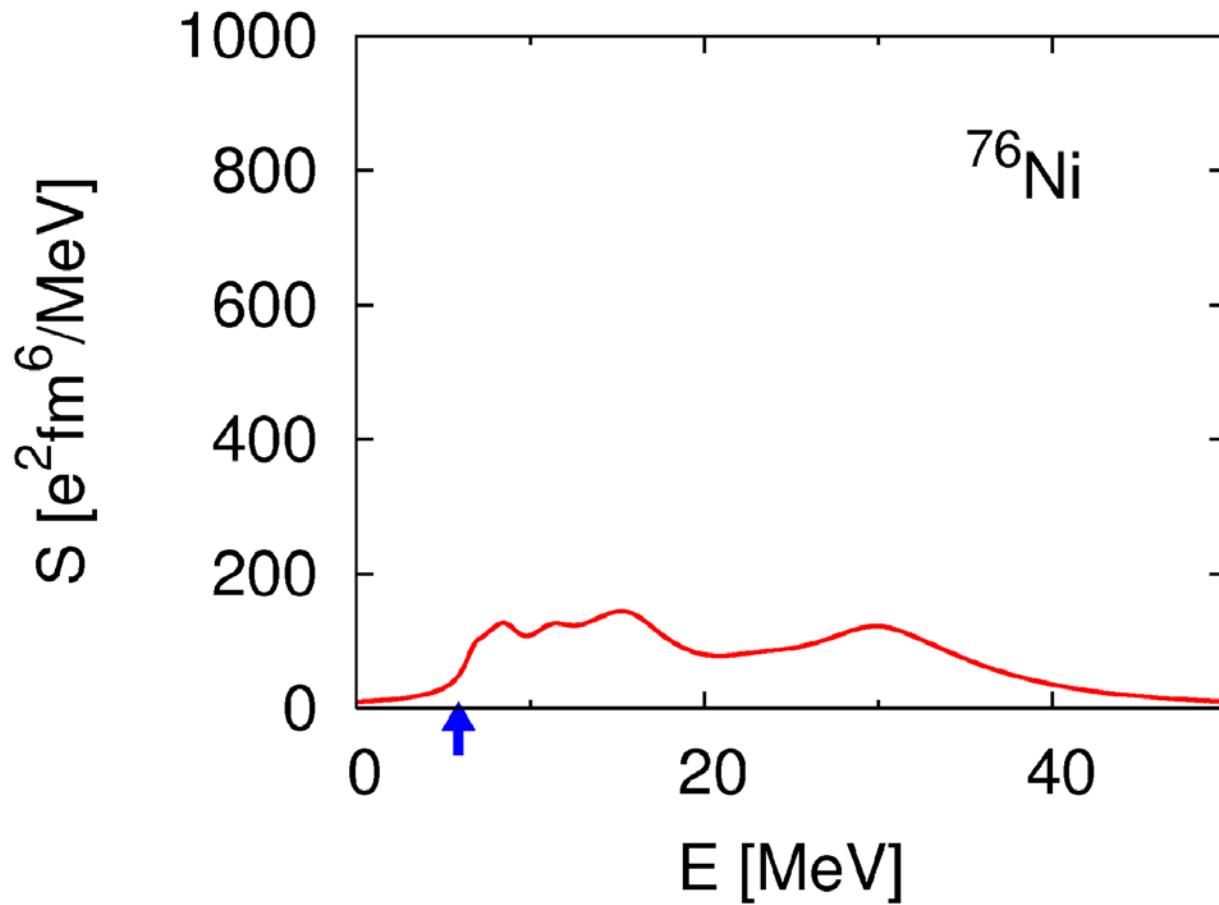
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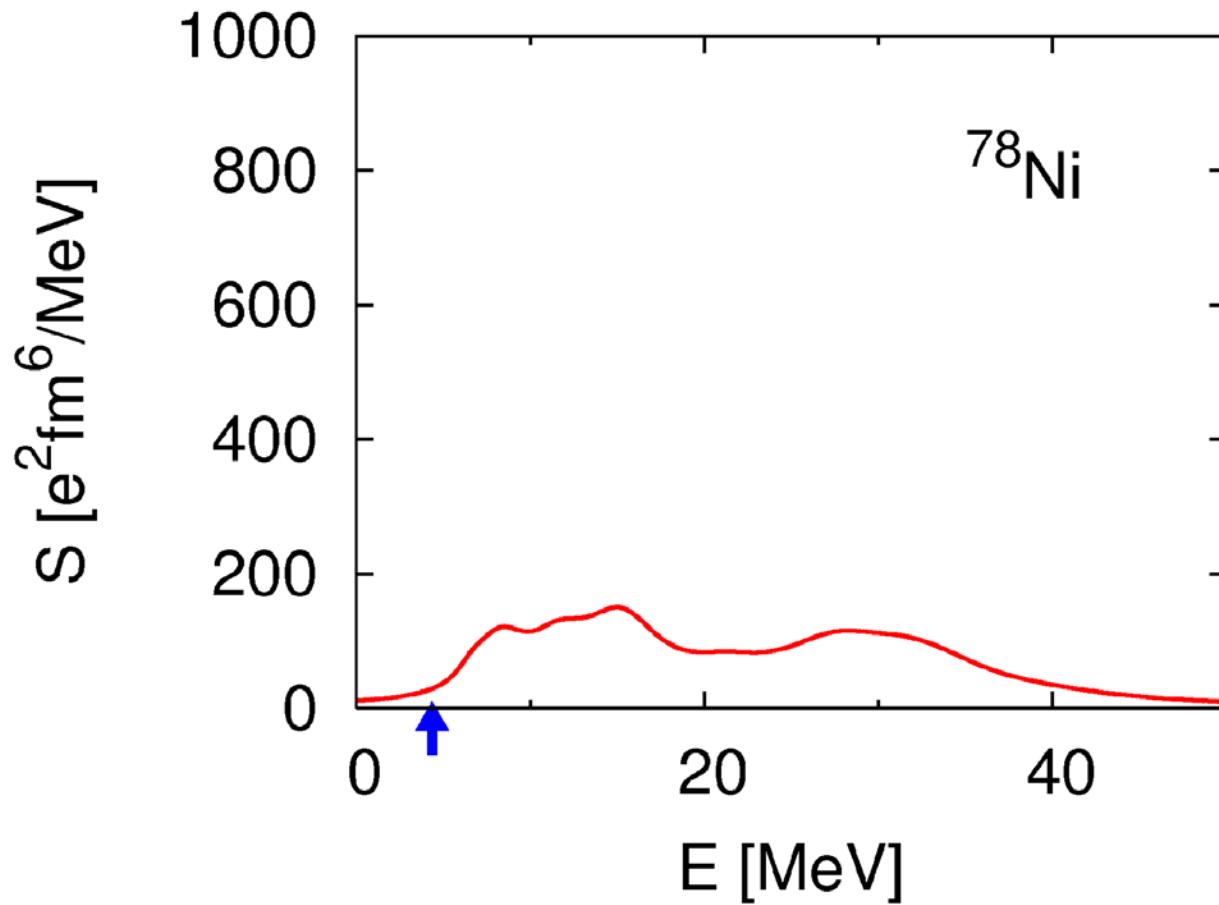
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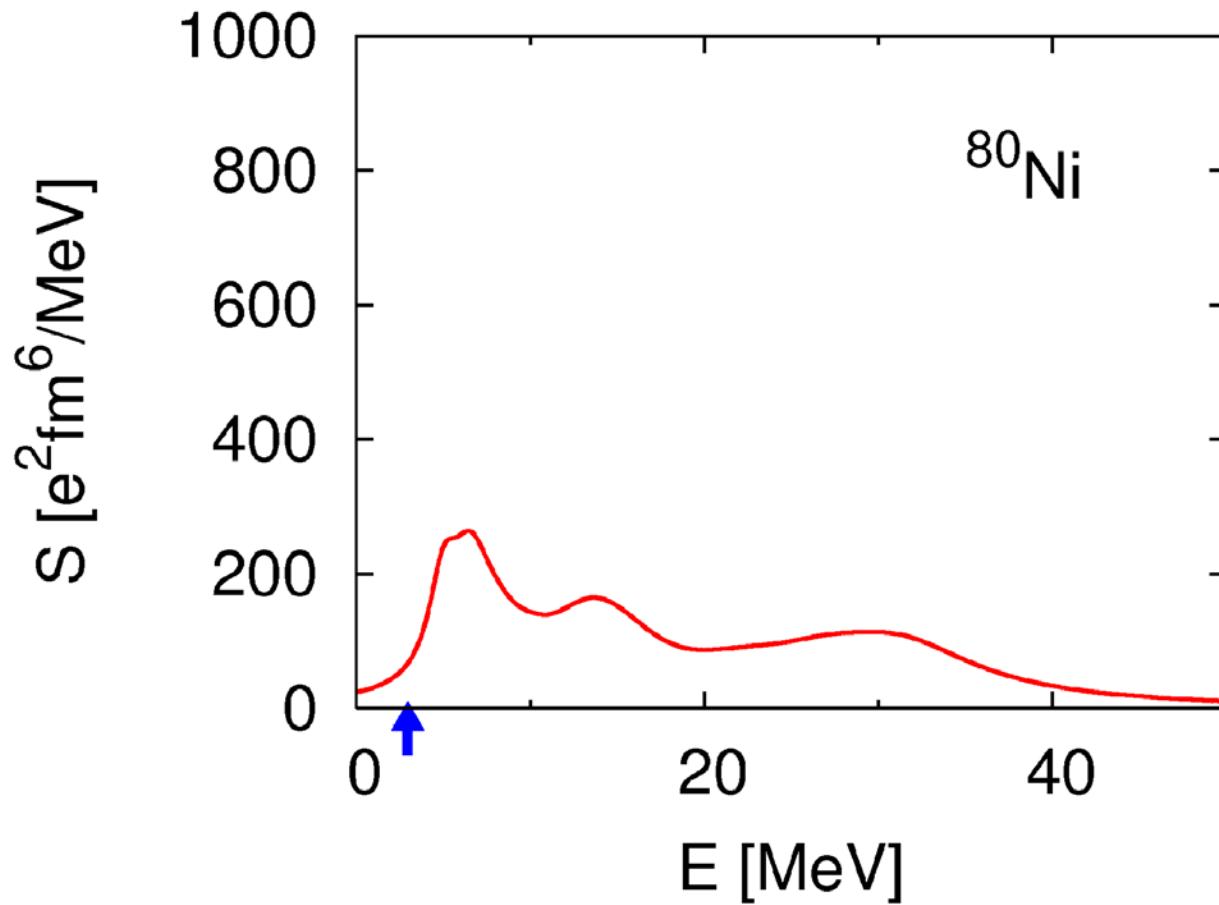
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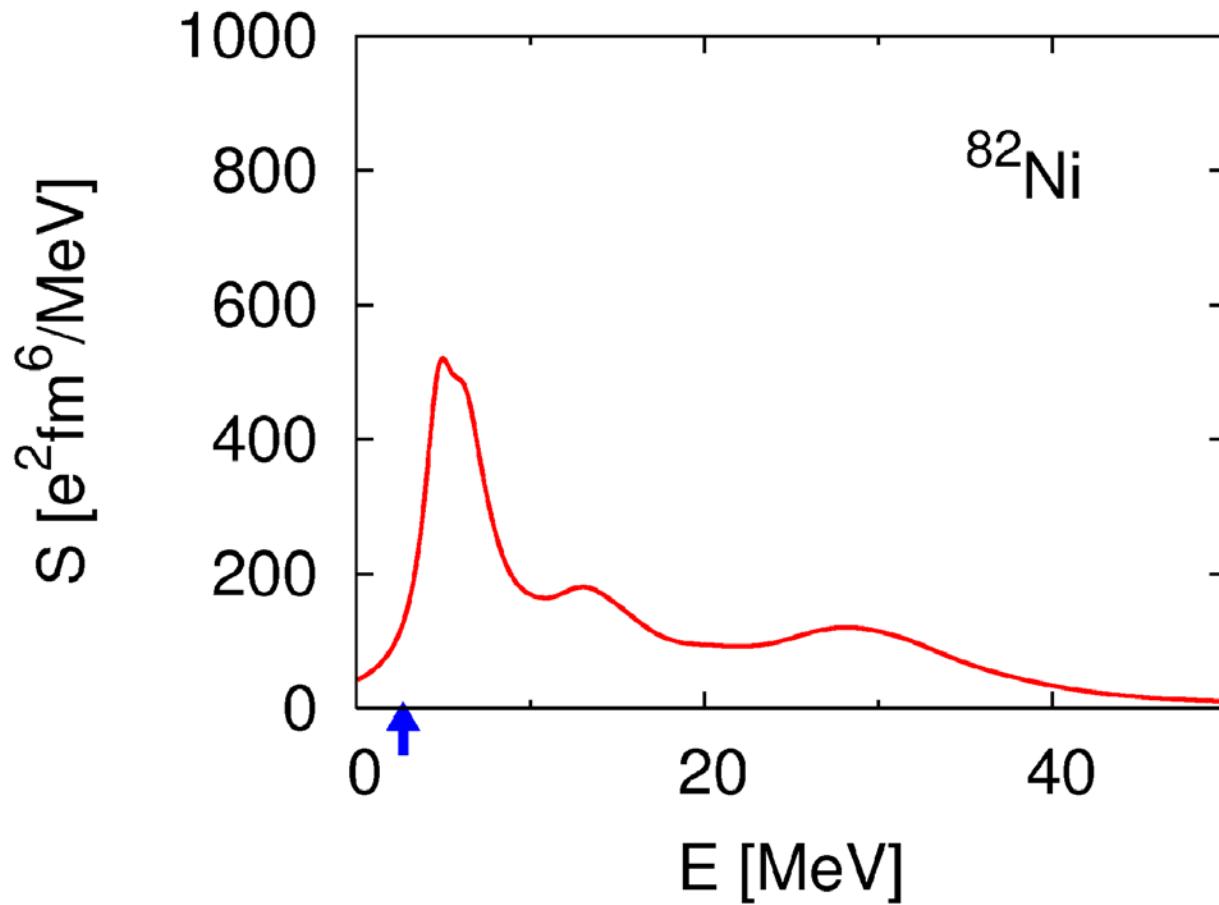
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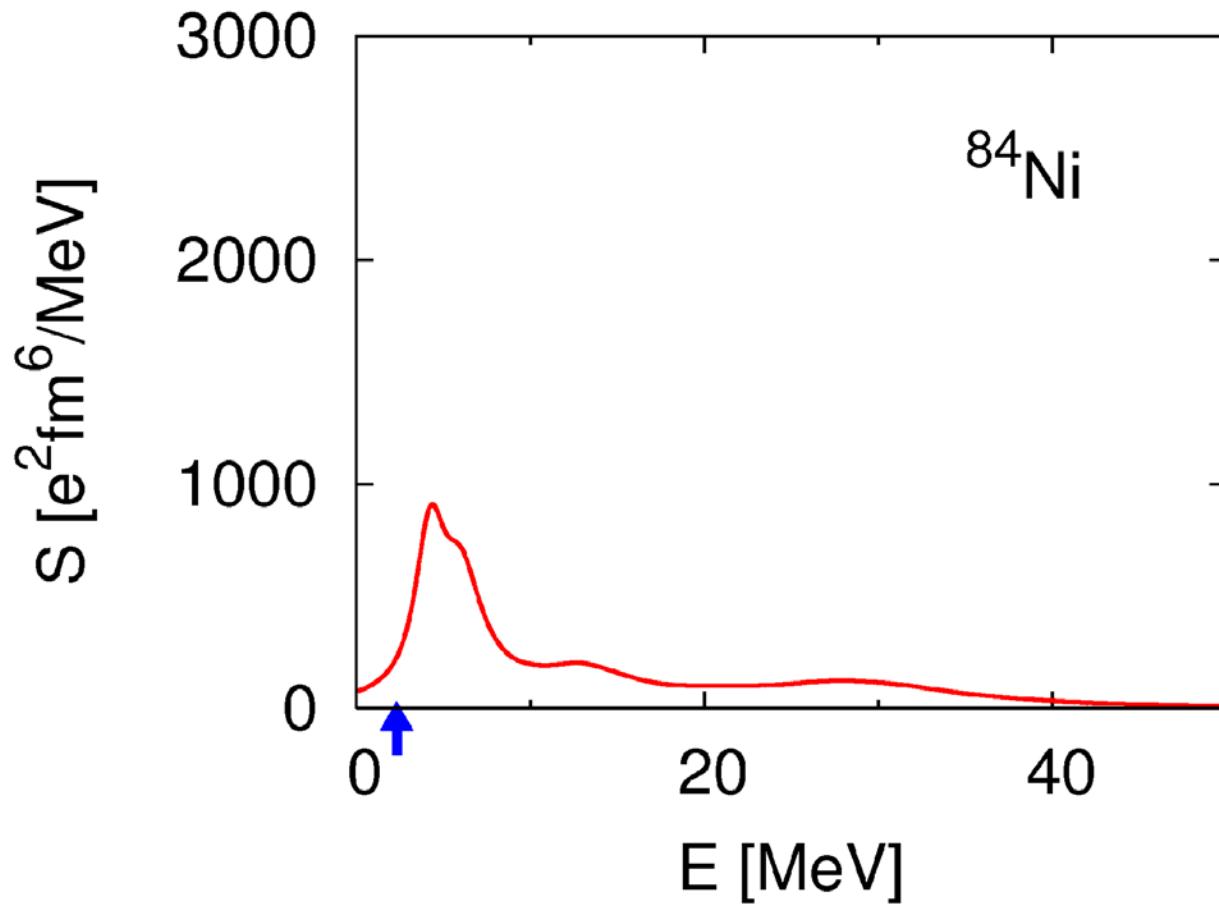
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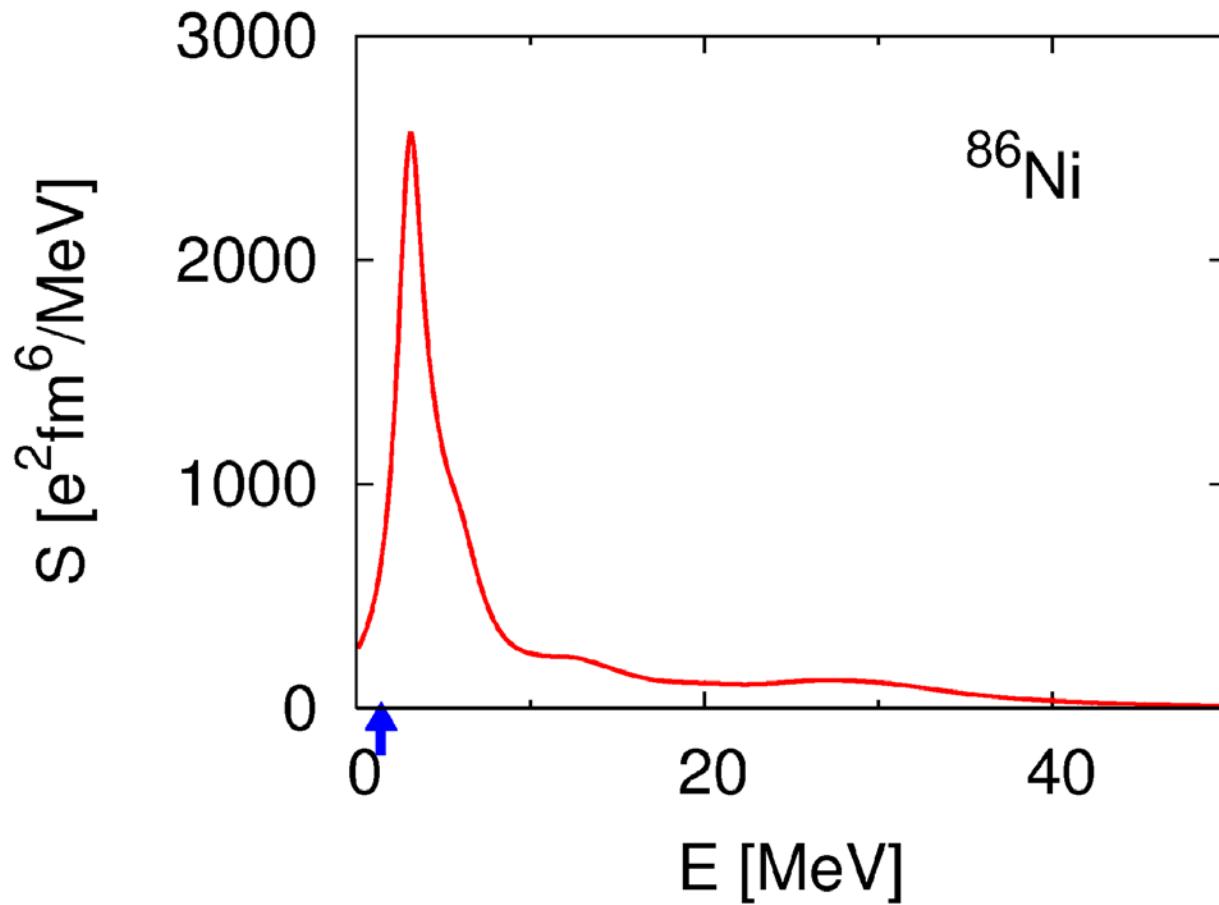
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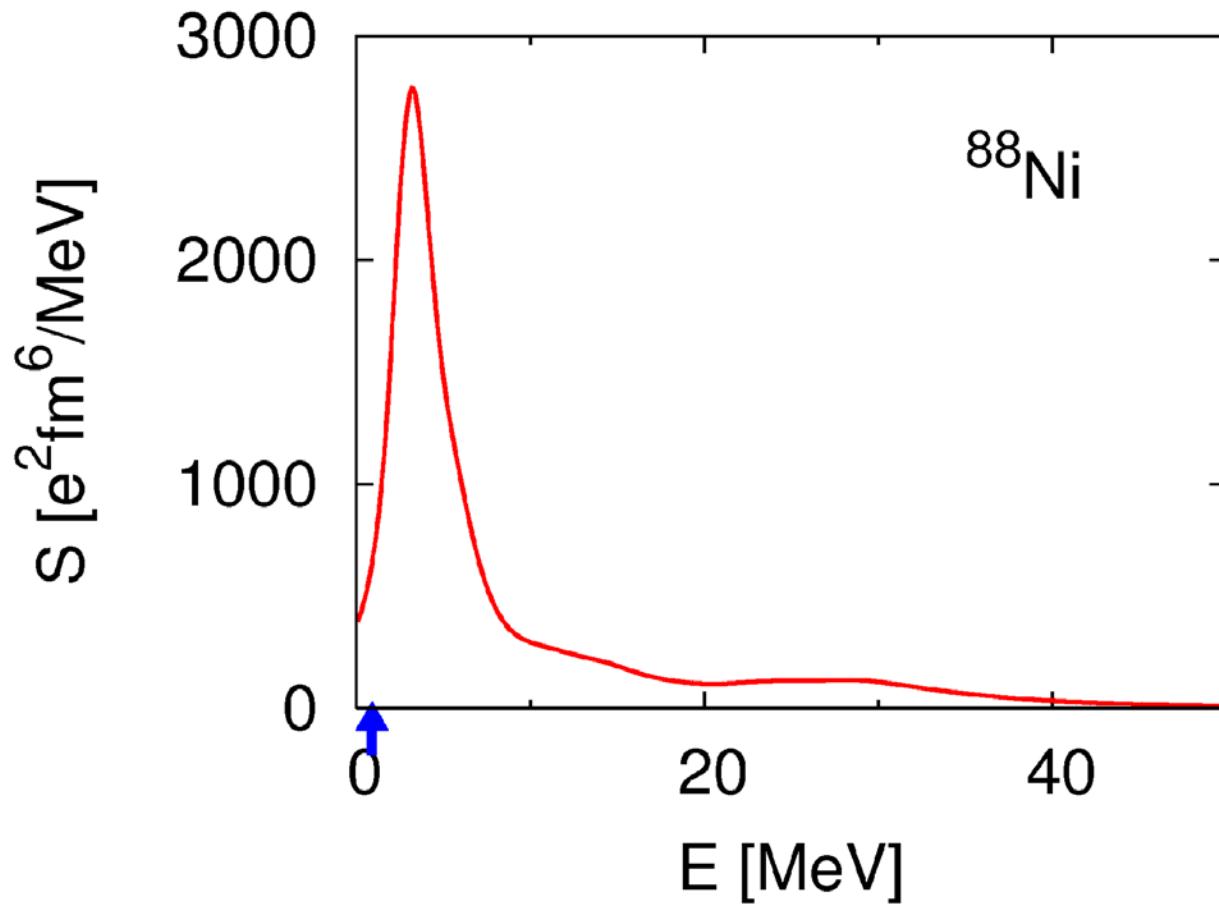
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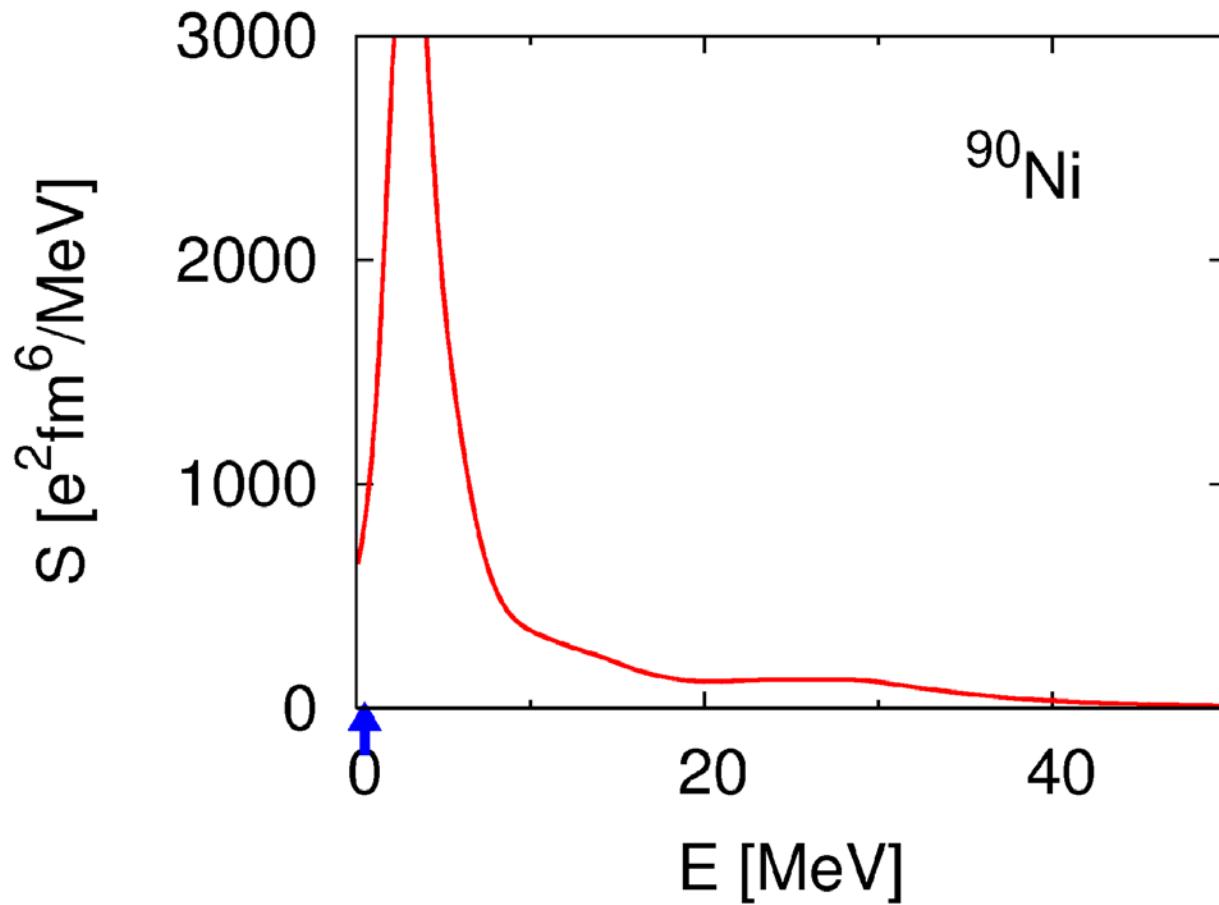
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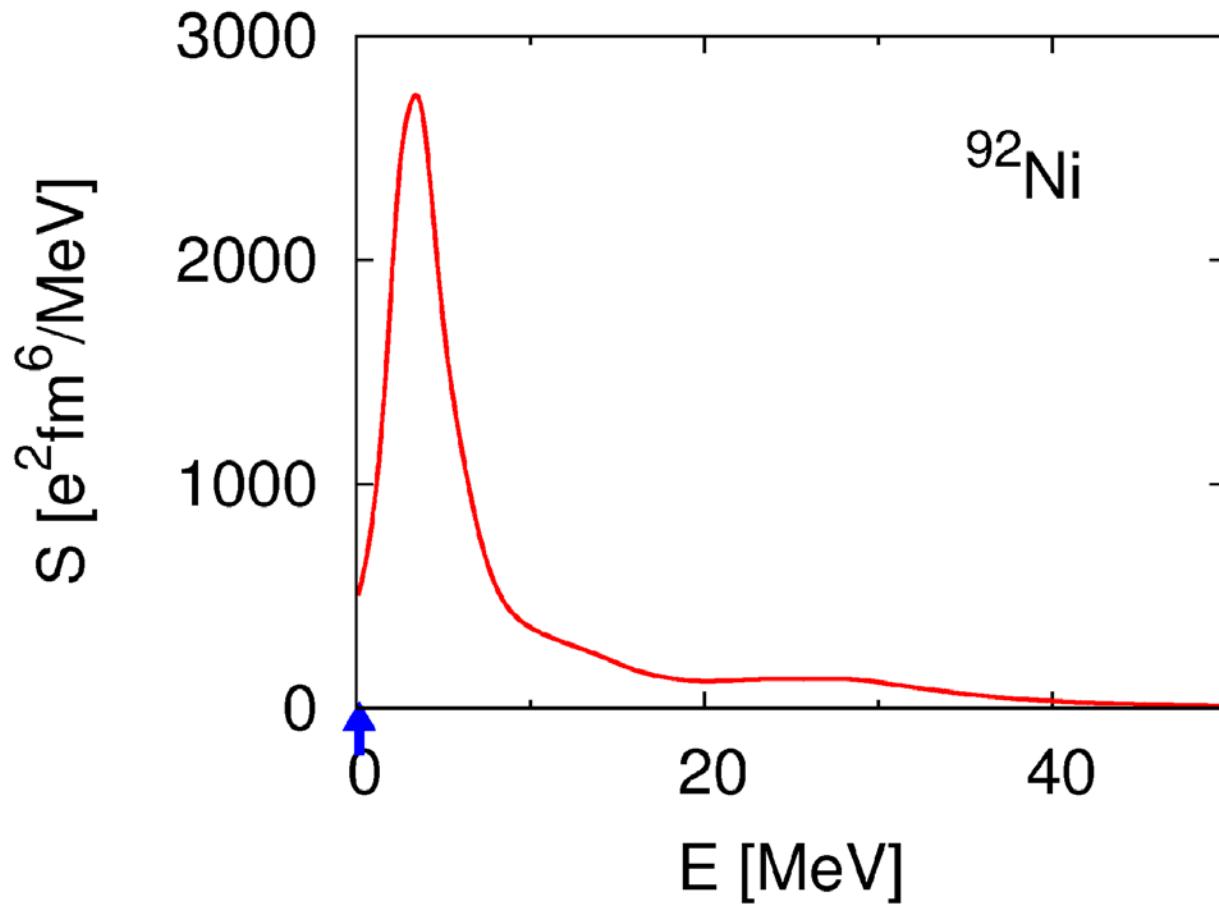
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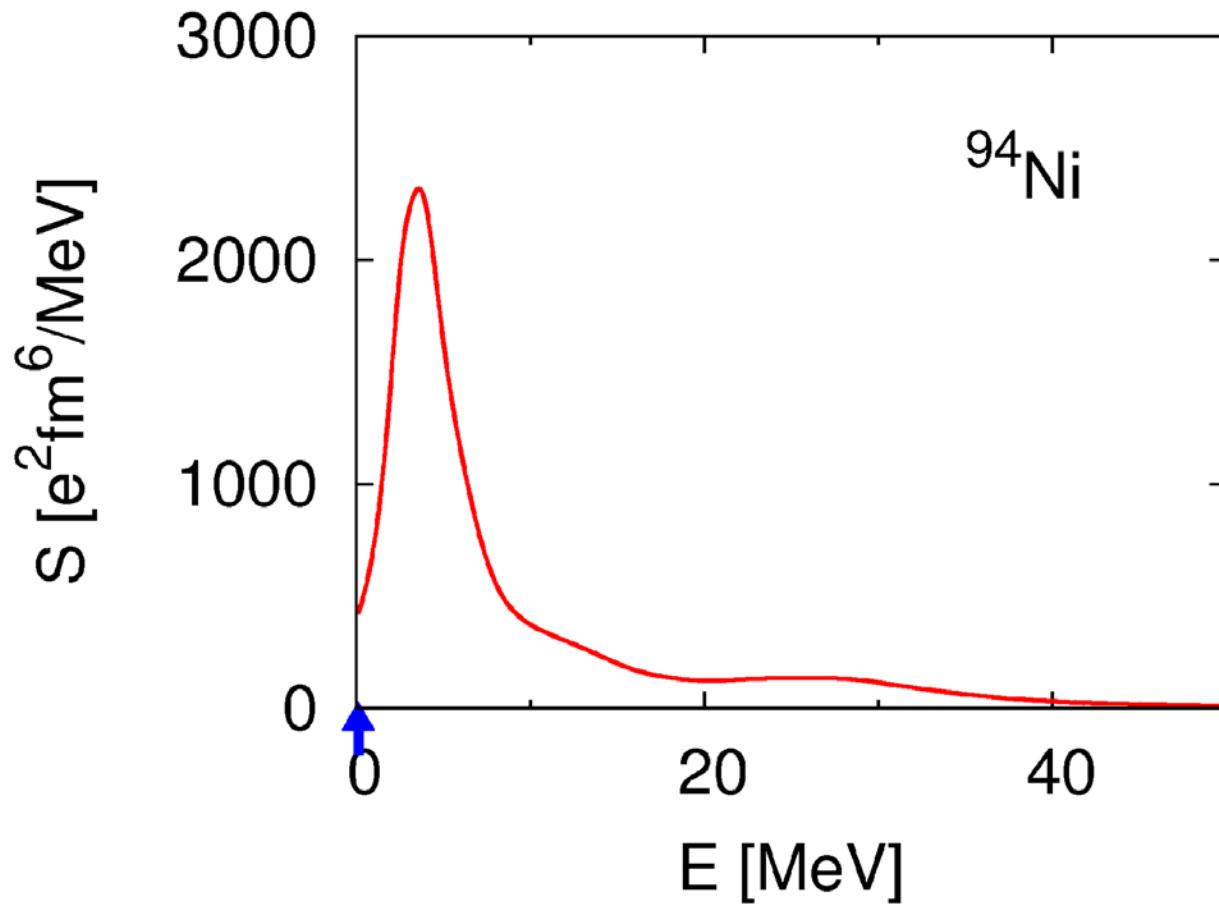
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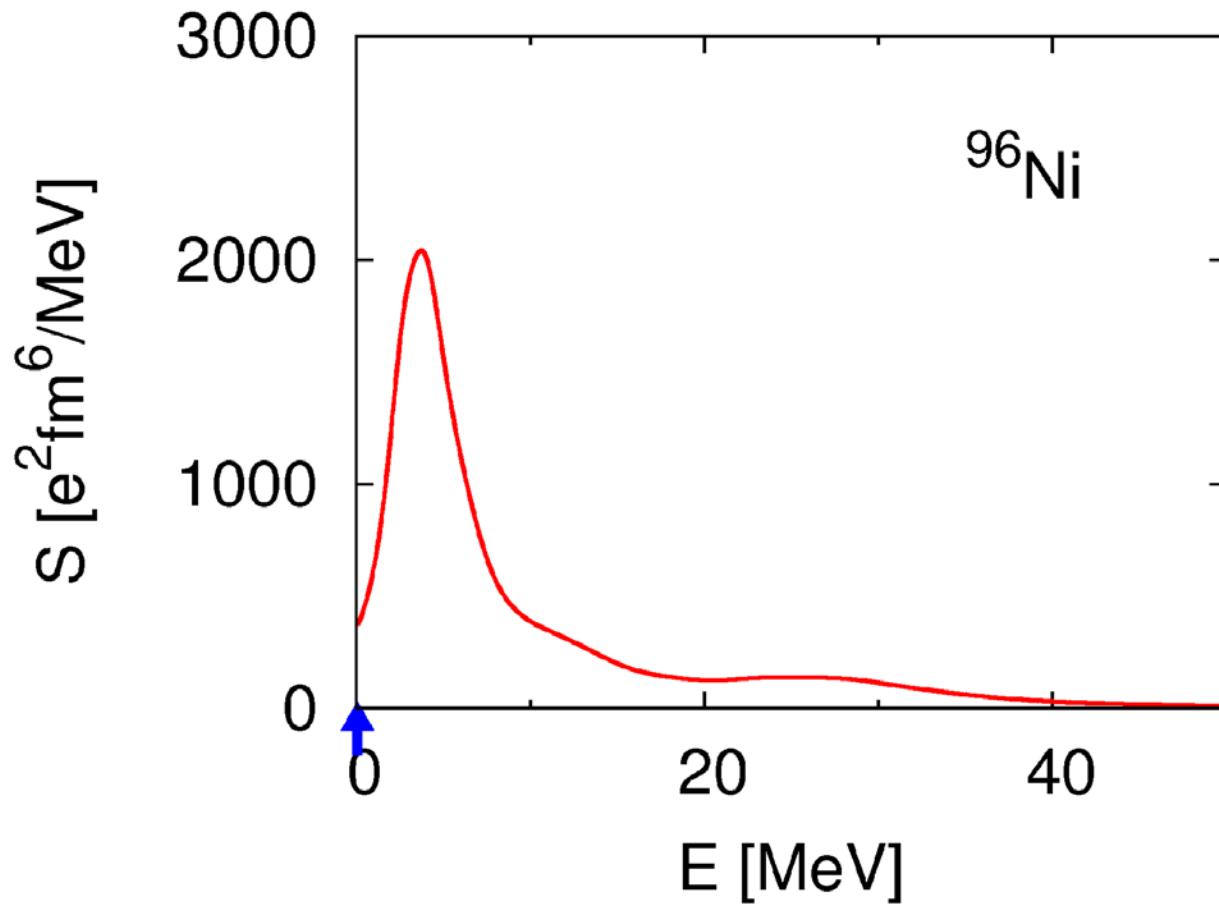
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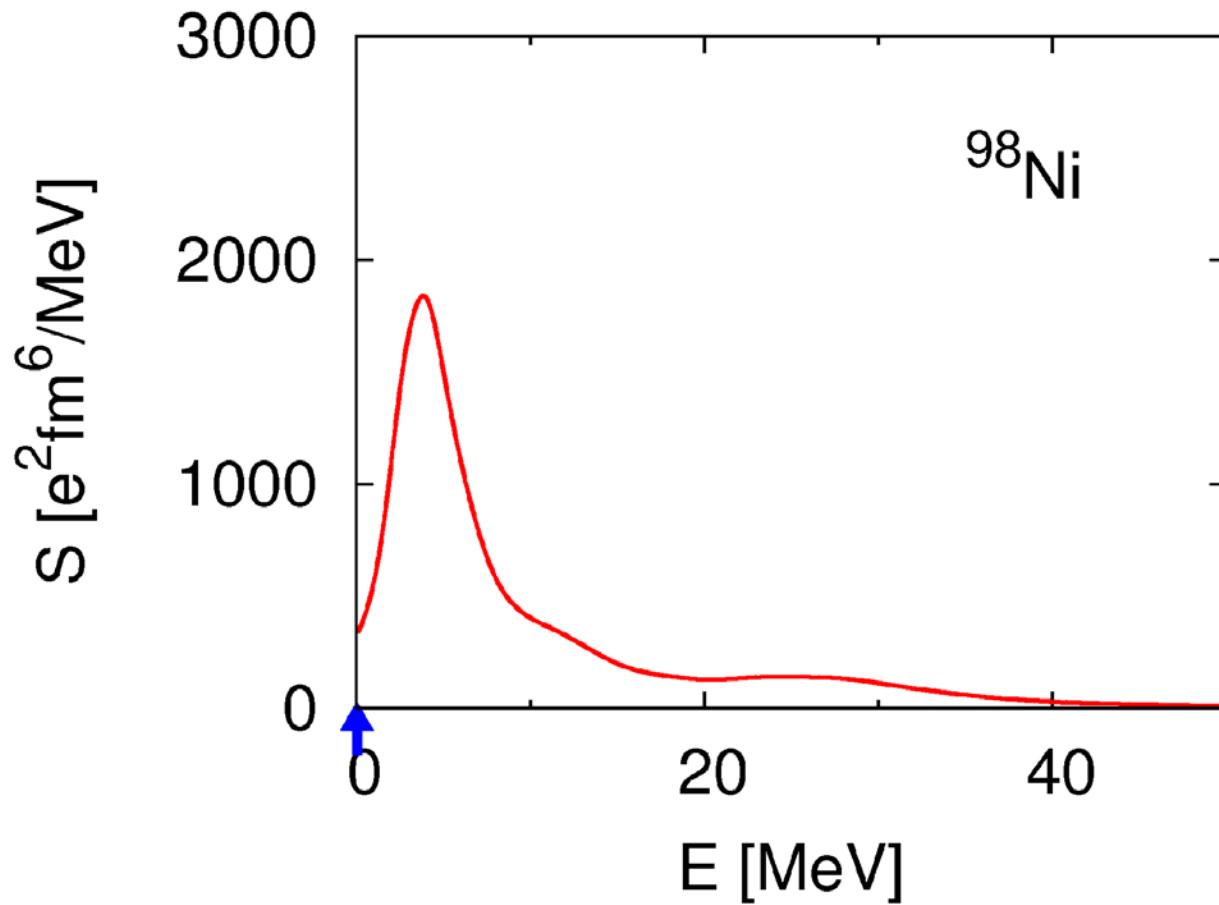
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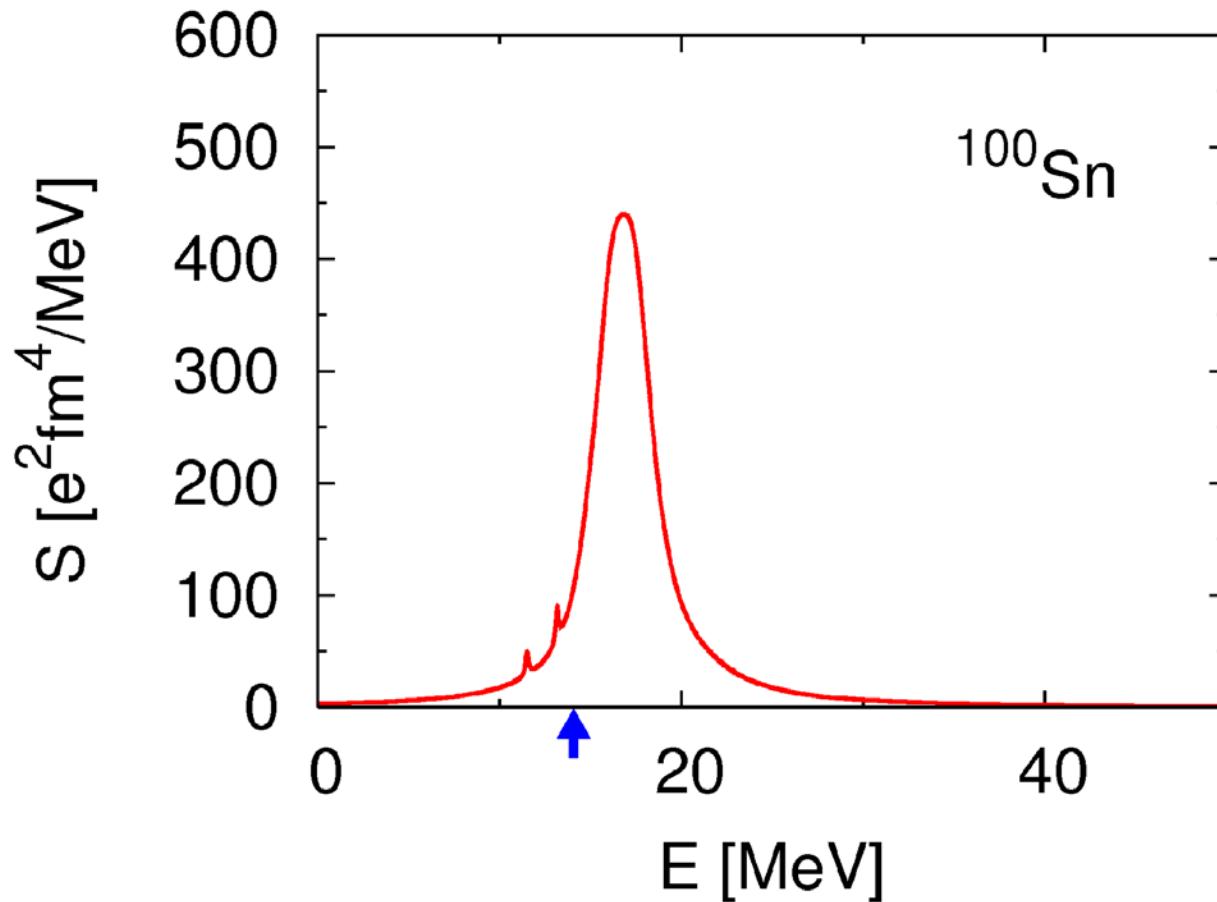
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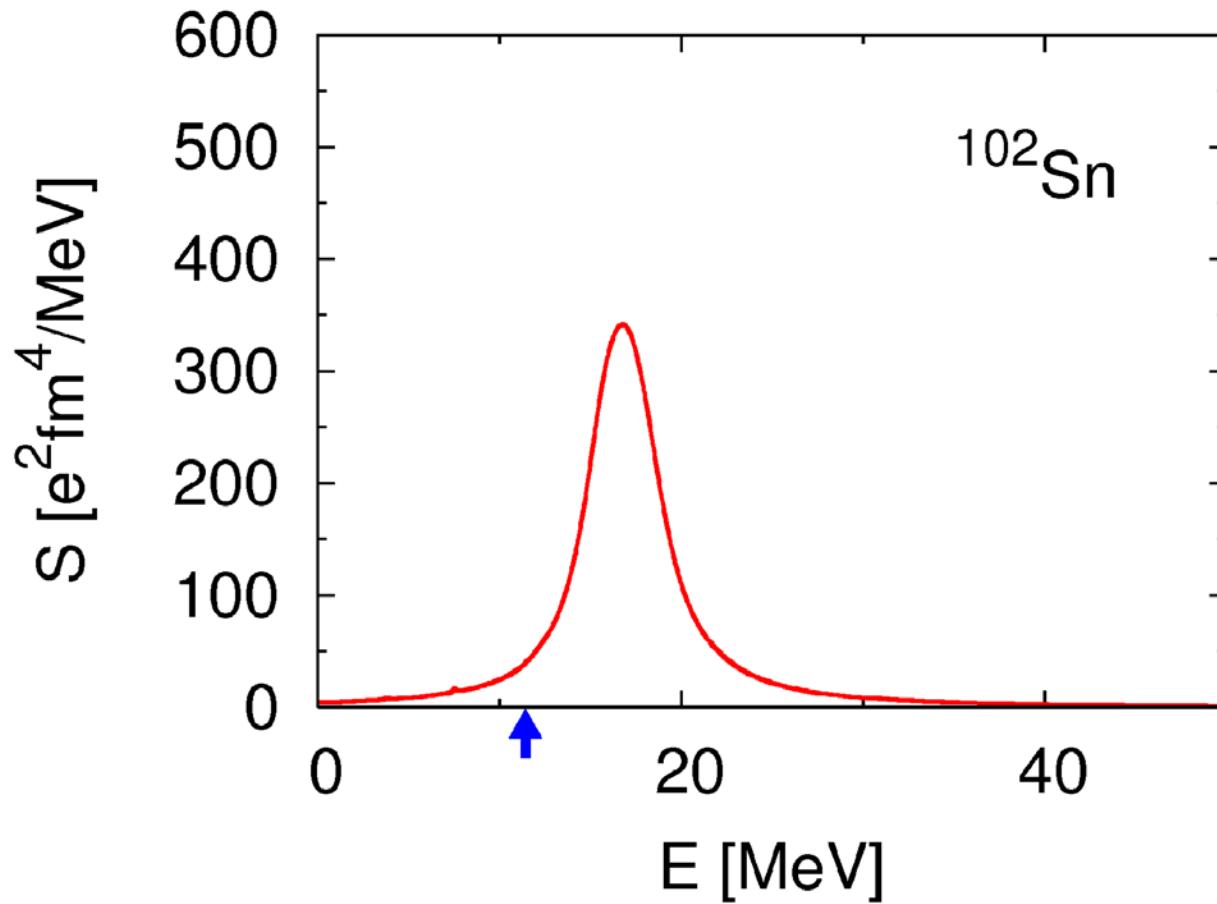


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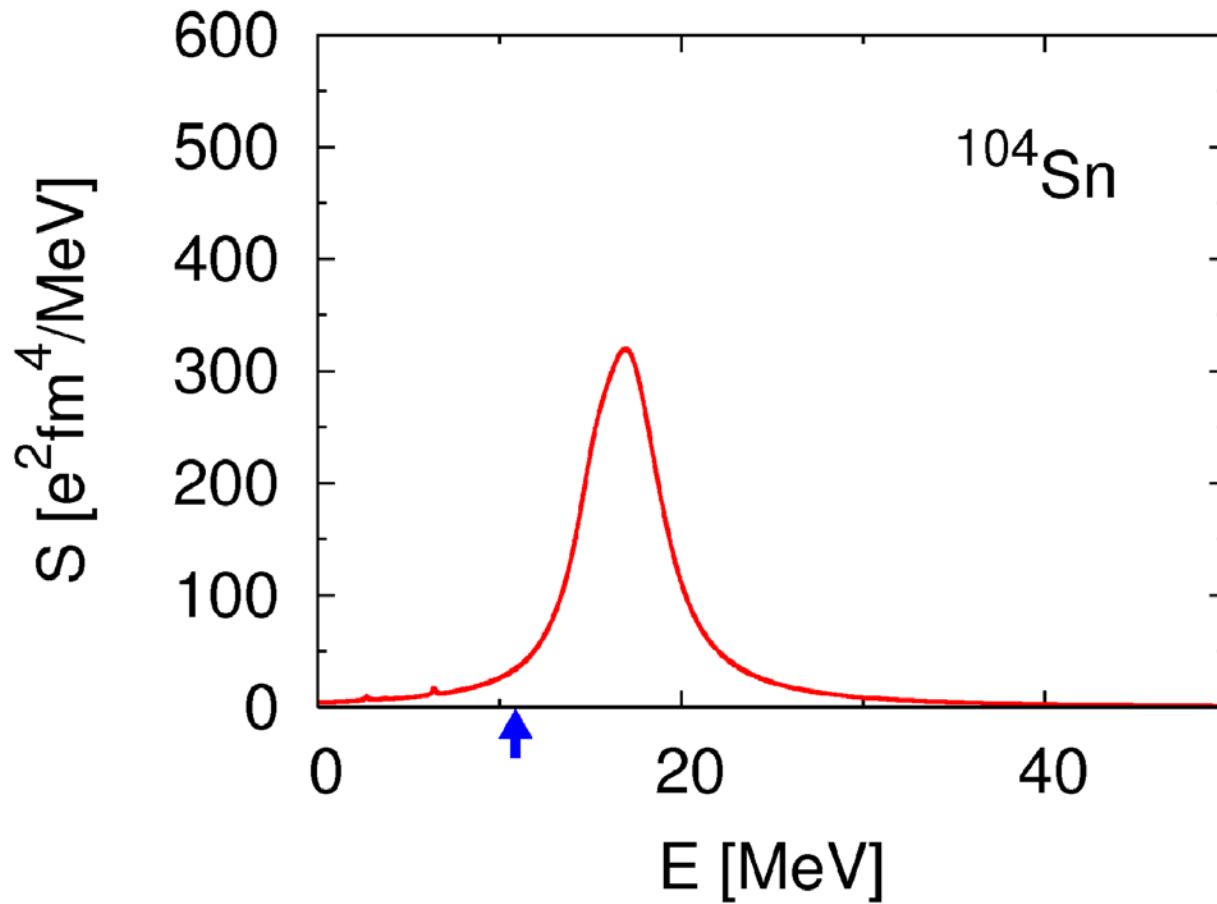


SkM\*

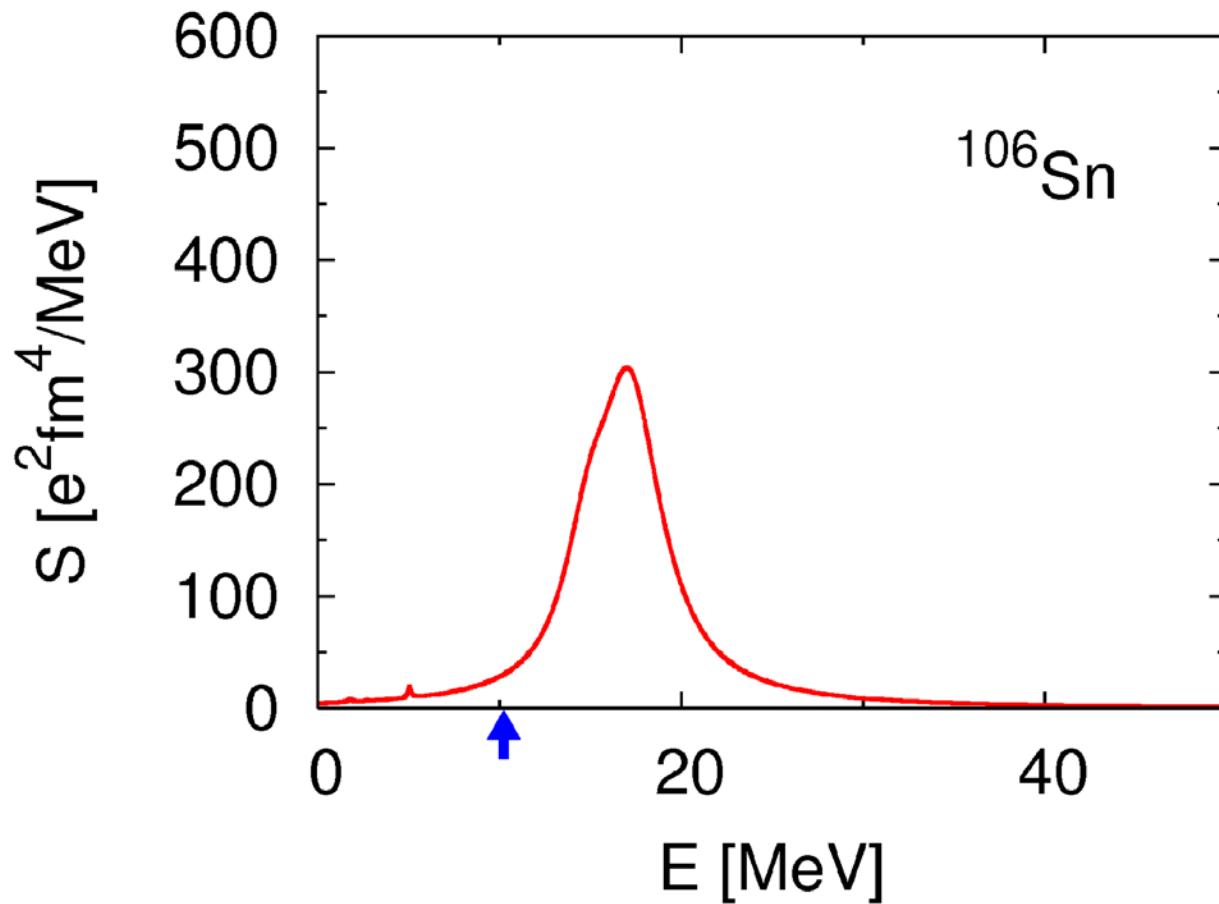
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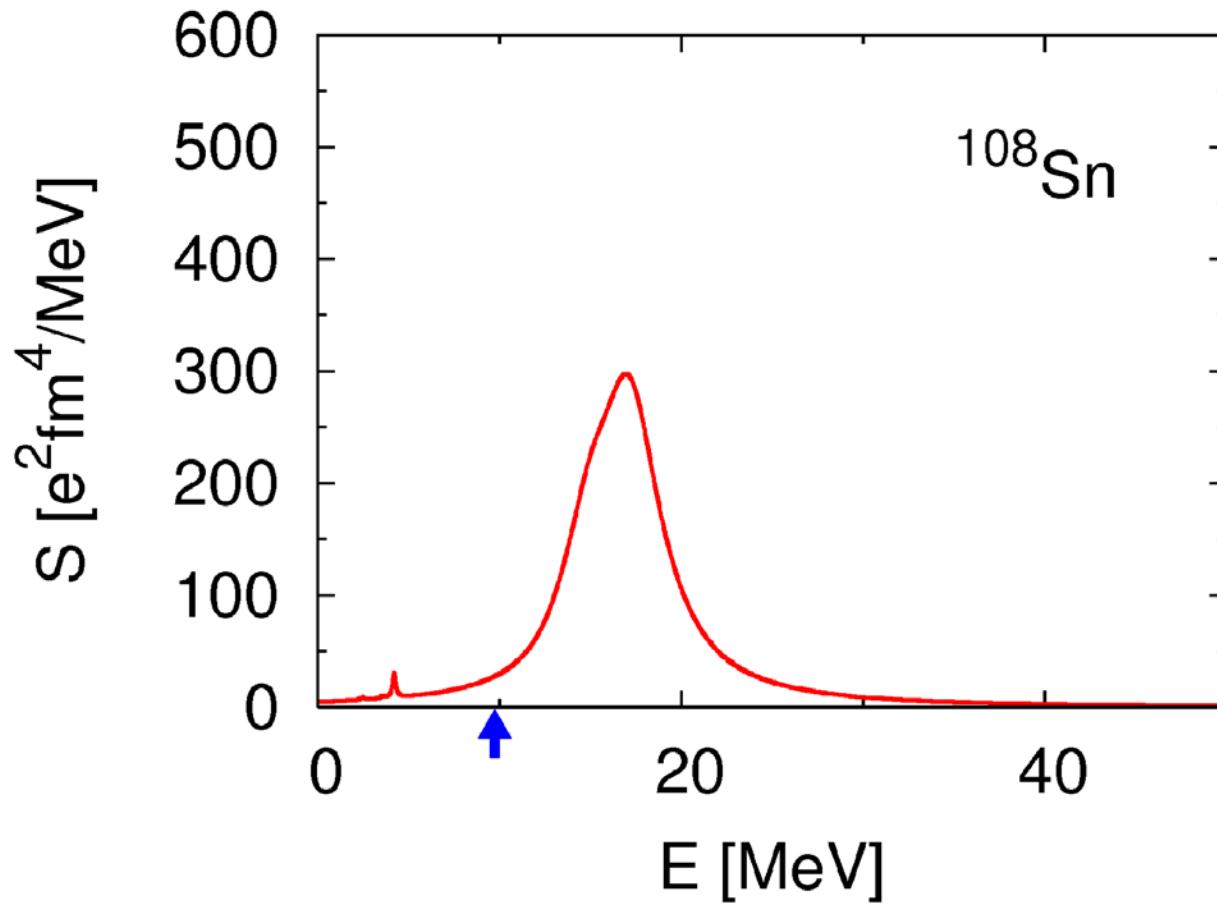
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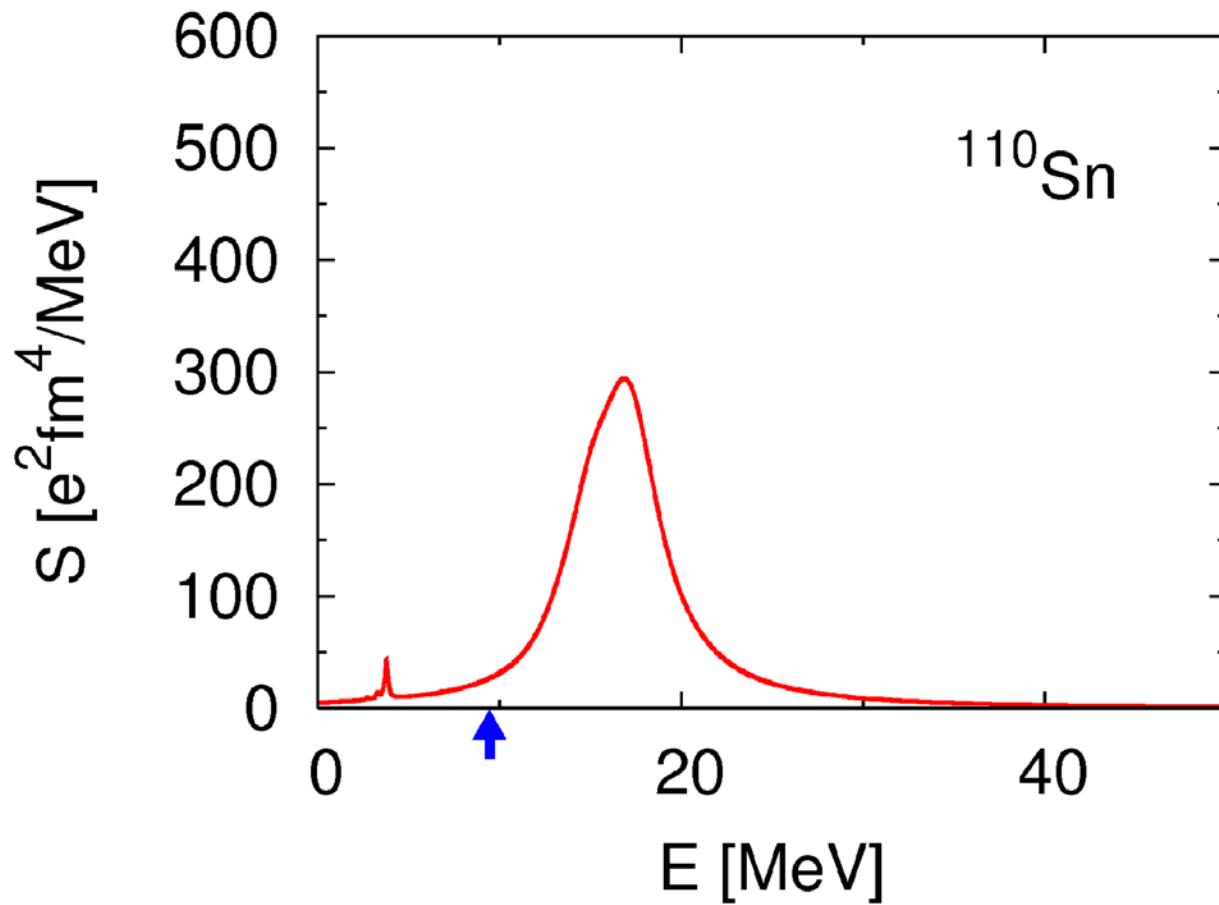
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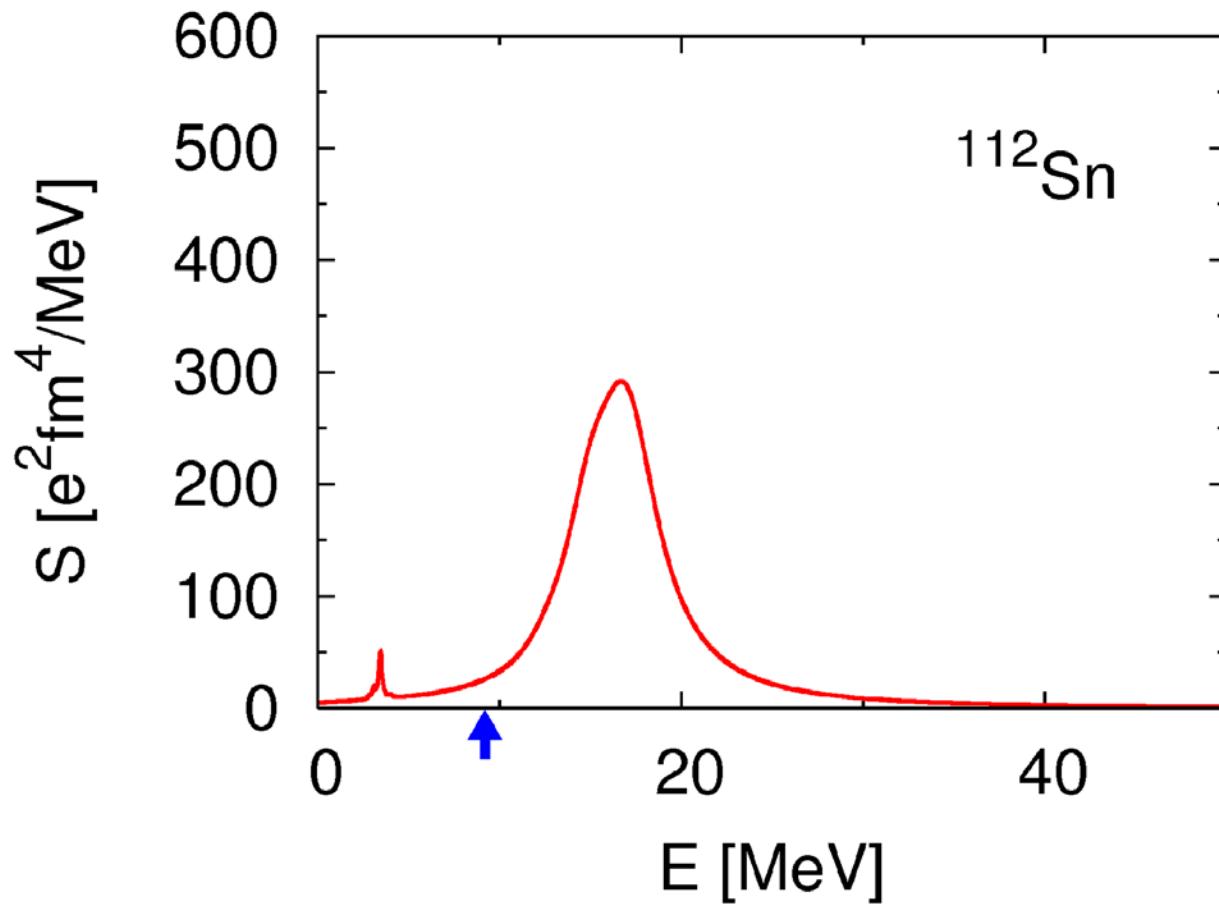
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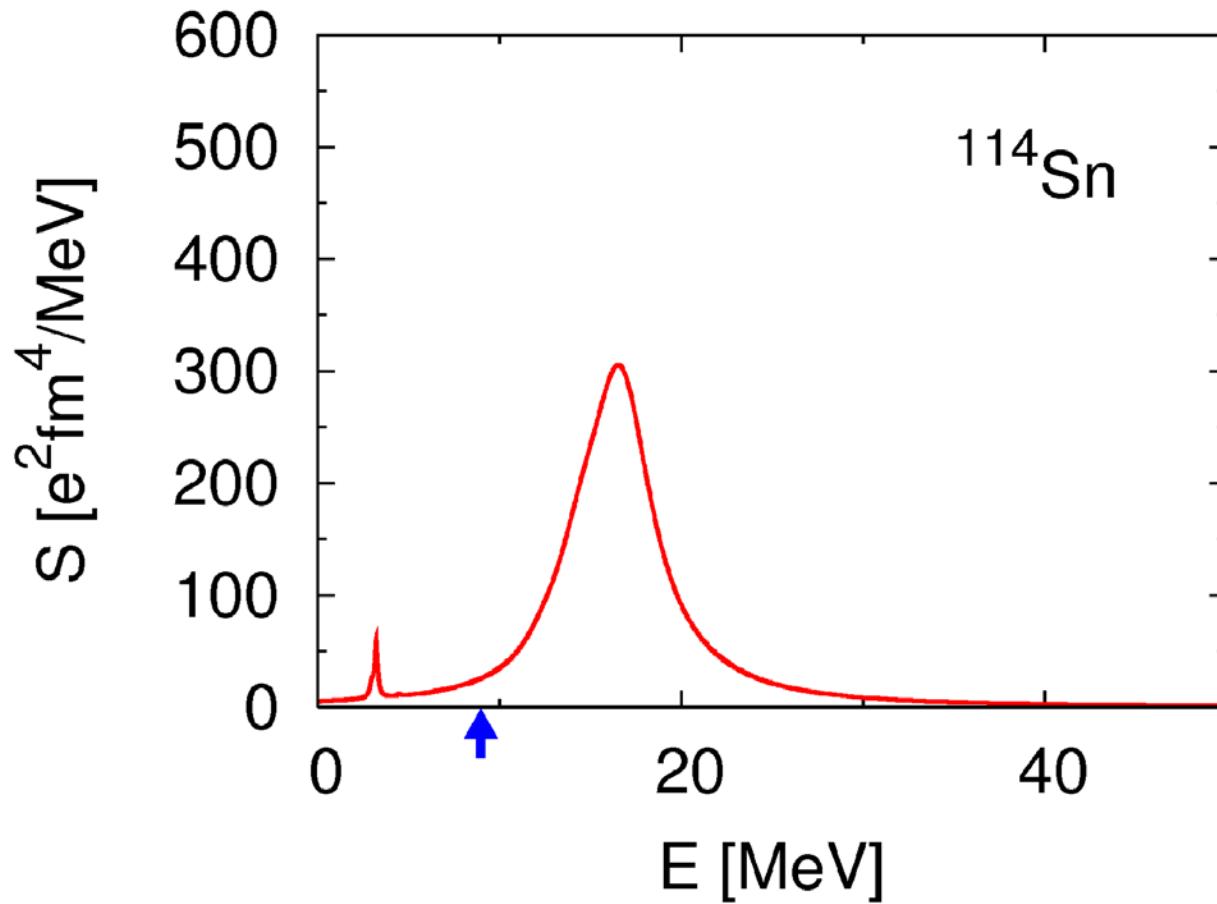
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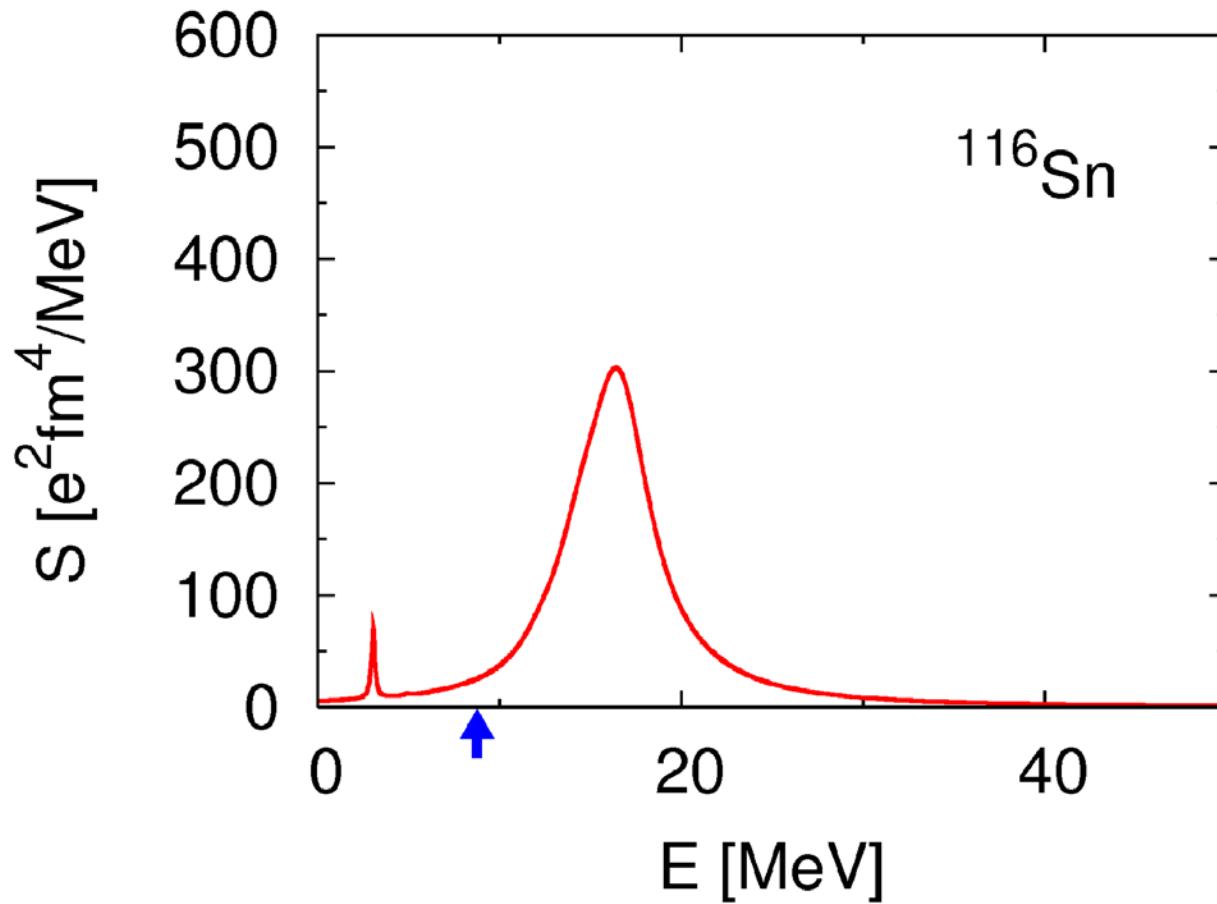
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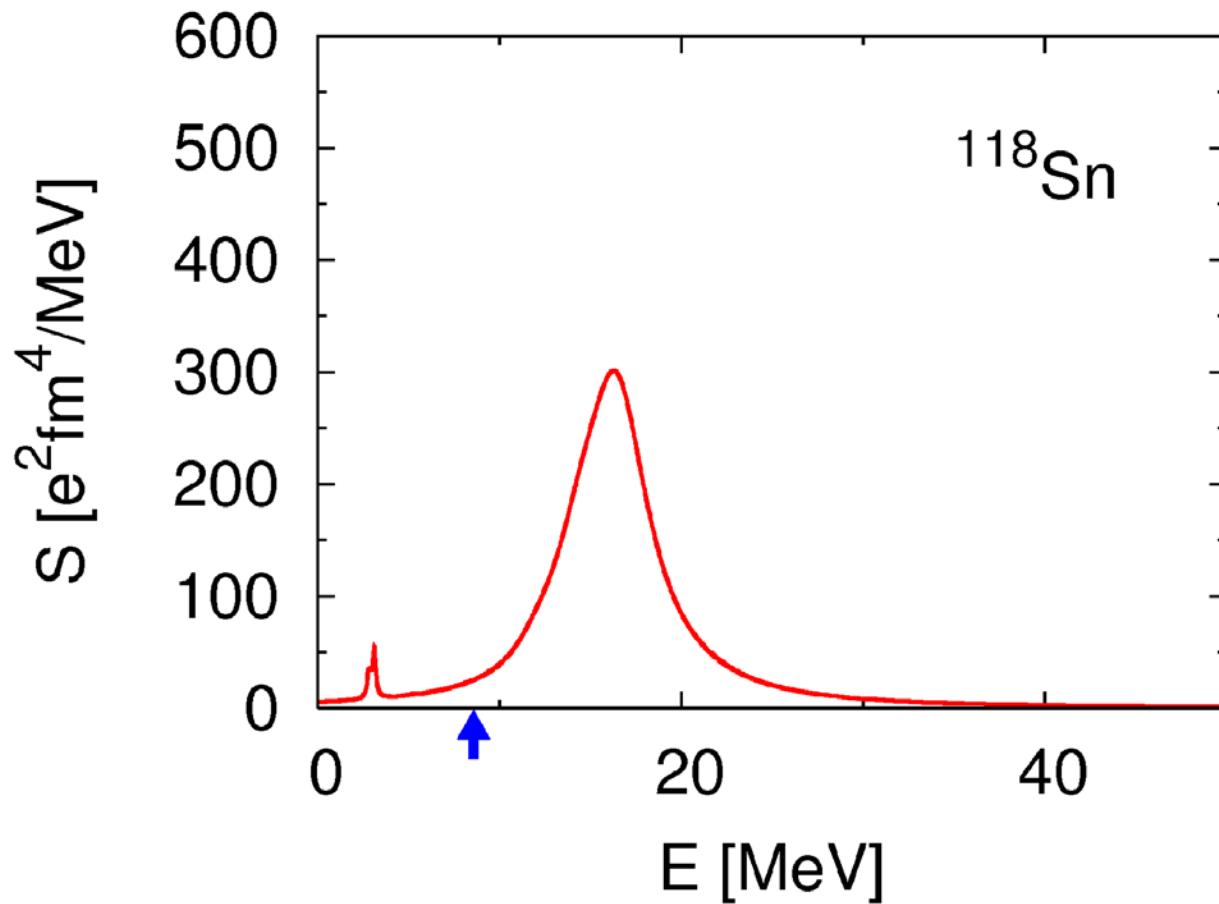
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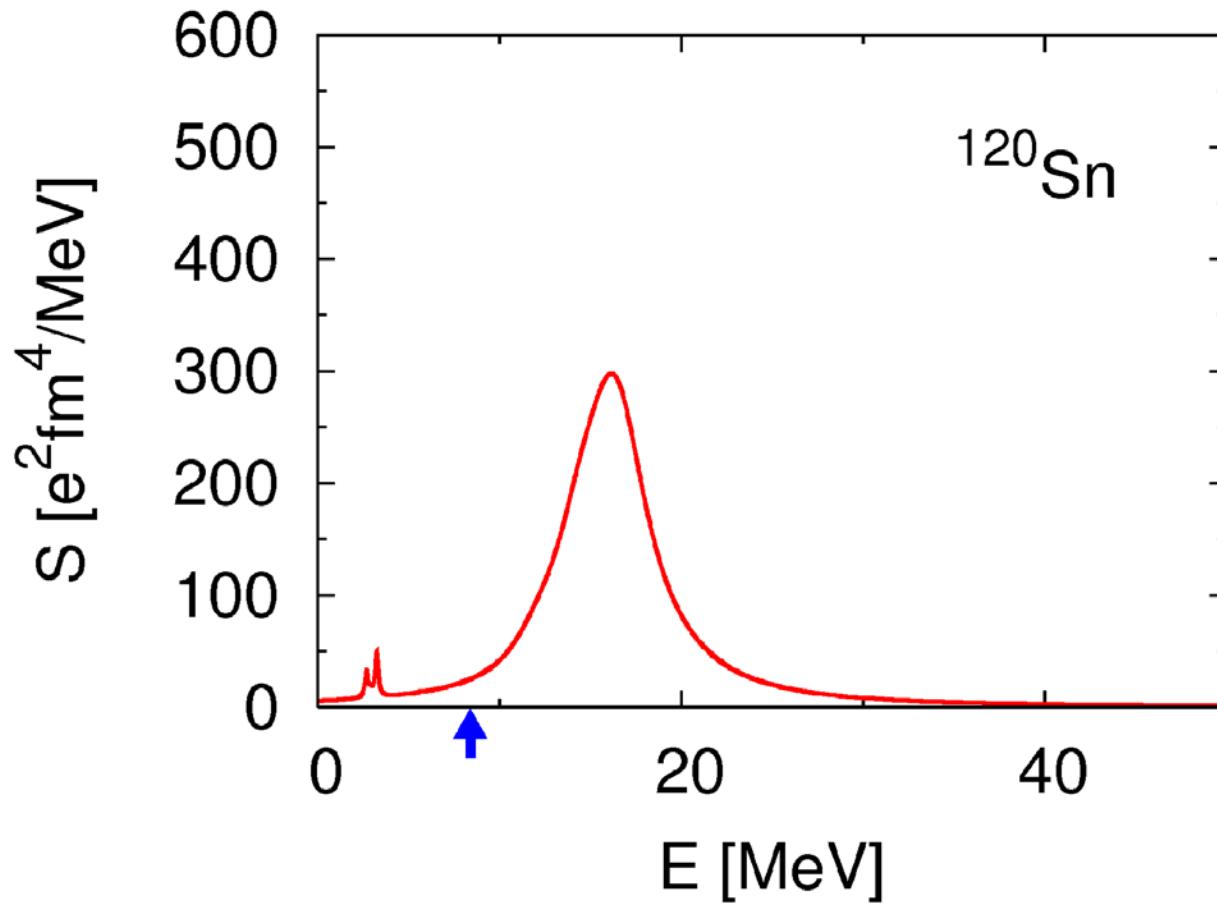
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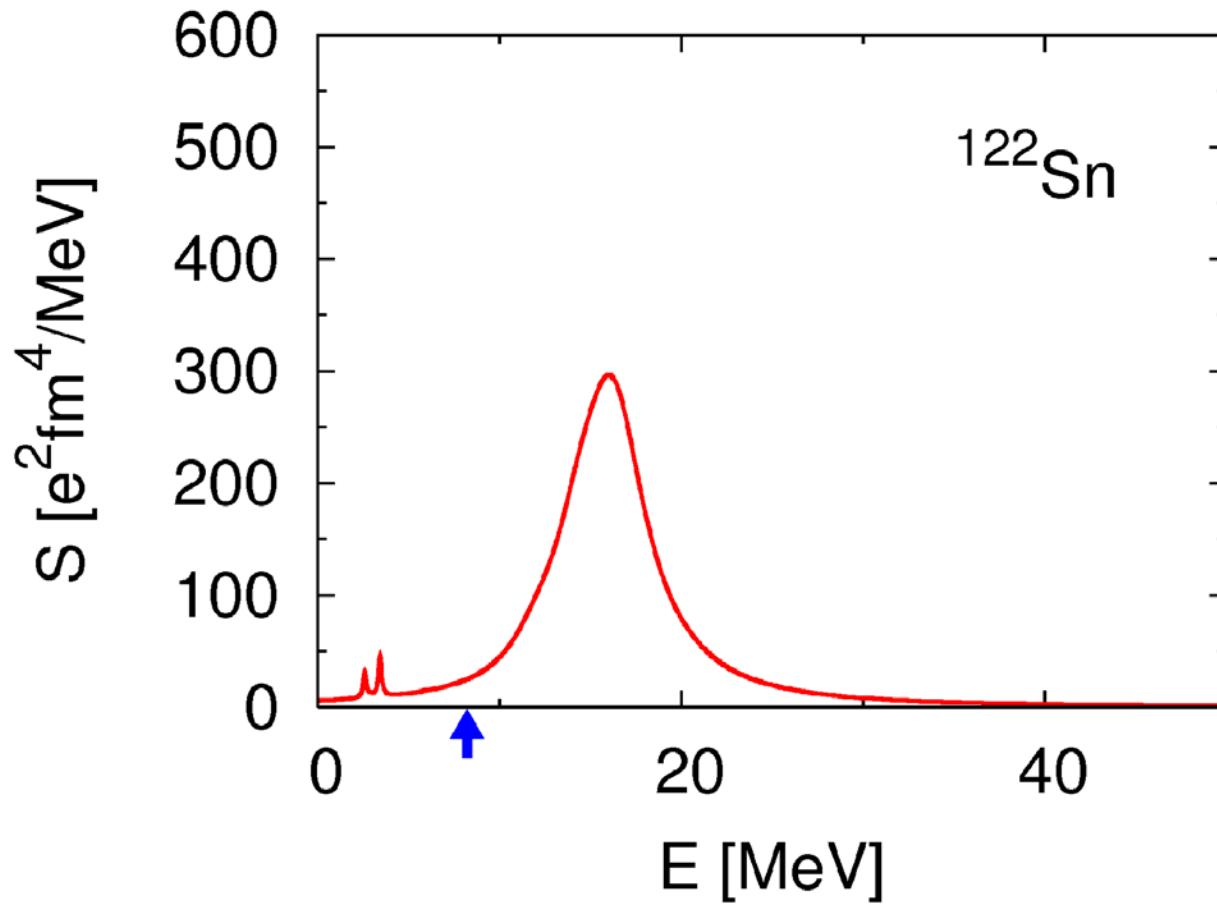
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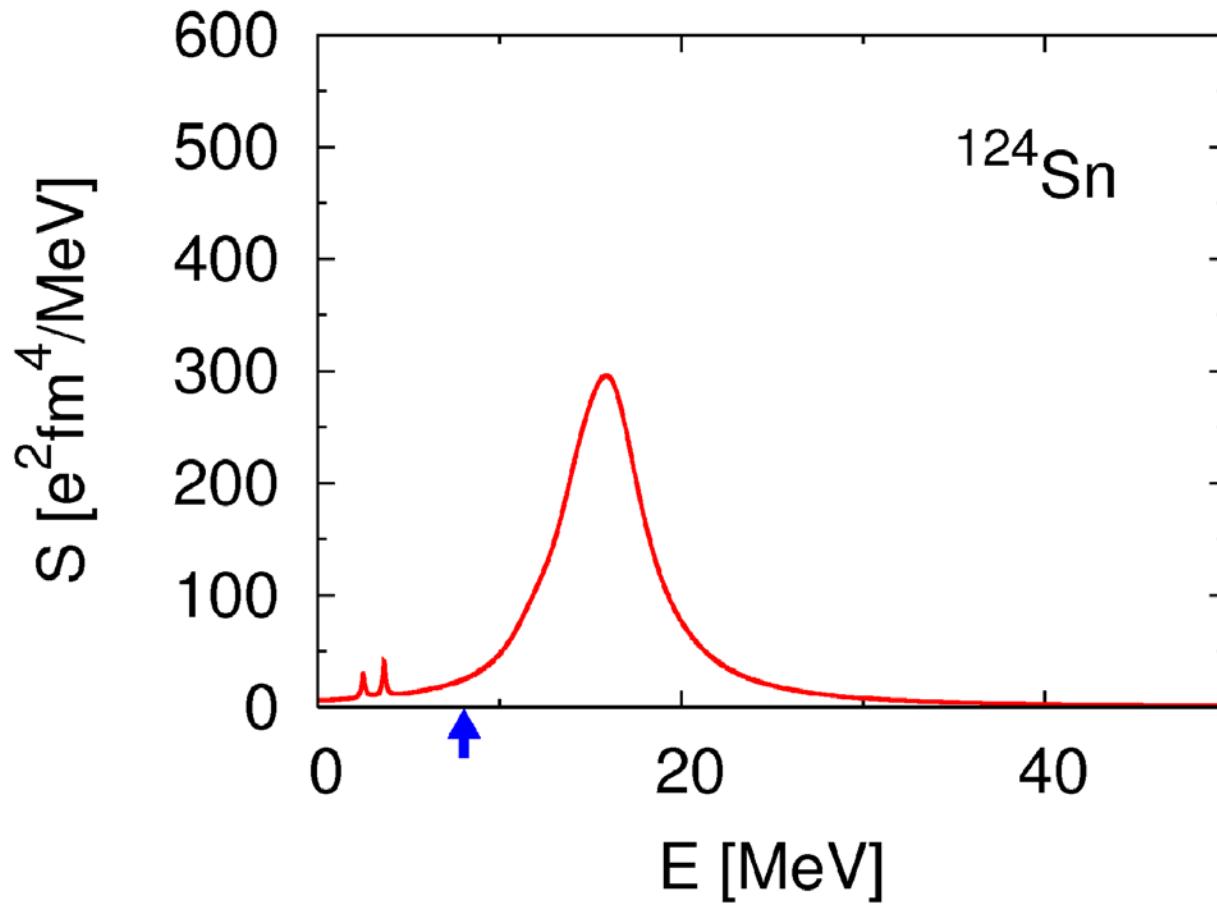
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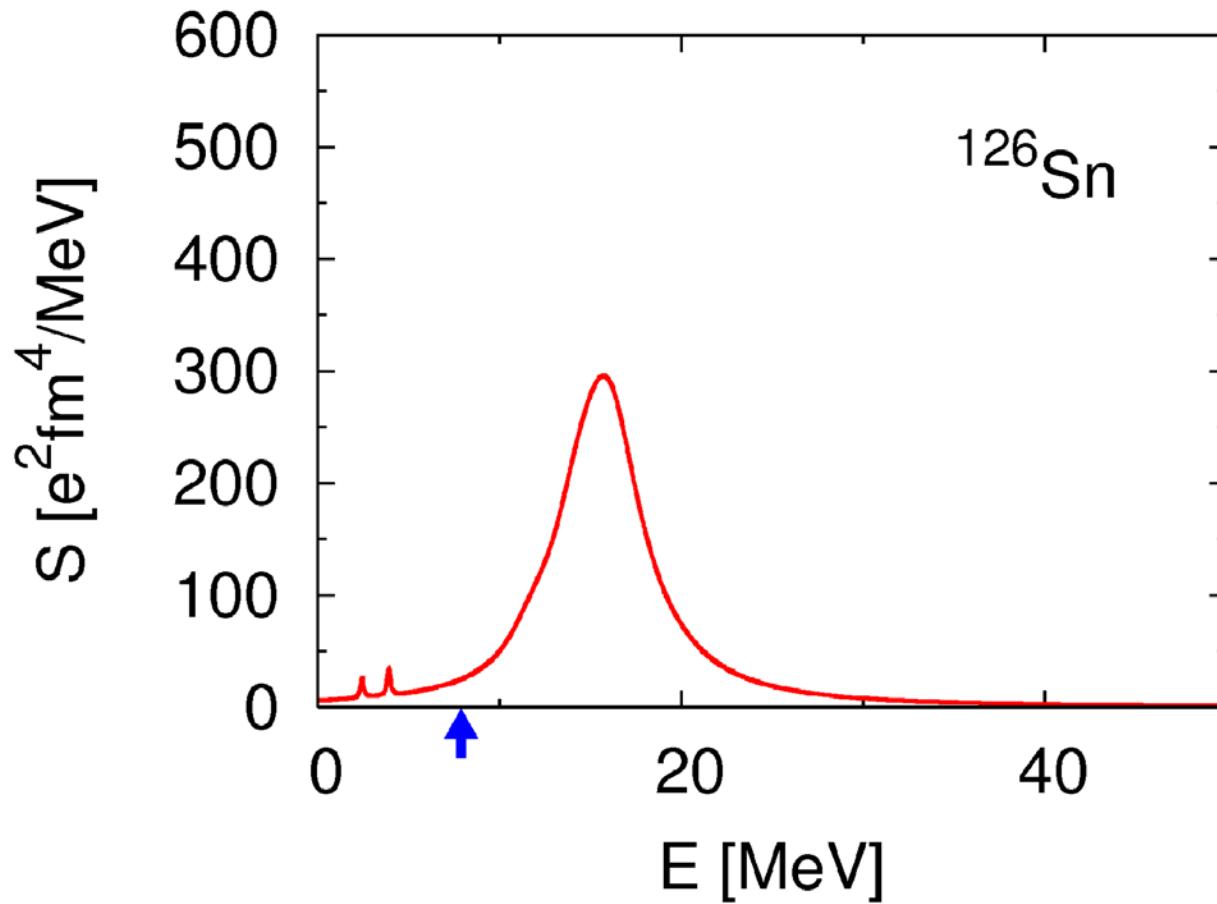
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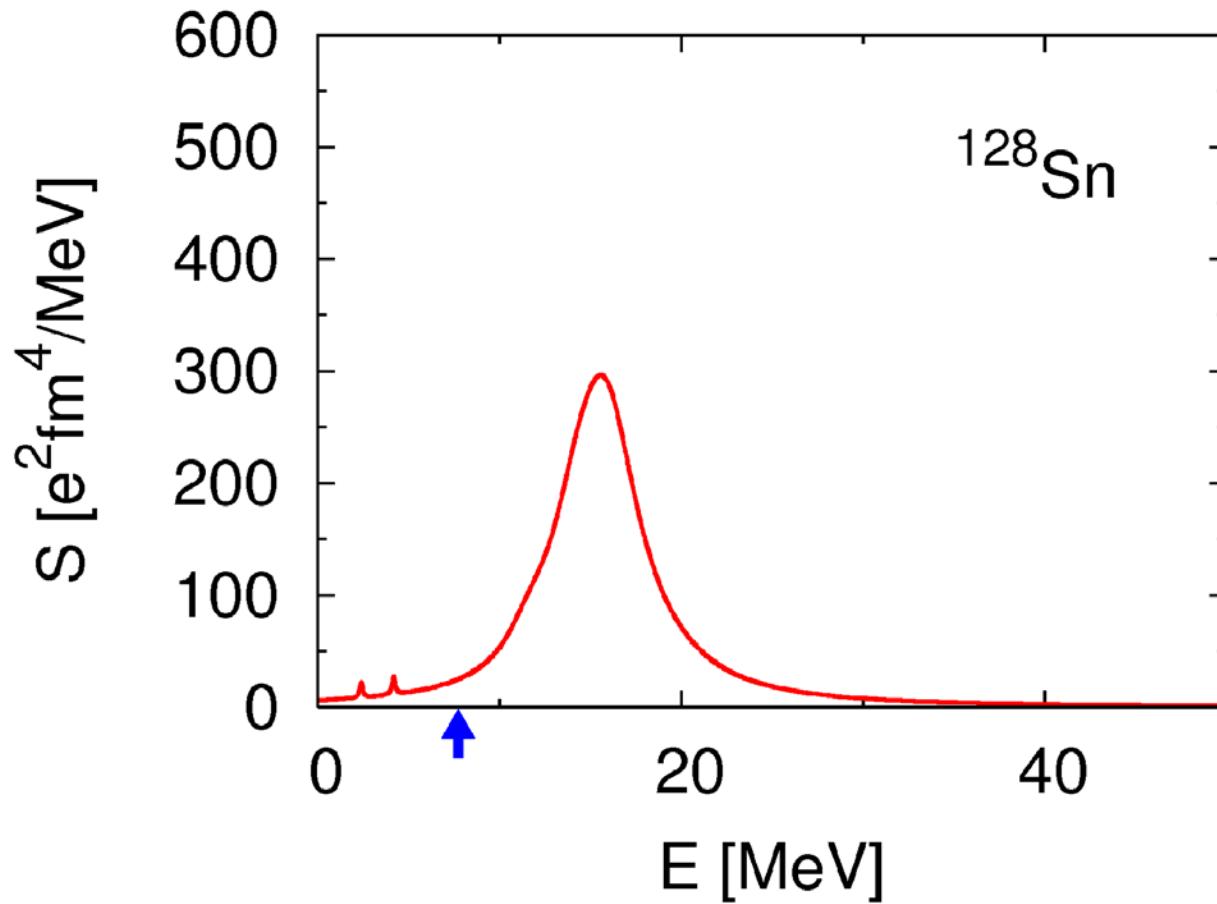
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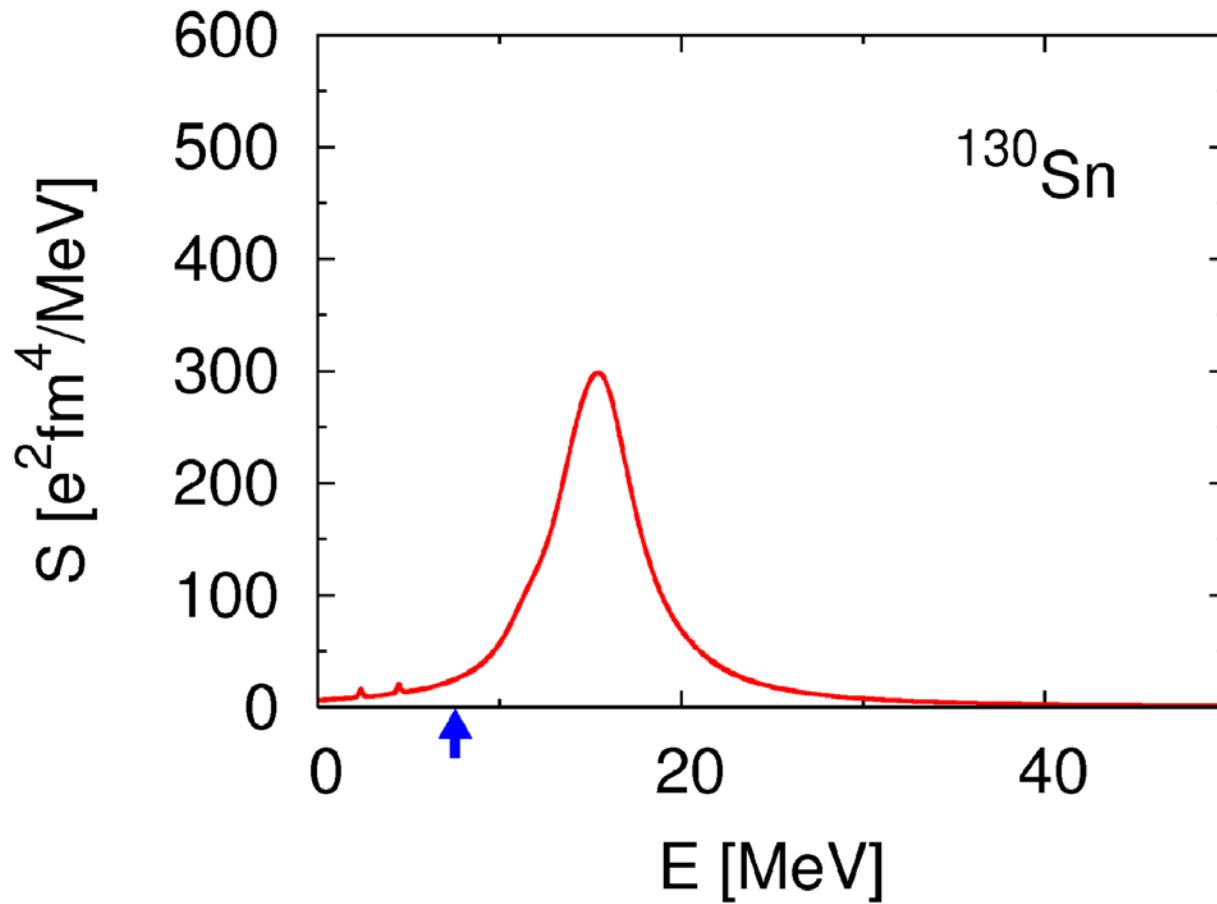
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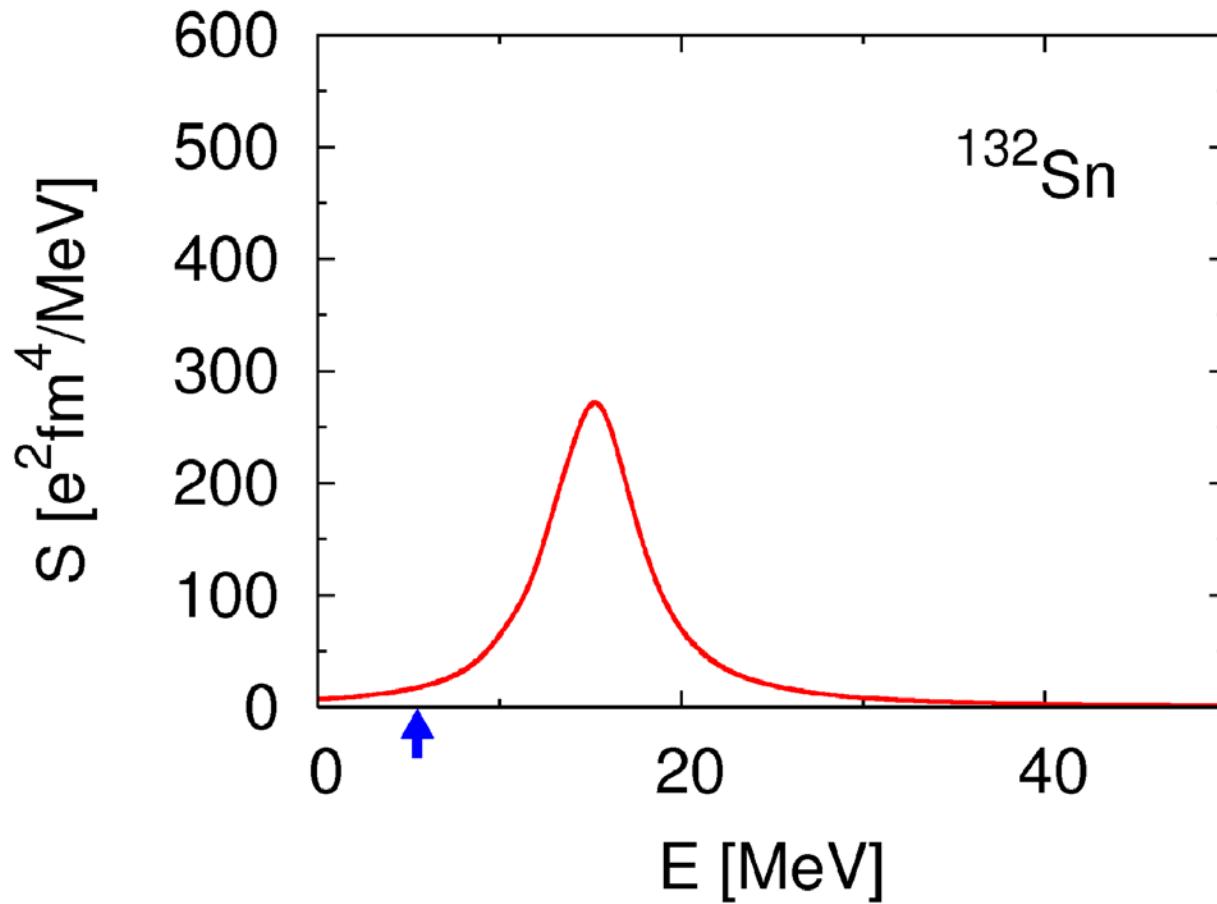
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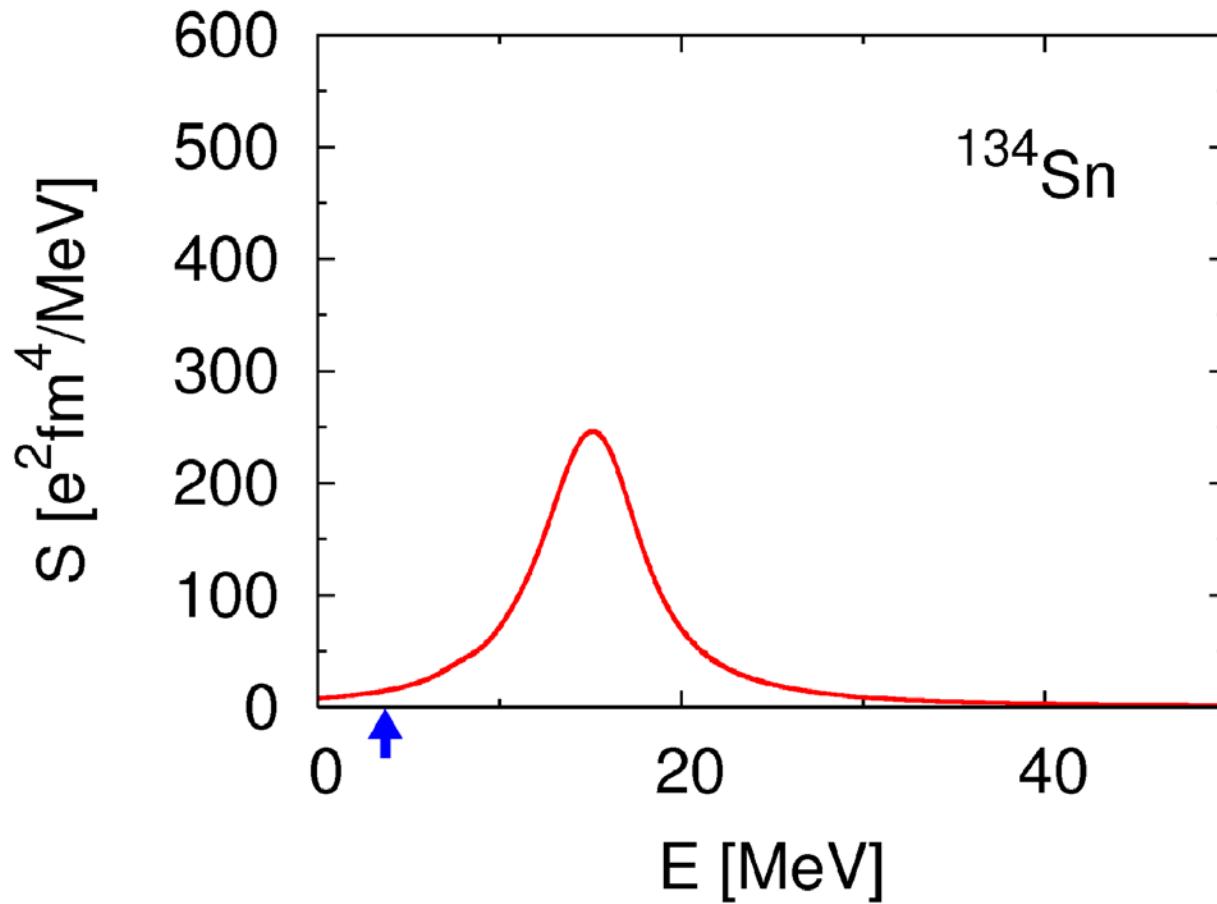
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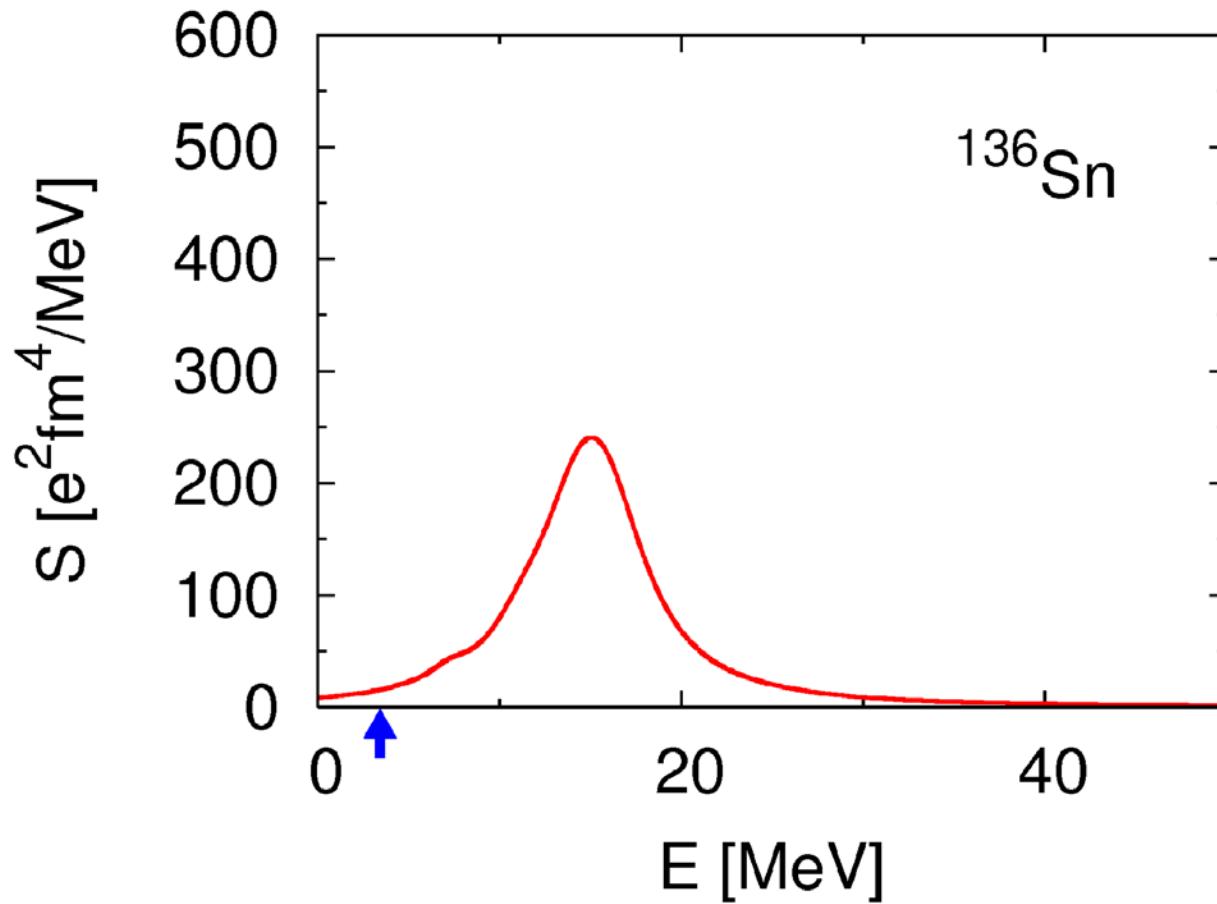
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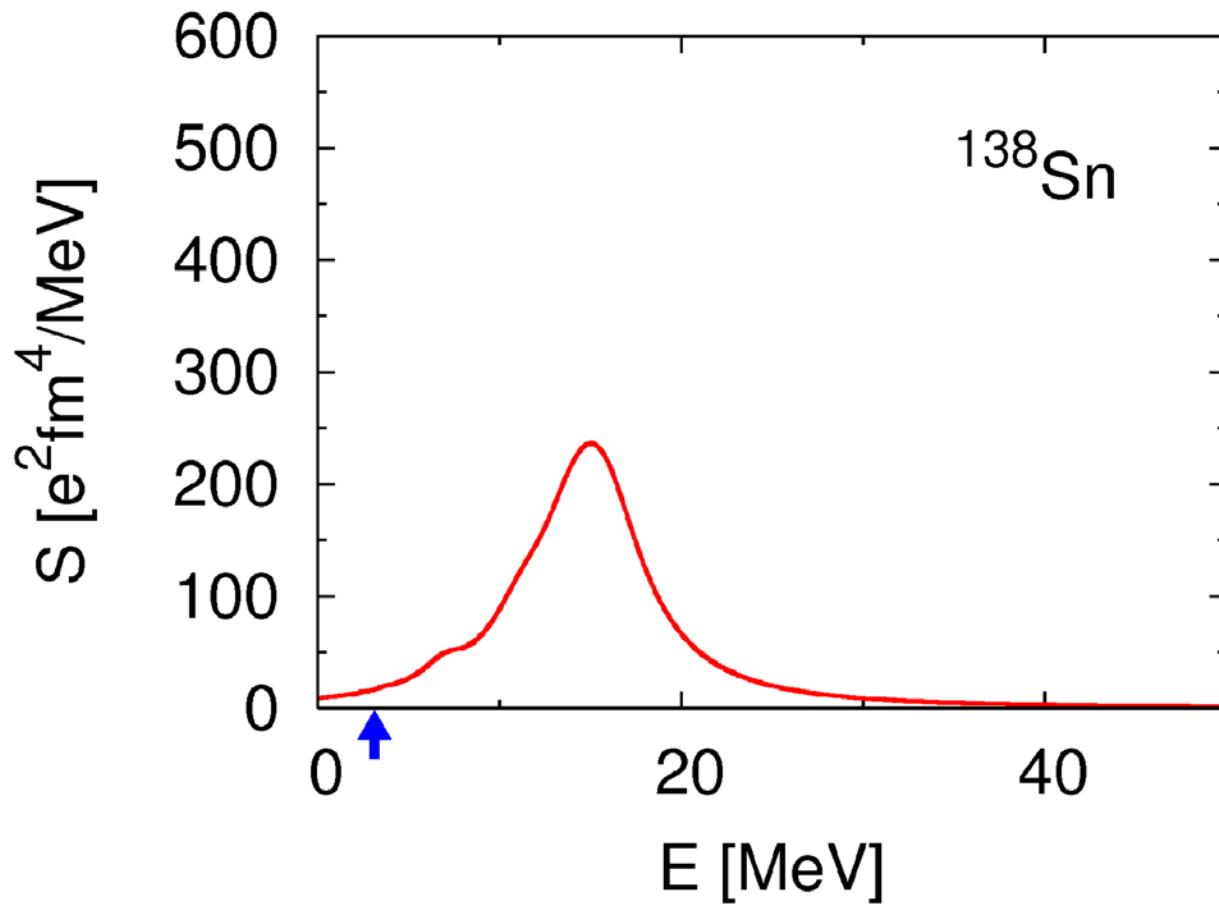
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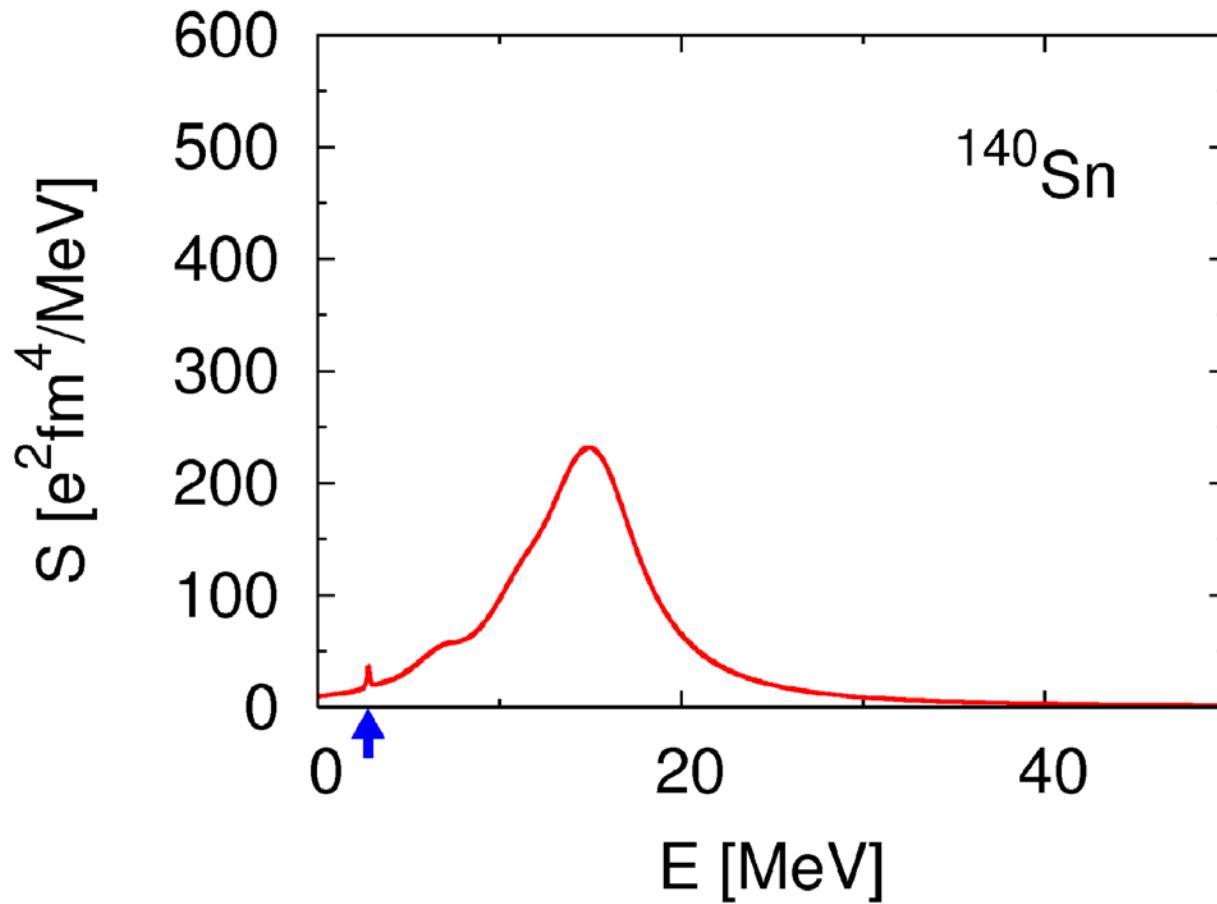
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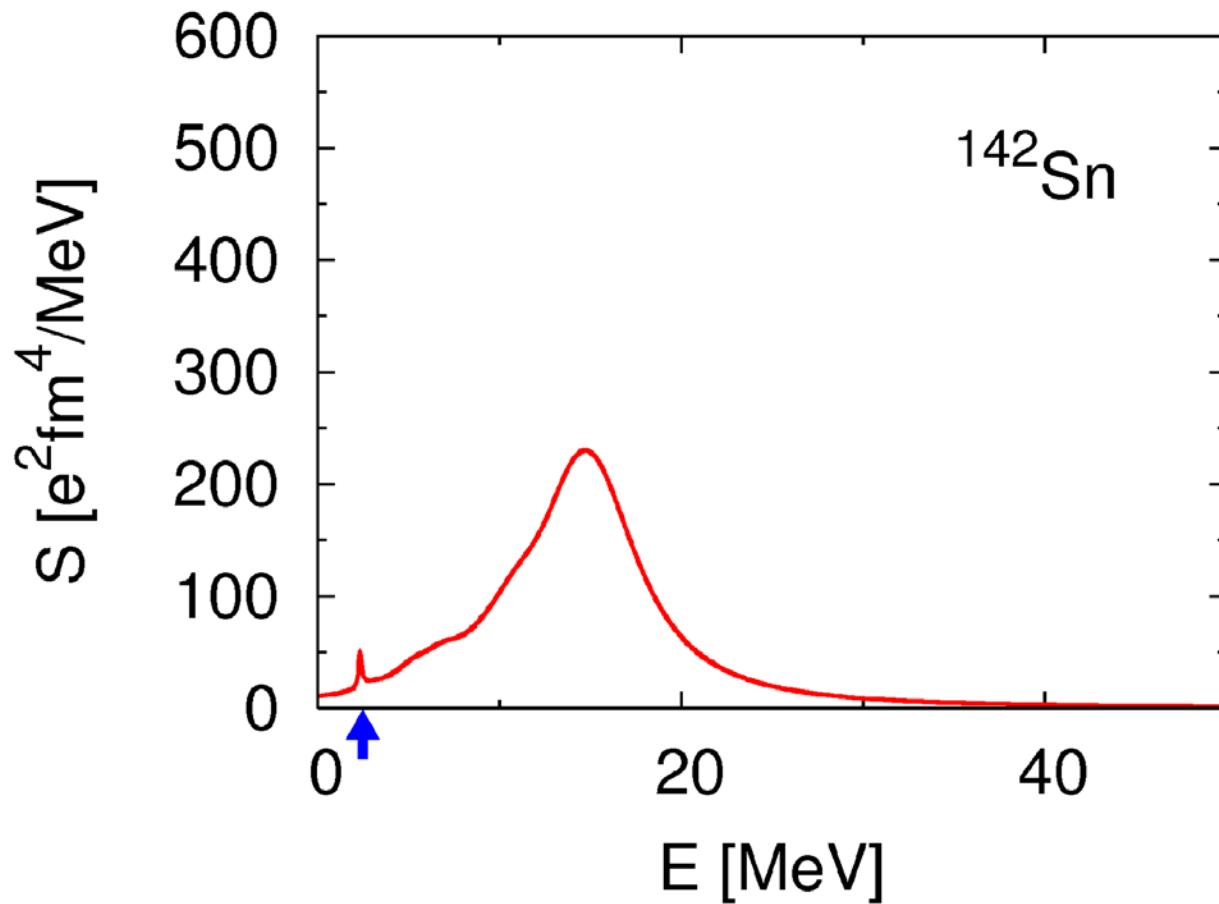
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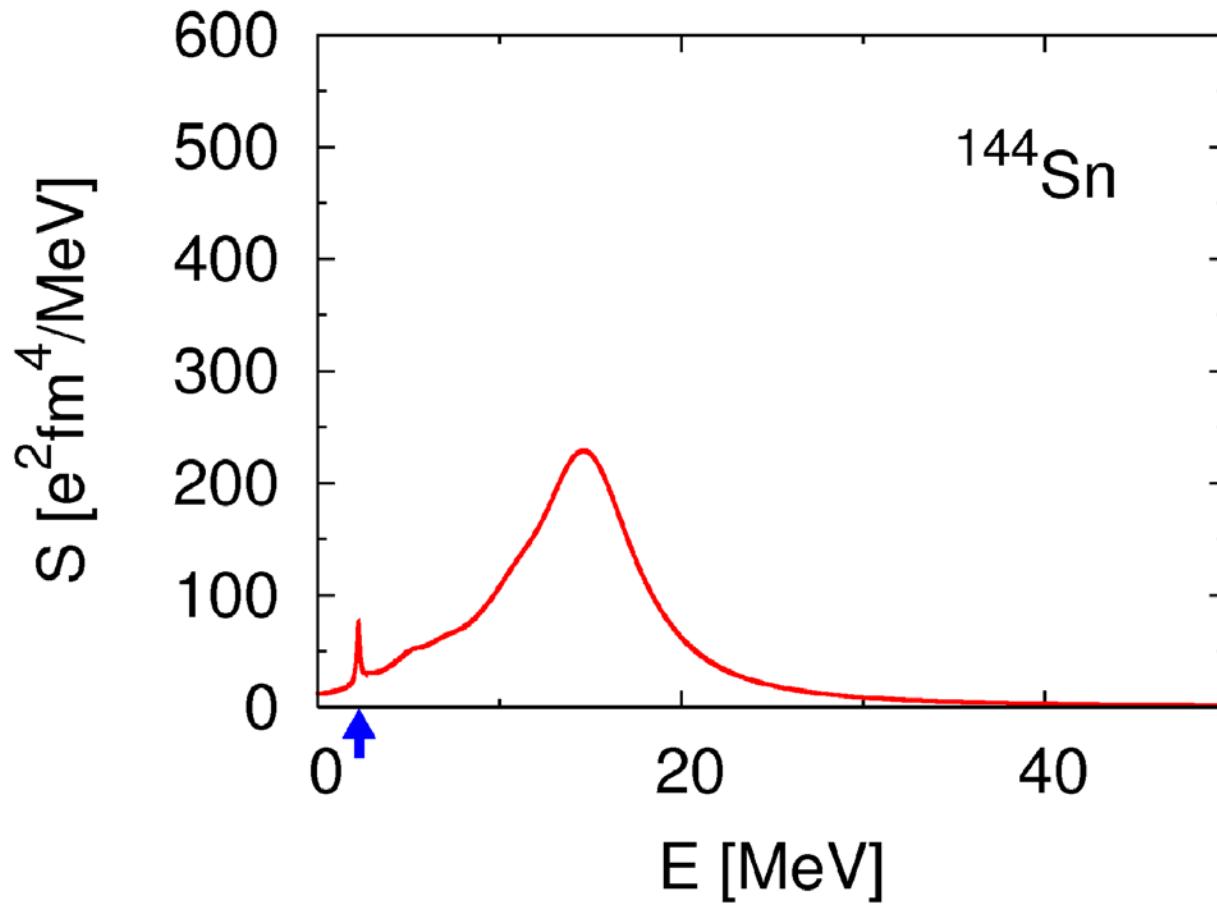
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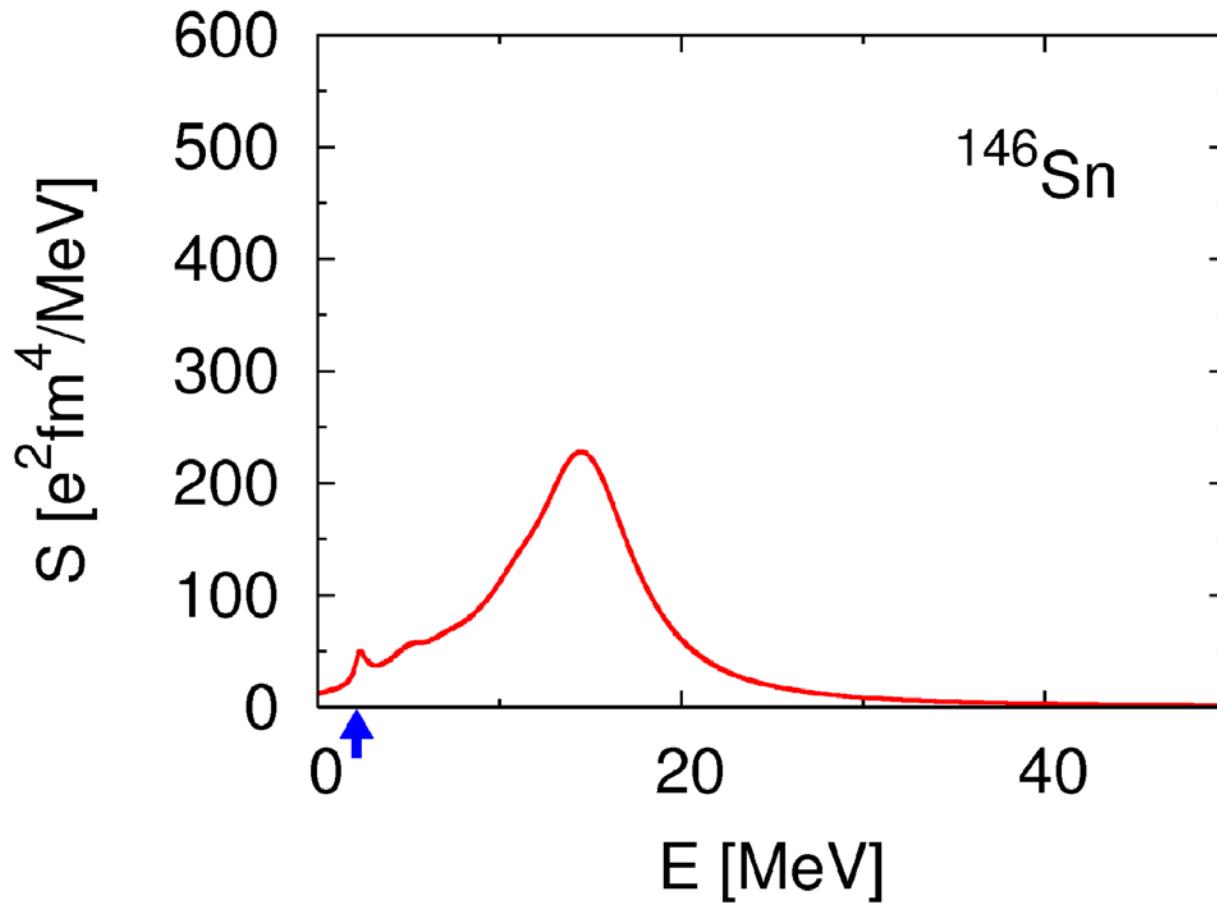
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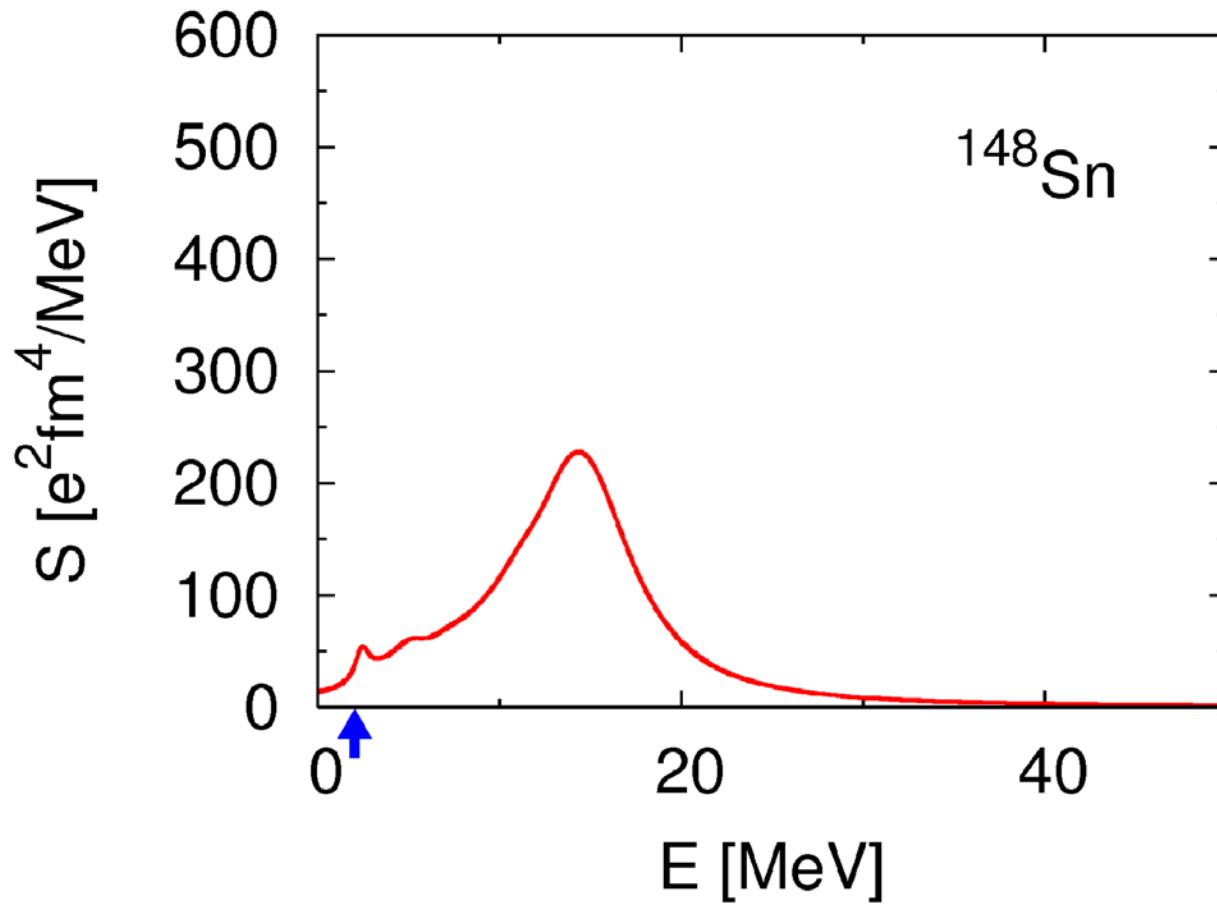
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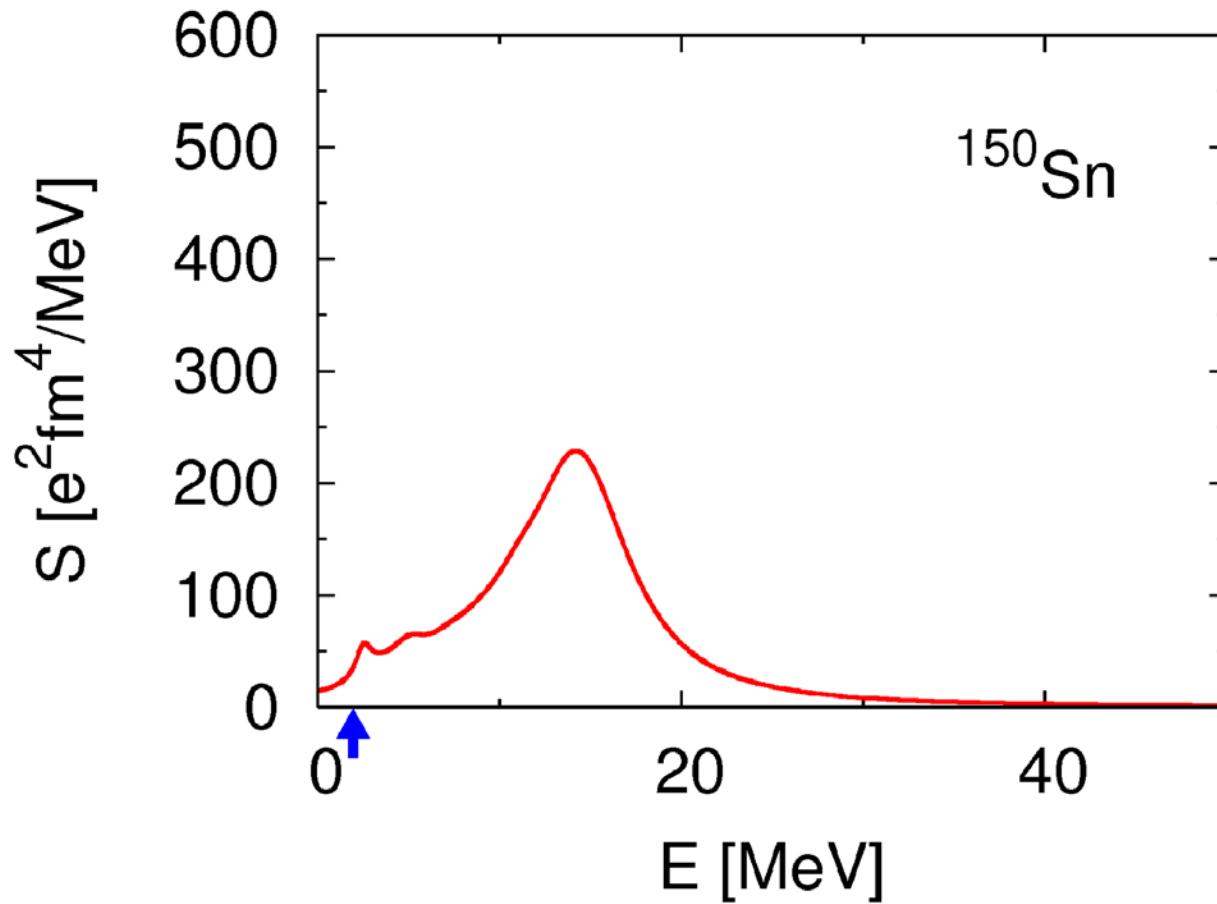
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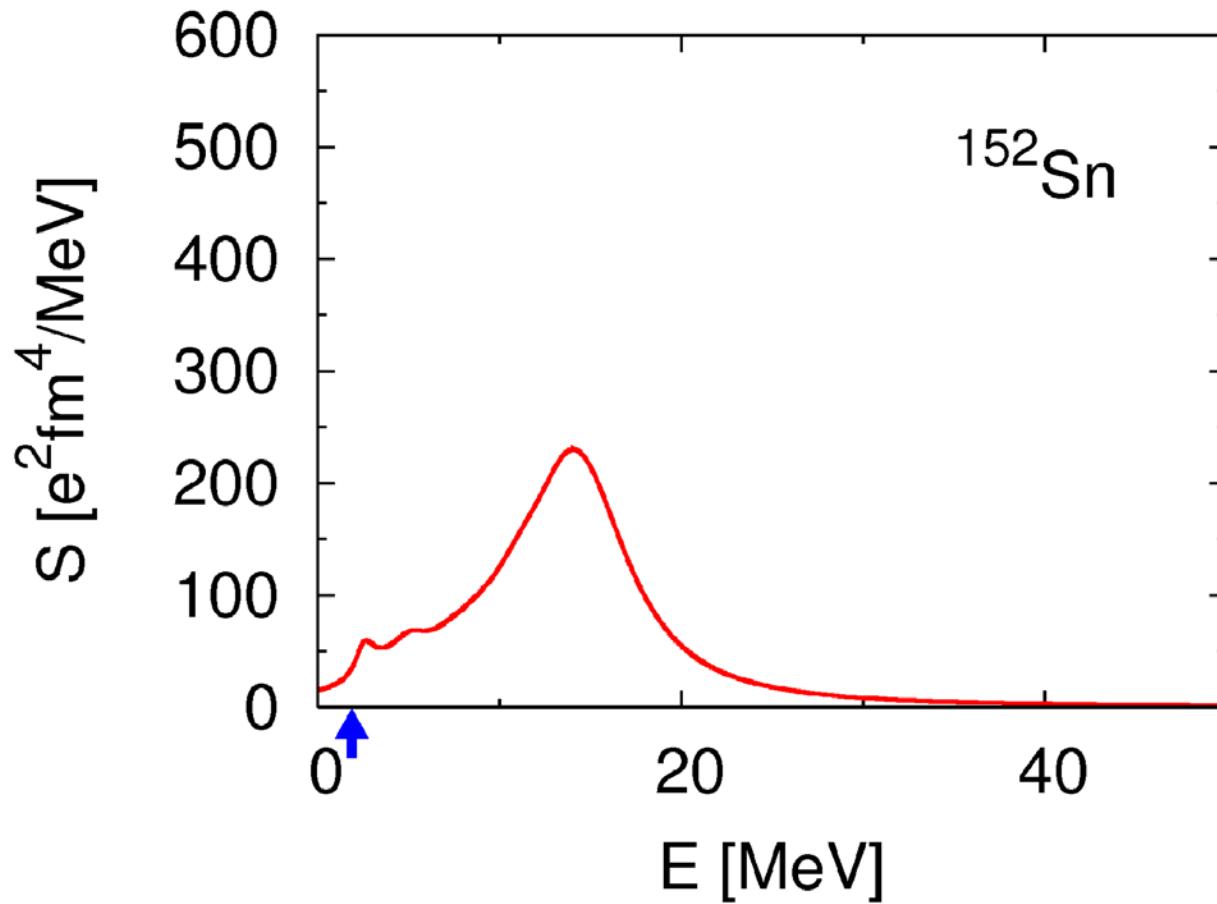
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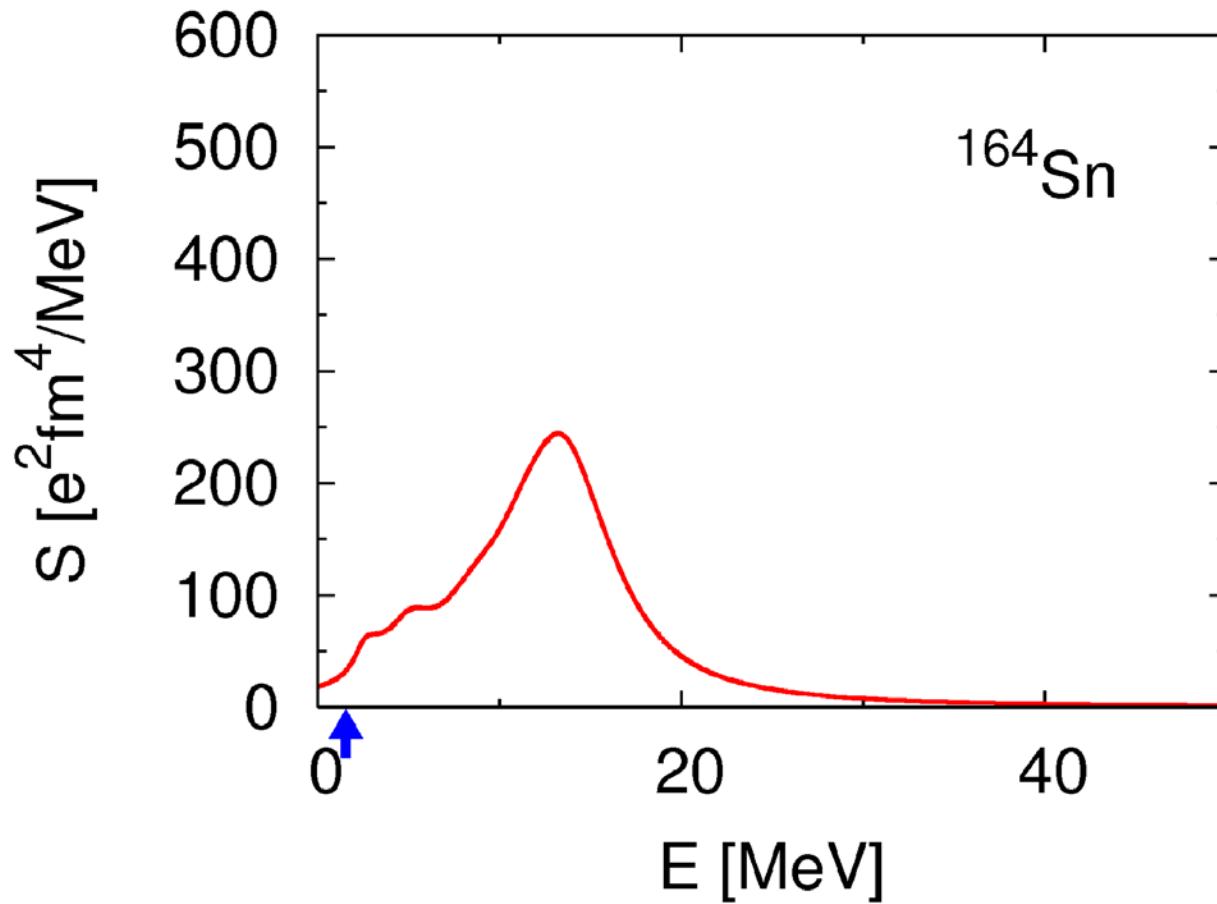


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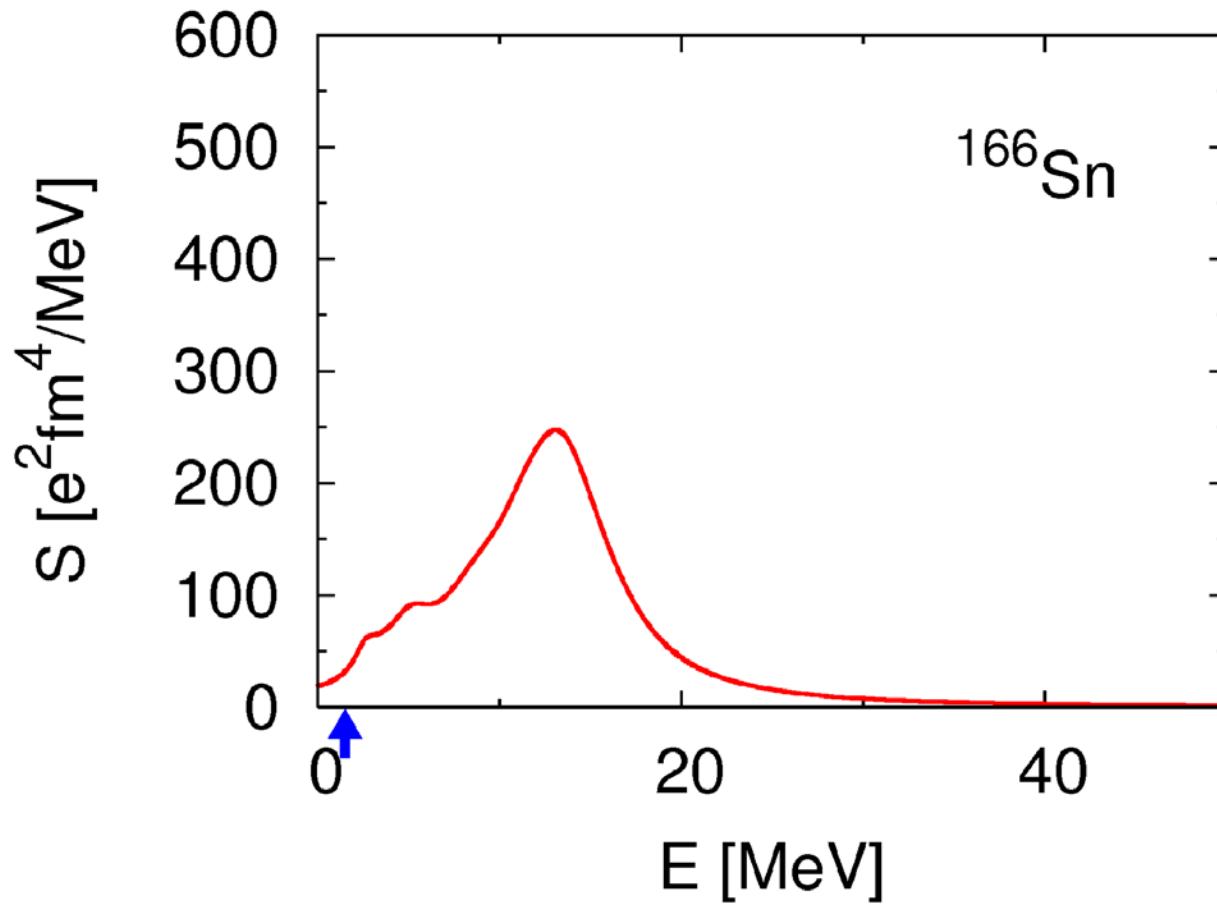


At  $A = 154 - 162$  ( $N = 104 - 112$ )  
ground states : deformed

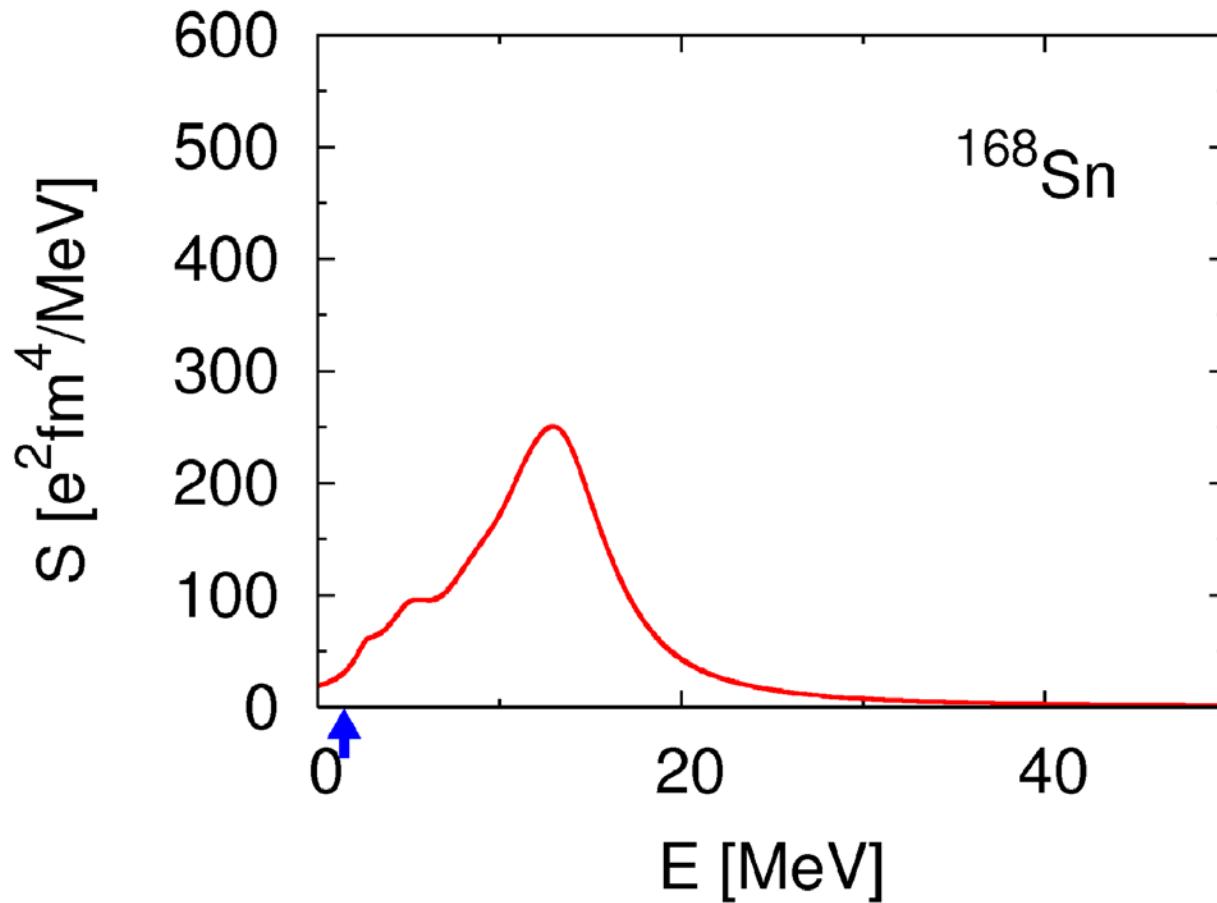
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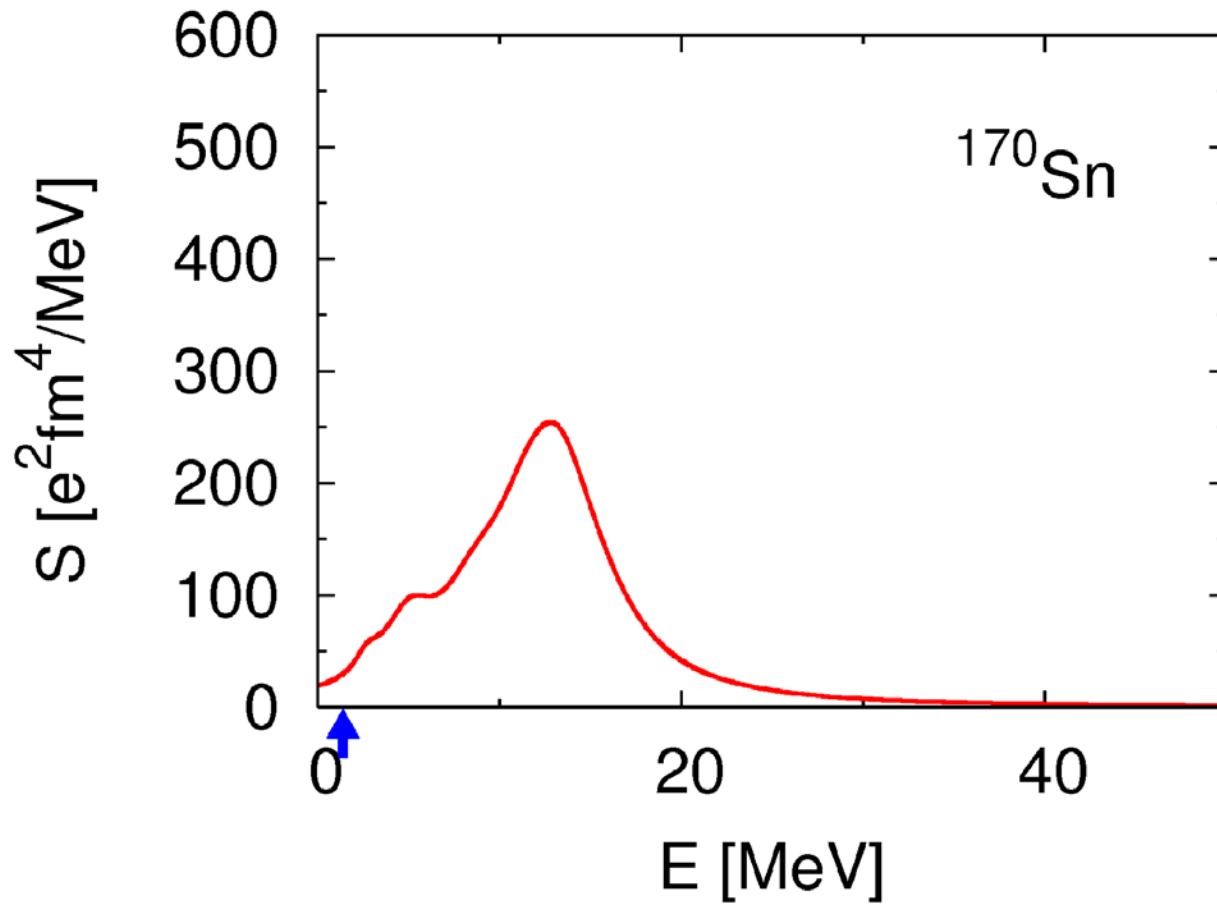
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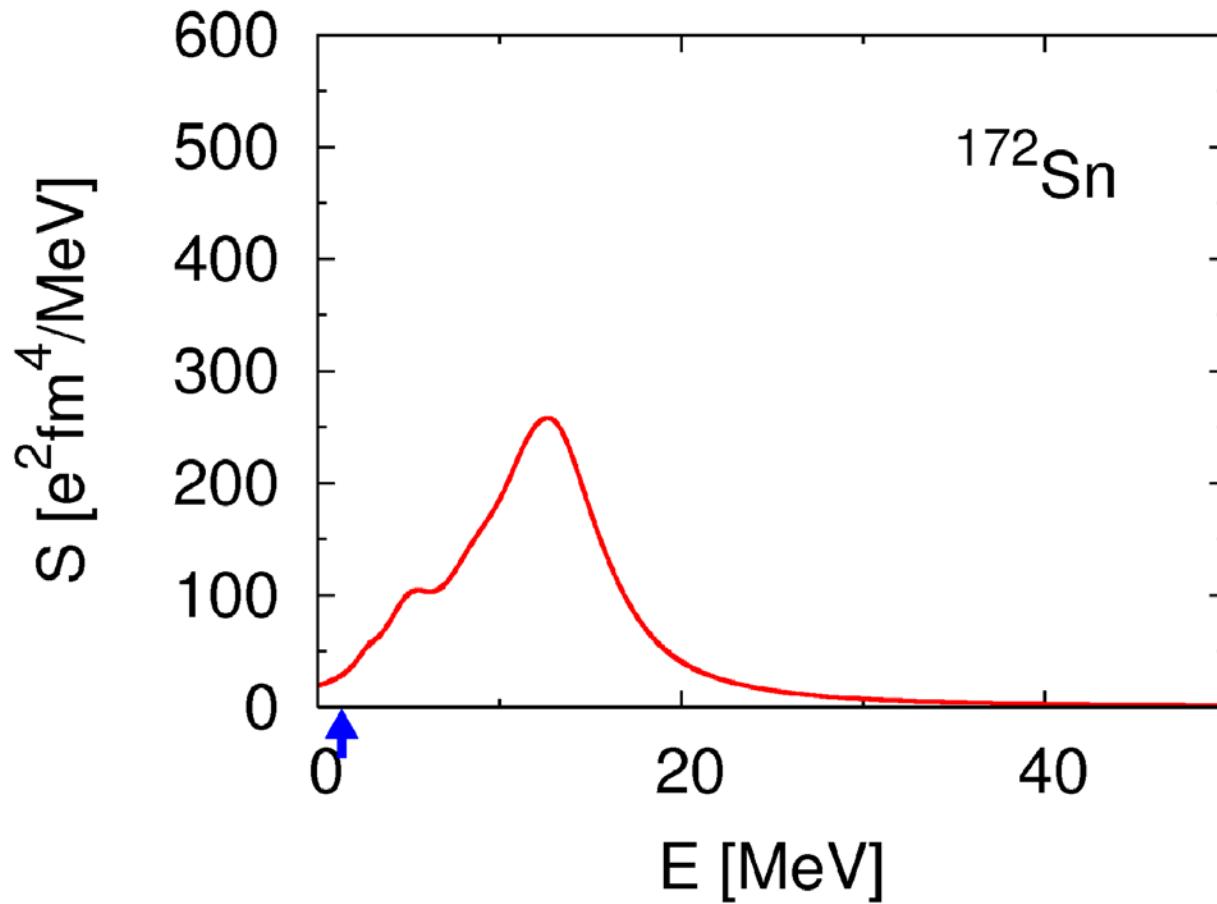
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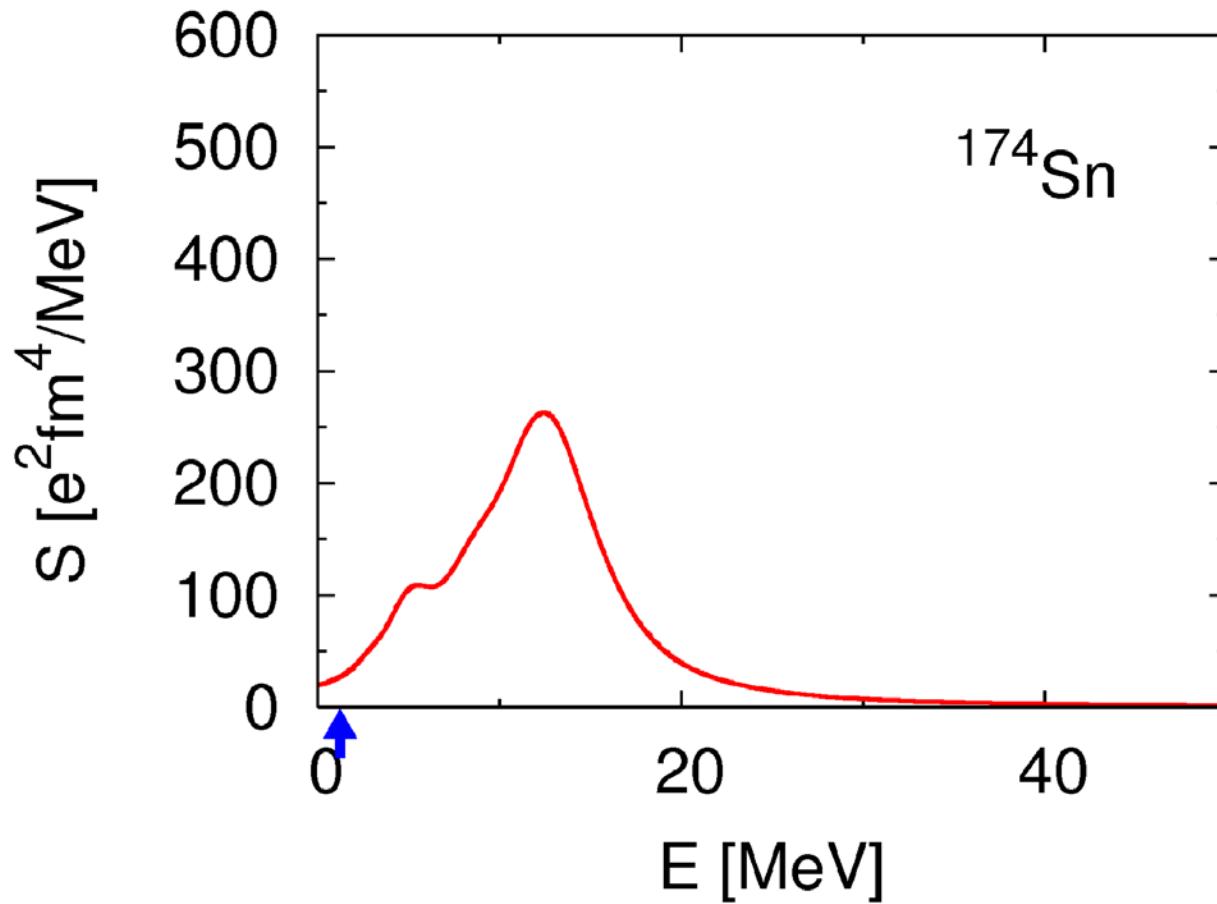
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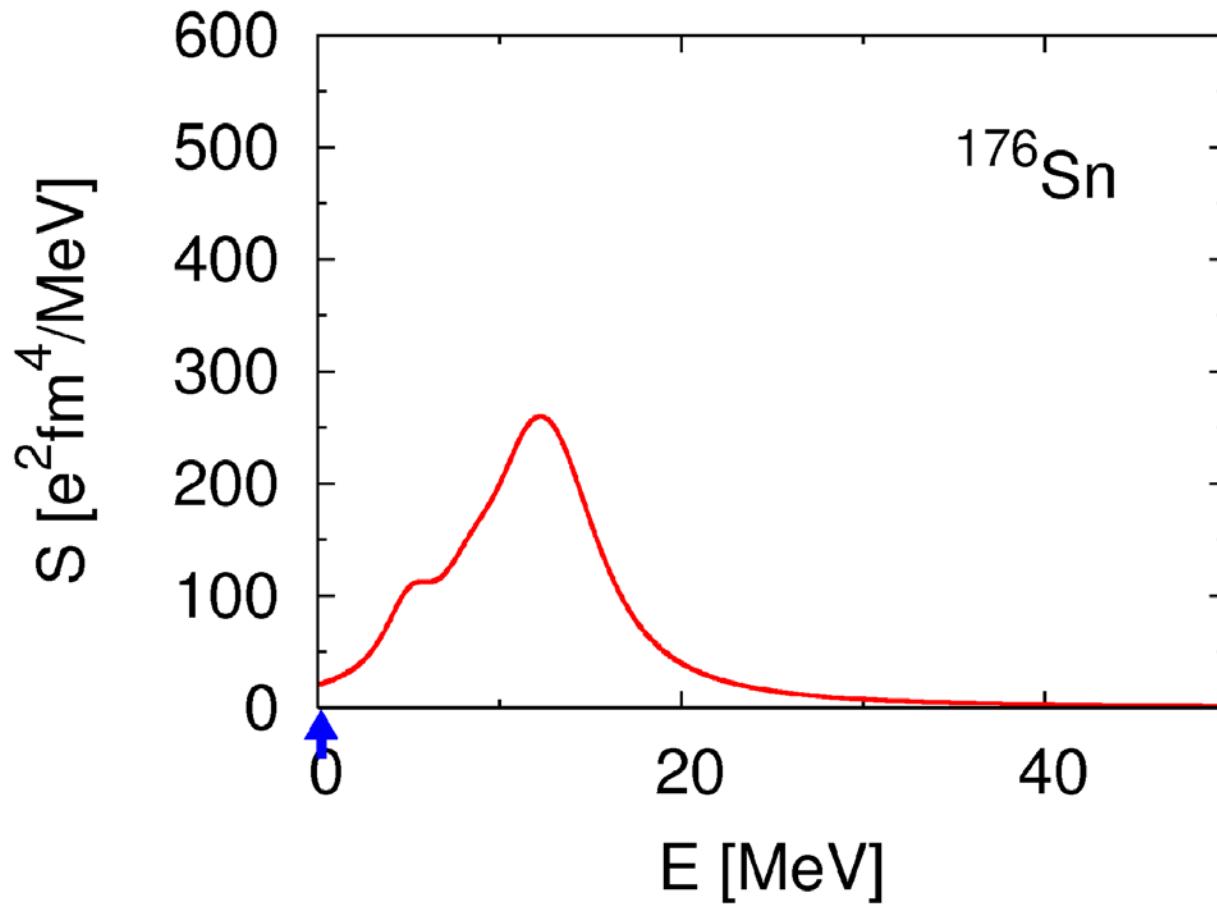
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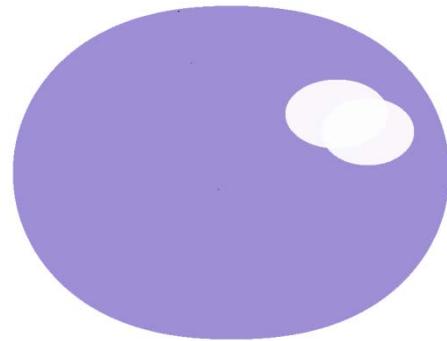
## Isoscalar $0^+$ strength functions



## 4. Deformed nuclei

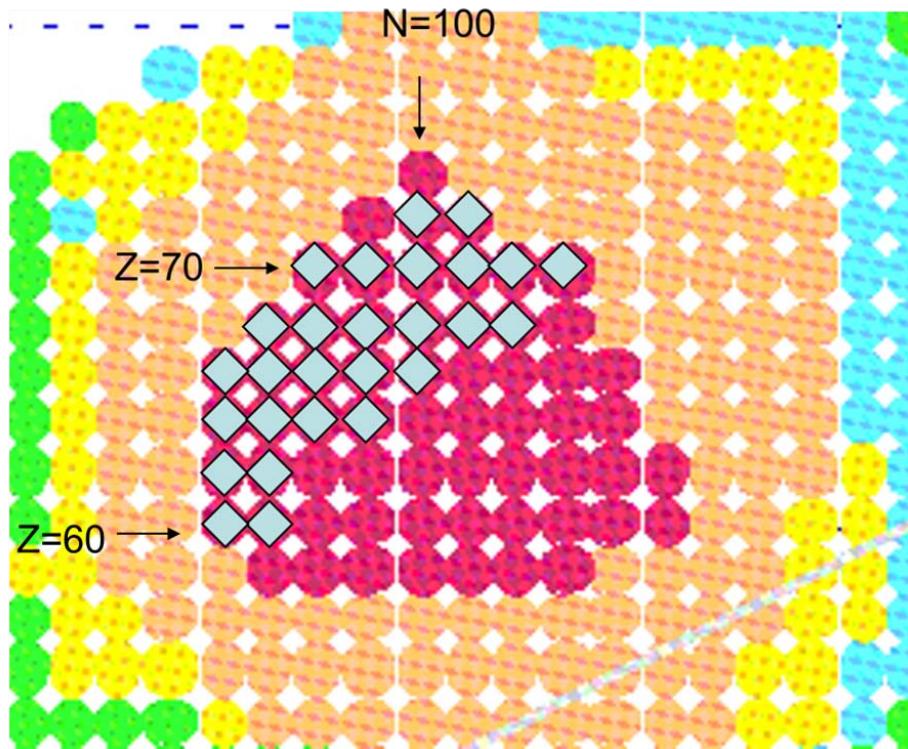
DFT breaks rotational symmetry in deformed nuclei.

Another code for deformed nuclei developed assuming axial symmetry and parity.



Quadrupole deformation  $\beta=0.3$   
Well deformed

# Deformed nuclei calculated

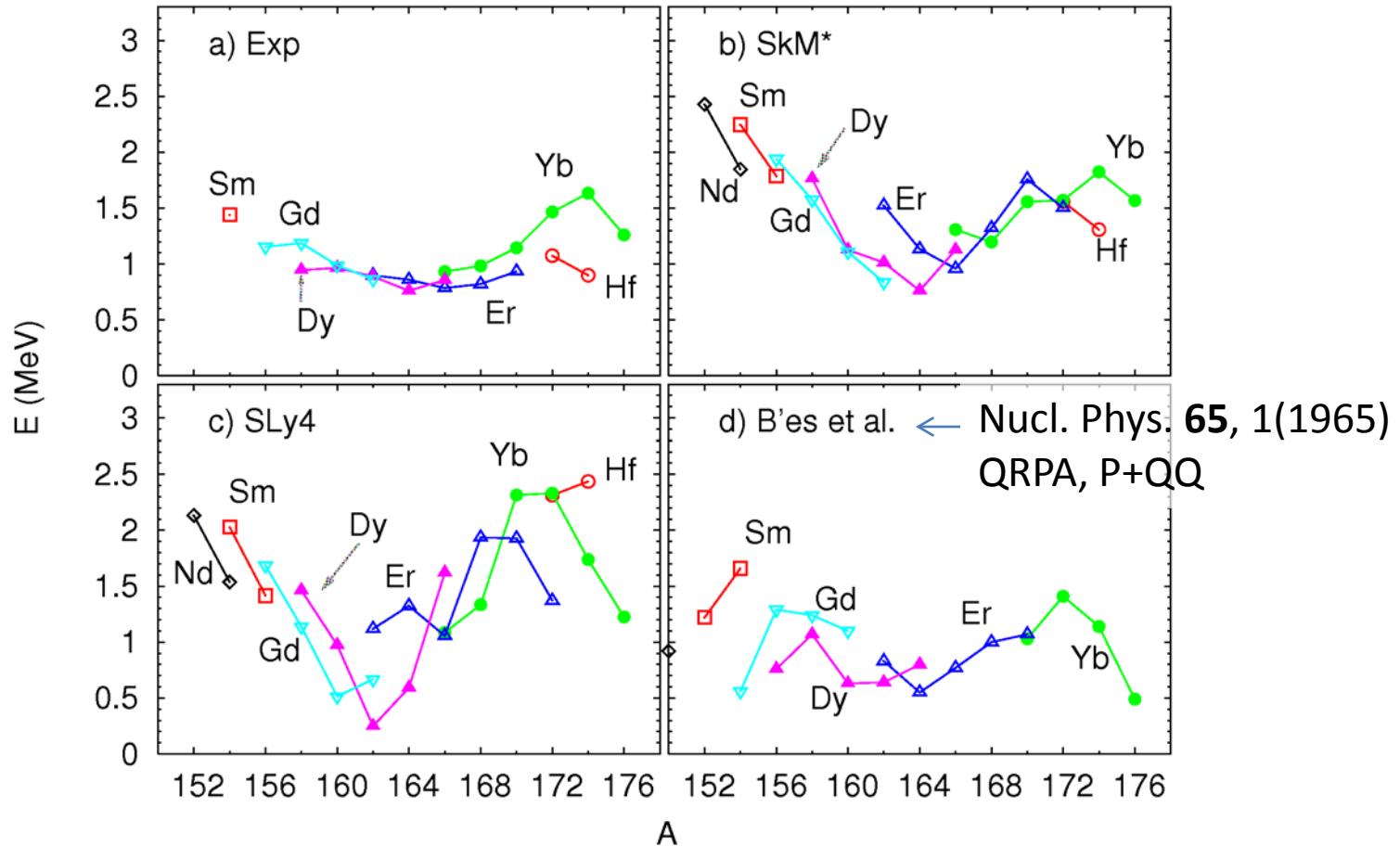


$\beta > 0.3$ ,  
(SkM\*)



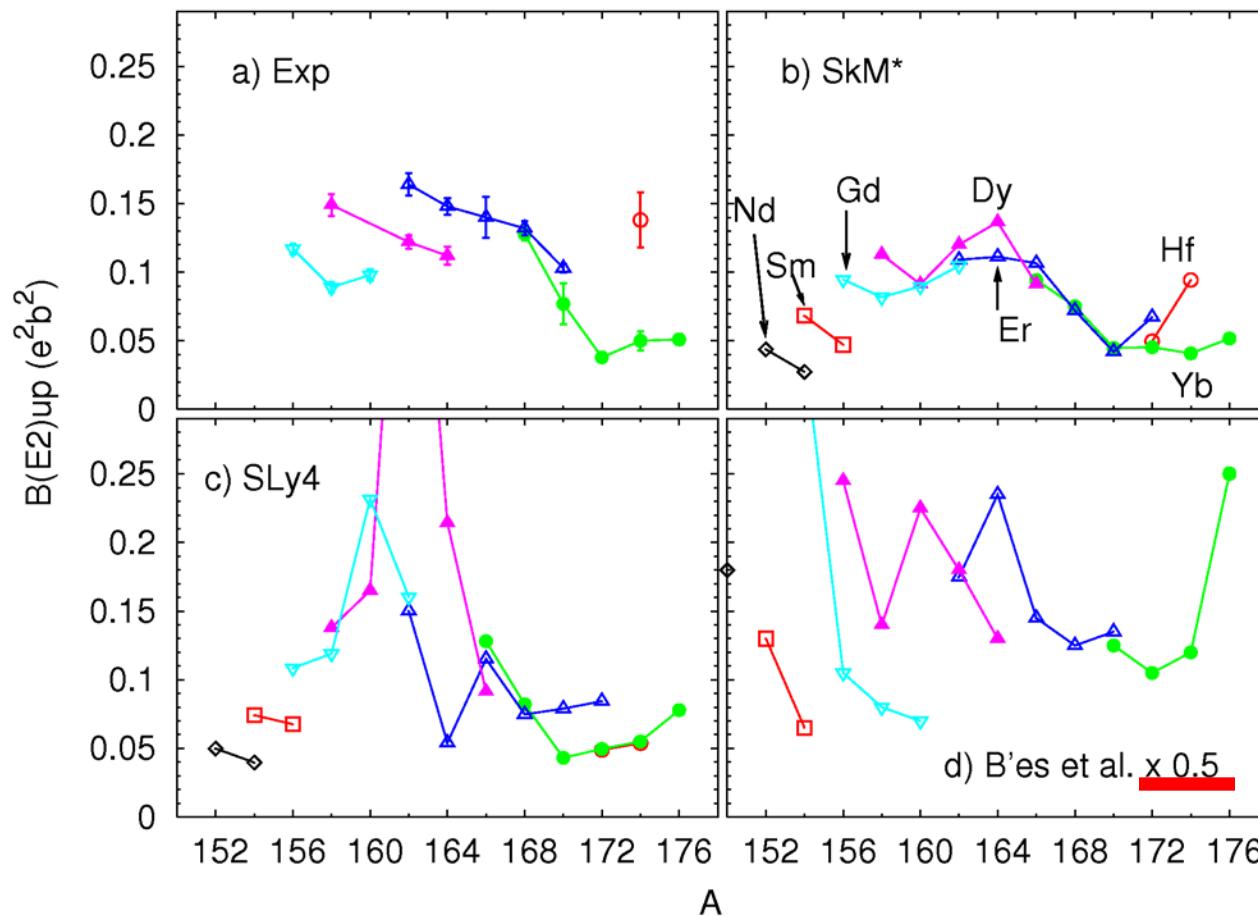
**Gamma-vibrational states  
measured**

# Energy of Gamma-vibrational states

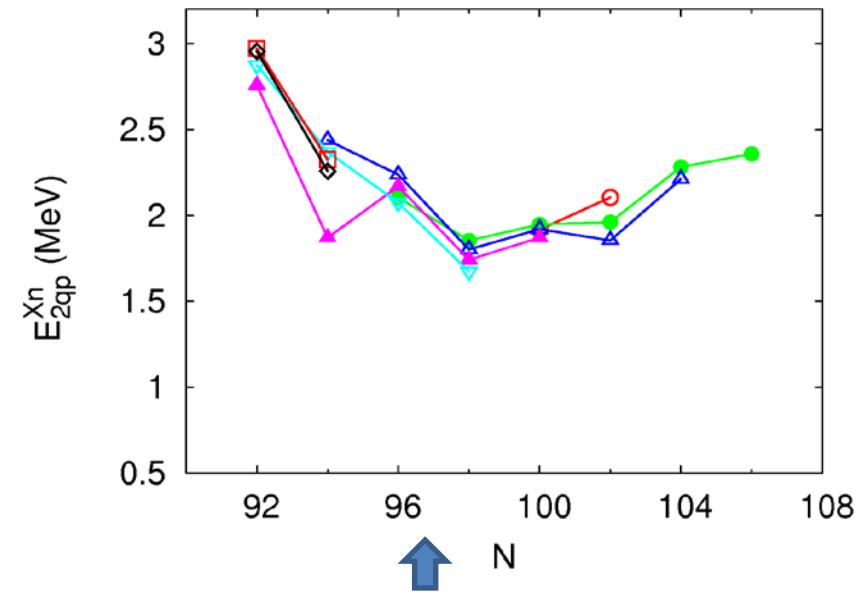
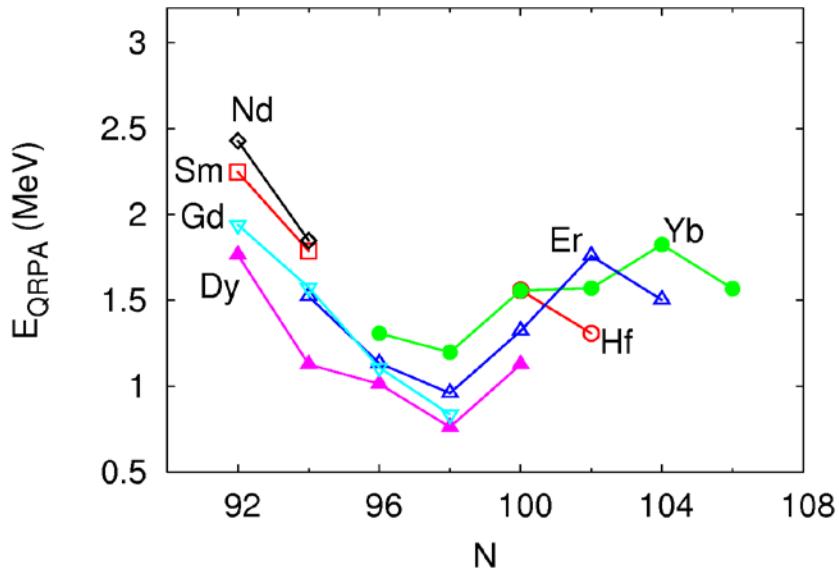


J. T. and J. Engel, Phys. Rev. C 84, 014332 (2011)

# $B(E2)^\uparrow$ of Gamma-vibrational states



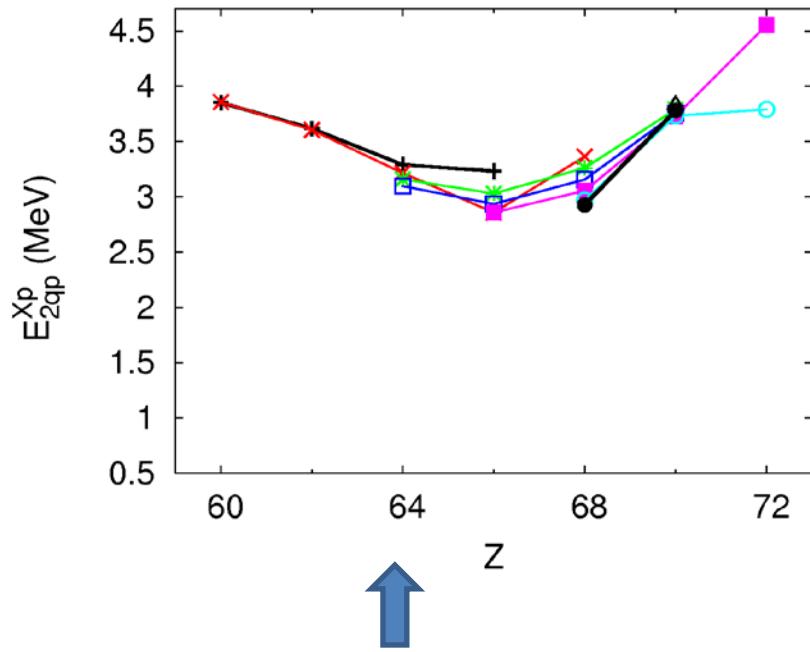
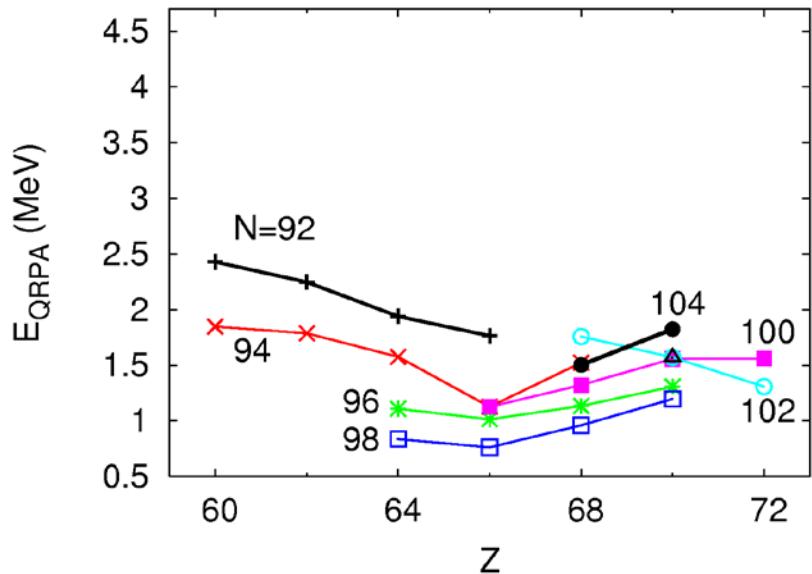
## *N-dependence of the gamma-vib. states (SkM\*)*



Two-quasiparticle energy of the comp. having the largest forward amp. of neutrons

Neutron unperturbed energy

## *Z-dependence of the gamma-vib. states ( $SkM^*$ )*



Two-quasiparticle energy of the comp. having the largest forward amp. of **protons**

Proton unperturbed energy

Correlation is seen in  
 $N$ - and  $Z$ - dependences of  $E_{QRPA}$  and  $E_{2qp}$

The  $N$  and  $Z$ -dependences of the calculated  $\gamma$ -vibrational states  
are dominated by the two-quasiparticle states

The experimental data show the weaker  $N$ - and  $Z$ - dependences  
than the calculation



The reality has more configuration mixing than QRPA.

## 5. Summary

1. It is becoming possible to calculate not only ground but also excited states of a much larger number of nuclear species than before thanks to powerful parallel computers.

The remarkable enhancement of the transition strength is found in the low-energy region of nuclei near the neutron drip line in a variety of isotopic chains and  $J^\pi$ .

2. Calculated results of  $\gamma$ -vibrational states have been compared with the exp. data systematically. They are not bad, but more many-body correlations are seen in the data.