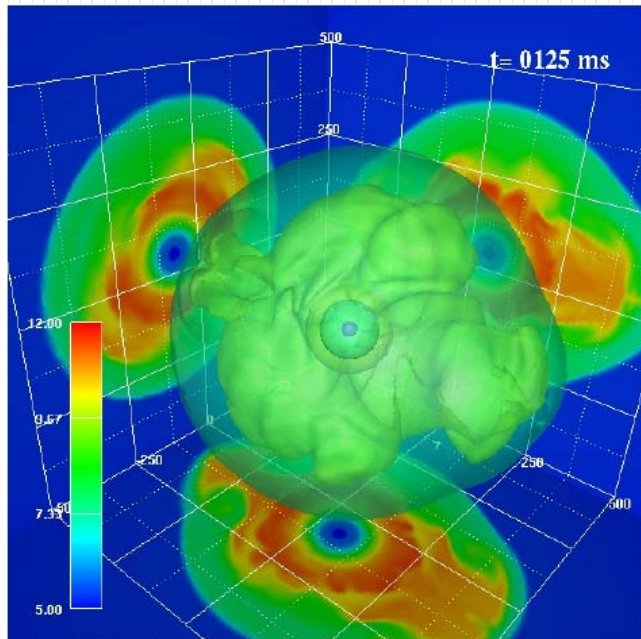


# 超新星爆発の3Dシミュレーション

Takiwaki, T., Kotake, K., & Suwa, Y. 2011, submitted to ApJ; arXiv:1108.3989  
and recent result



Tomoya Takiwaki  
National Astronomical  
Observatory of Japan  
**HPCI researcher**

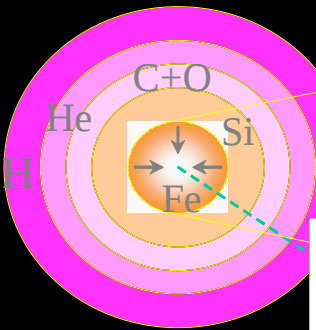
# Supernovae

## neutrino driven explosion

**core collapse**

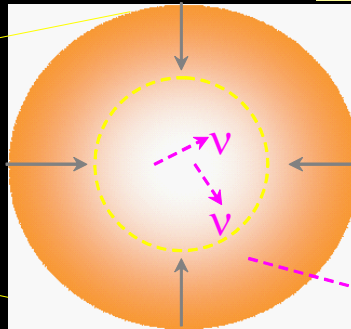
$$M \gtrsim 8M_{\odot}$$

$$e^{-} + p \rightarrow \nu_e + n$$



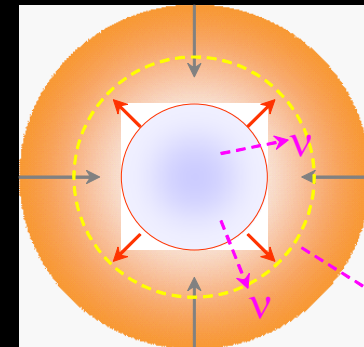
**$\nu$  trapping**

$$\rho_c \sim 10^{12} \text{g/cm}^3$$



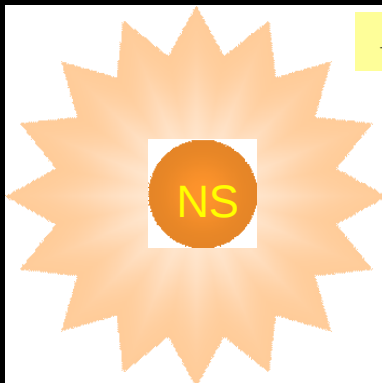
**core bounce**

$$\rho_c \sim 3 \times 10^{14} \text{g/cm}^3$$

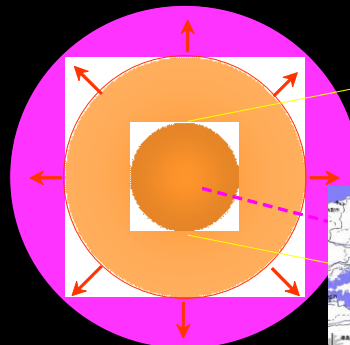


**SN explosion**

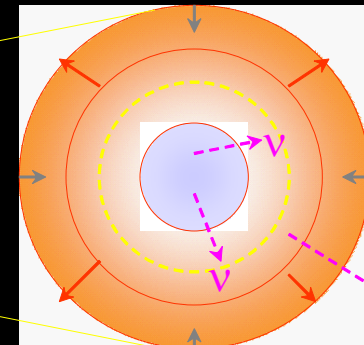
$$E_{exp} \sim 10^{51} \text{erg}$$



**shock in envelope**



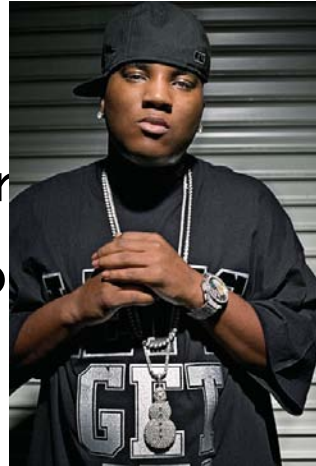
**shock propagation in core**



# History of supernovae studies

-  ase(Colgate & 6)

imulation  
ce of neutr

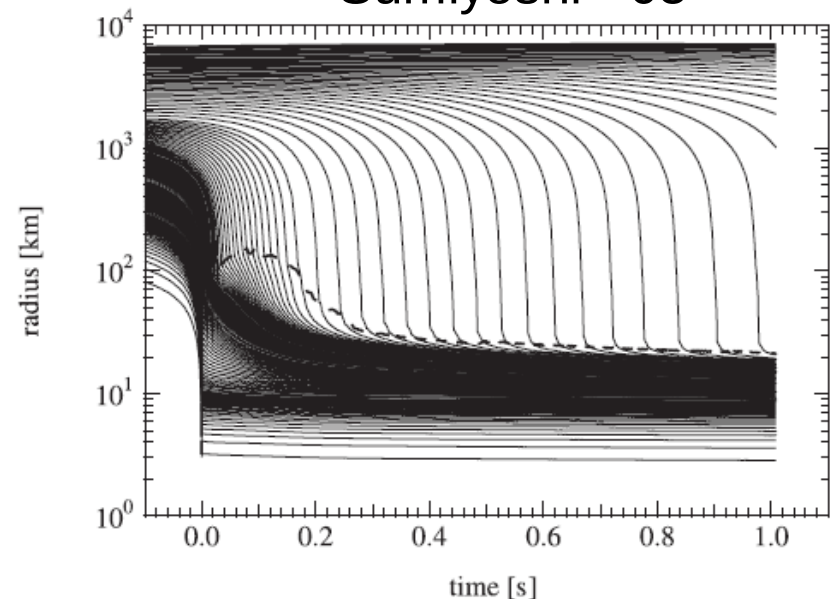
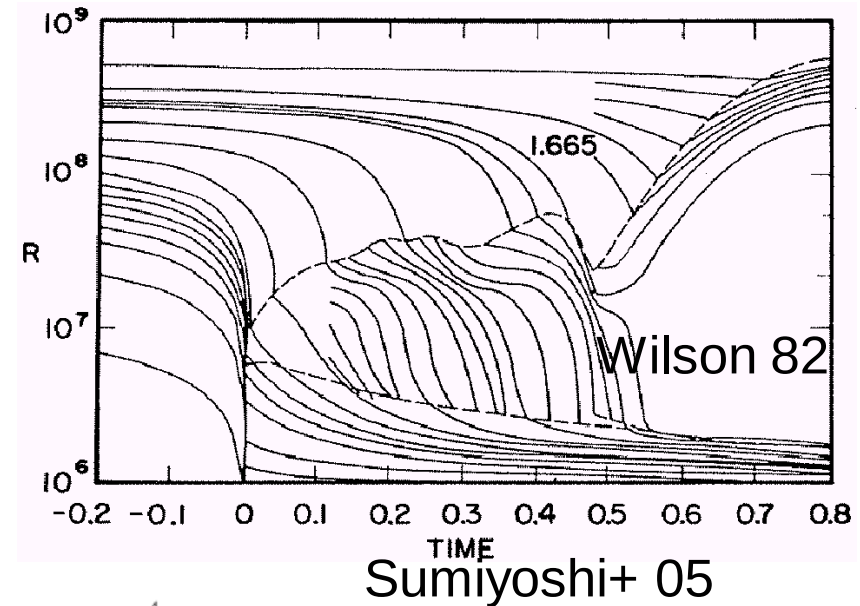


- Young Phase (Wilson 82)



hi et al. ' 05)  
simulation could  
the supernovae

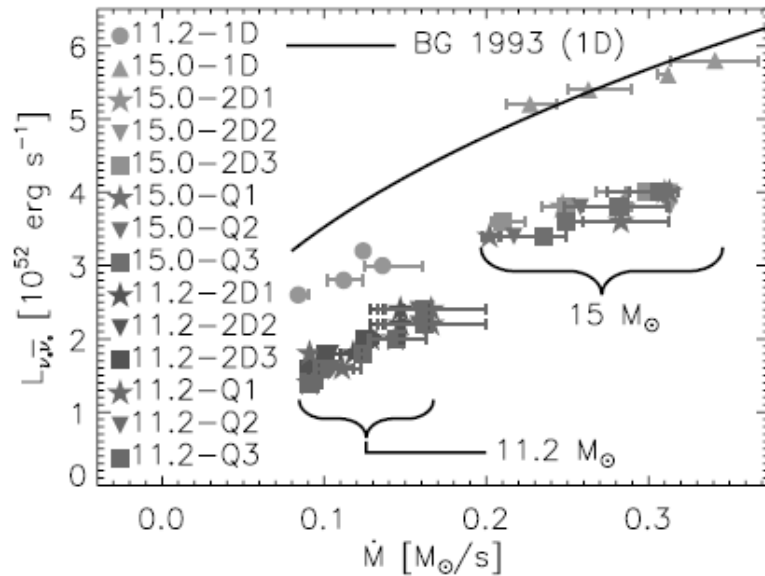
Supernovae modelers devote  
about 50 years to solve neutrino  
transport with adequate accuracy.



# Breakthrough by 2D simulations

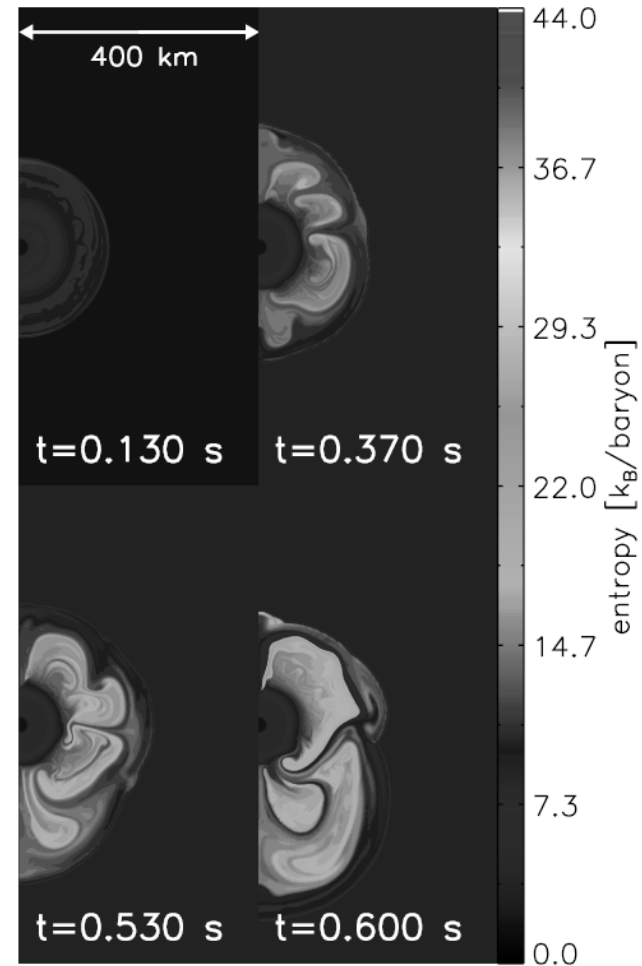
## Luminosity

Murphy & Burrows 2008



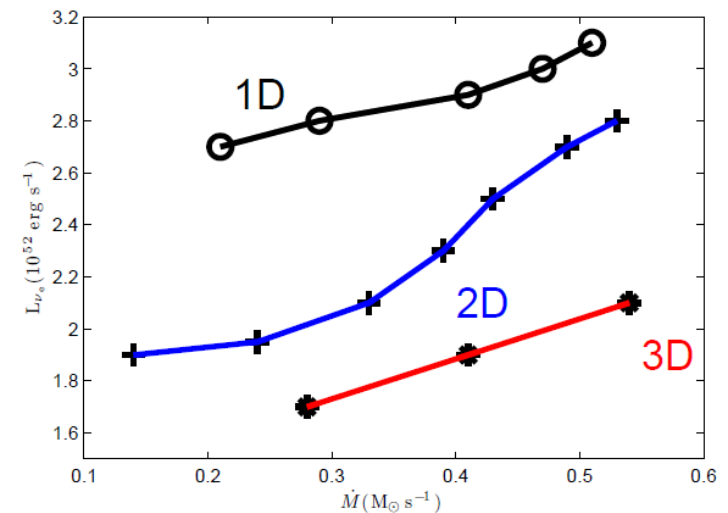
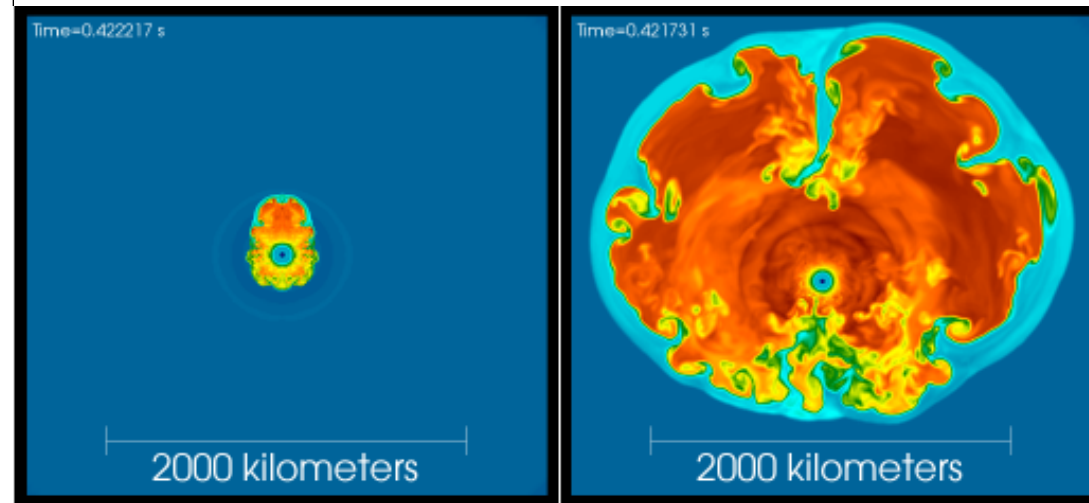
Mass accretion rate

In 2D simulations, the neutrino luminosity required for reviving shock is reduced !



# Is 3D simulation key for successful explosion?

Nordhaus et al. 2010



2D Cylindrical(Left) vs 3D Cartesian

(Right) Gray Luminosity Adaptive mesh refinement is used

**3D simulation require less luminosity compared to 2D!**

Counter argument is presented by Hanke et al 2011. 3D model might not be always good for explosion.

**Under a realistic situation, is 3D good or bad?**

**Anyway... nature is 3D.**

# The feature of our study

- previous works

2D with spectral neutrino transport (Buras 2006, Marek & Janka 2009, Suwa et al. 2010) or

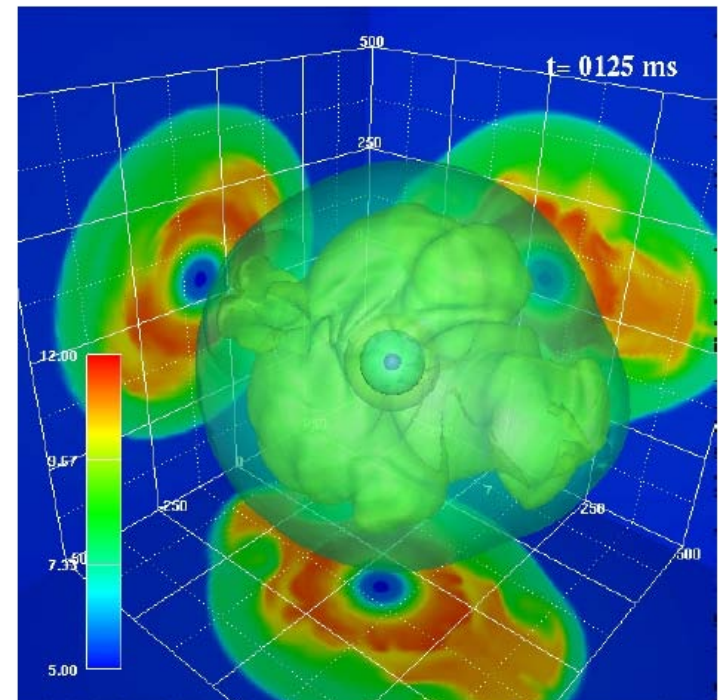
3D with simple assumption of neutrino luminosity (Iwakami et al 2008, Nordhaus et al. 2010)

- this work

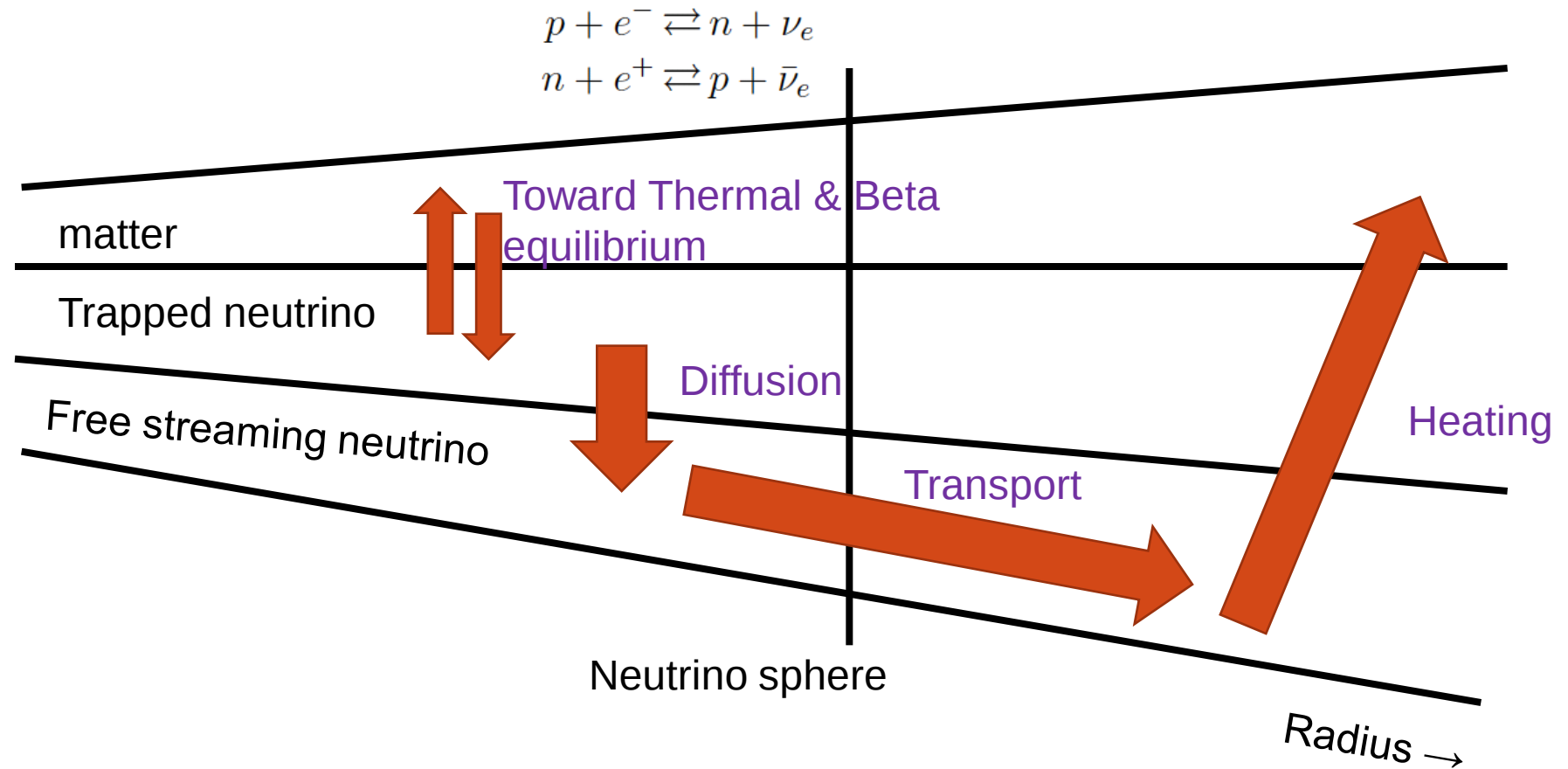
combining with good feature of the previous work,

3D simulation with spectral neutrino transport is presented!

Takiwaki, T., Kotake, K., & Suwa, Y. 2011,  
submitted to ApJ; arXiv:1108.3989



# Neutrino transport, concept



IDSA( isotropic diffusion source approximations)

Dividing neutrino into two parts, trapped and free streaming

For  $v_X$ , simple leakage scheme

# Neutrino transport, trapped part

$$\begin{aligned} \frac{df}{cdt} + \mu \frac{\partial f}{\partial r} + \left[ \mu \left( \frac{d \ln \rho}{cdt} + \frac{3v}{cr} \right) + \frac{1}{r} \right] (1 - \mu^2) \frac{\partial f}{\partial \mu} \\ + \left[ \mu^2 \left( \frac{d \ln \rho}{cdt} + \frac{3v}{cr} \right) - \frac{v}{cr} \right] E \frac{\partial f}{\partial E} \\ = j(1 - f) - \chi f + \frac{E^2}{c(hc)^3} \\ \times \left[ (1 - f) \int R f' d\mu' - f \int R (1 - f') d\mu' \right]. \end{aligned}$$

$f(x, y, z, E, \theta, \phi)$   
6 dimensional variable

## Trapped Particle

### Angular integration

$$\Rightarrow \frac{df^t}{cdt} + \frac{1}{3} \frac{d \ln \rho}{cdt} E \frac{\partial f^t}{\partial E} = j - (j + \chi) f^t - \Sigma.$$

Diffusion term

### Energy integration

$$\begin{aligned} Y^t &= \frac{m_b}{\rho} \frac{4\pi}{(hc)^3} \int f^t E^2 dE d\mu \\ Z^t &= \frac{m_b}{\rho} \frac{4\pi}{(hc)^3} \int f^t E^3 dE d\mu, \end{aligned}$$

$$\begin{aligned} \frac{\partial}{\partial t} (\rho Y^t) + \frac{\partial}{r^2 \partial r} (r^2 v \rho Y^t) \\ = m_b \frac{4\pi c}{(hc)^3} \int [j - (j + \chi) f^t - \Sigma] E^3 dE. \end{aligned}$$

Determined  
parameter for Fermi-  
Dirac distribution  
by Y and Z

$$f_l^t(E) = \{\exp[\beta_l(E - \mu_l)] + 1\}^{-1},$$

# Neutrino transport, free streaming part

$$\begin{aligned} \frac{df}{cdt} + \mu \frac{\partial f}{\partial r} + \left[ \mu \left( \frac{d \ln \rho}{cdt} + \frac{3v}{cr} \right) + \frac{1}{r} \right] (1 - \mu^2) \frac{\partial f}{\partial \mu} \\ + \left[ \mu^2 \left( \frac{d \ln \rho}{cdt} + \frac{3v}{cr} \right) - \frac{v}{cr} \right] E \frac{\partial f}{\partial E} \\ = j(1 - f) - \chi f + \frac{E^2}{c(hc)^3} \\ \times \left[ (1 - f) \int R f' d\mu' - f \int R (1 - f') d\mu' \right]. \end{aligned}$$

$f(x,y,z,E,\theta,\phi)$   
6 dimensional variable

Weak coupling

$$\Rightarrow \frac{\partial \hat{f}^s}{c \partial \hat{t}} + \hat{\mu} \frac{\partial \hat{f}^s}{\partial r} + \frac{1}{r} (1 - \hat{\mu}^2) \frac{\partial \hat{f}^s}{\partial \hat{\mu}} = -(\hat{j} + \hat{\chi}) \hat{f}^s + \hat{\Sigma}.$$

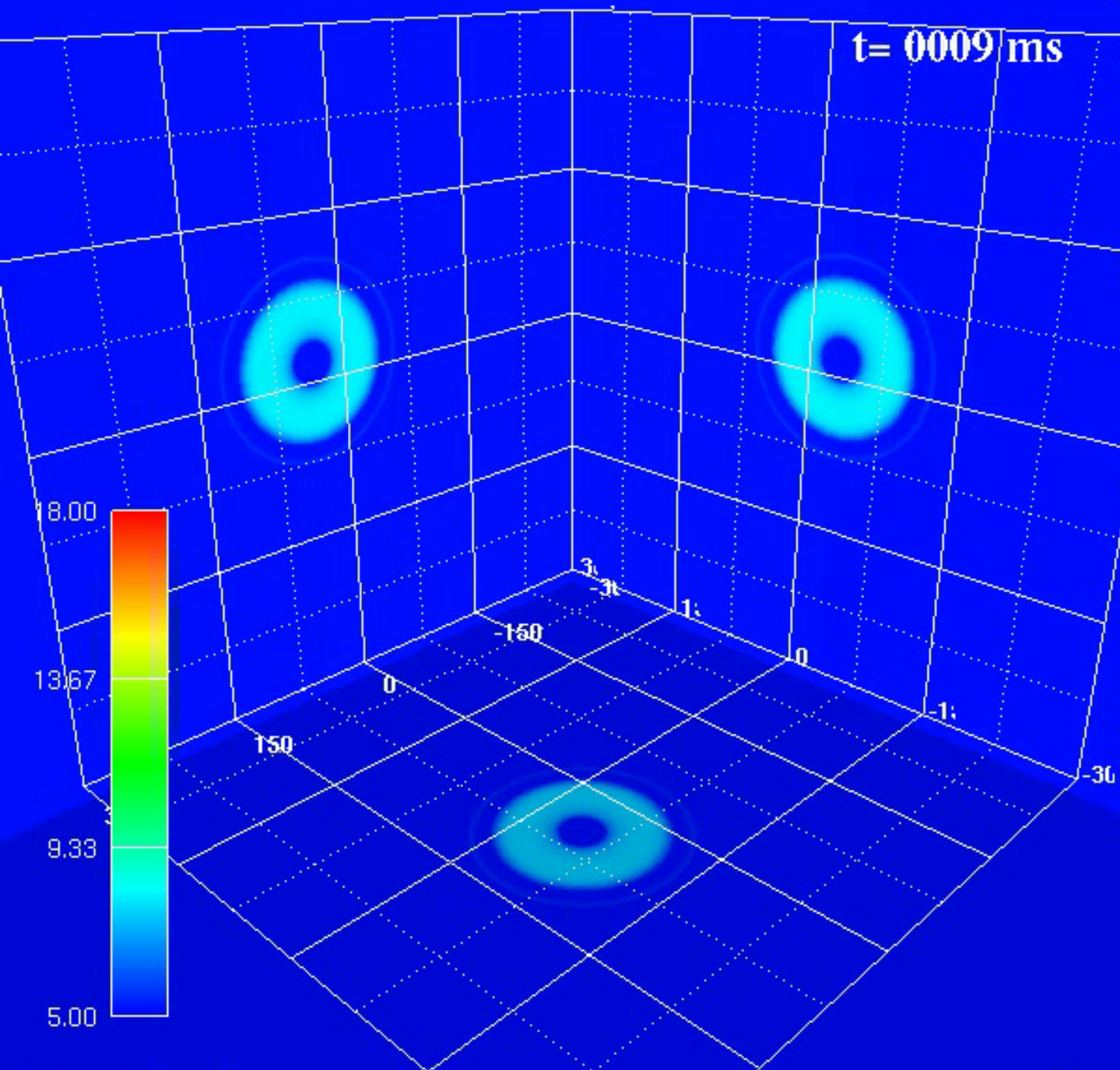
Angular integration is performed.

Different from the original IDSA,

We treat the LHS explicitly and the RHS implicitly.

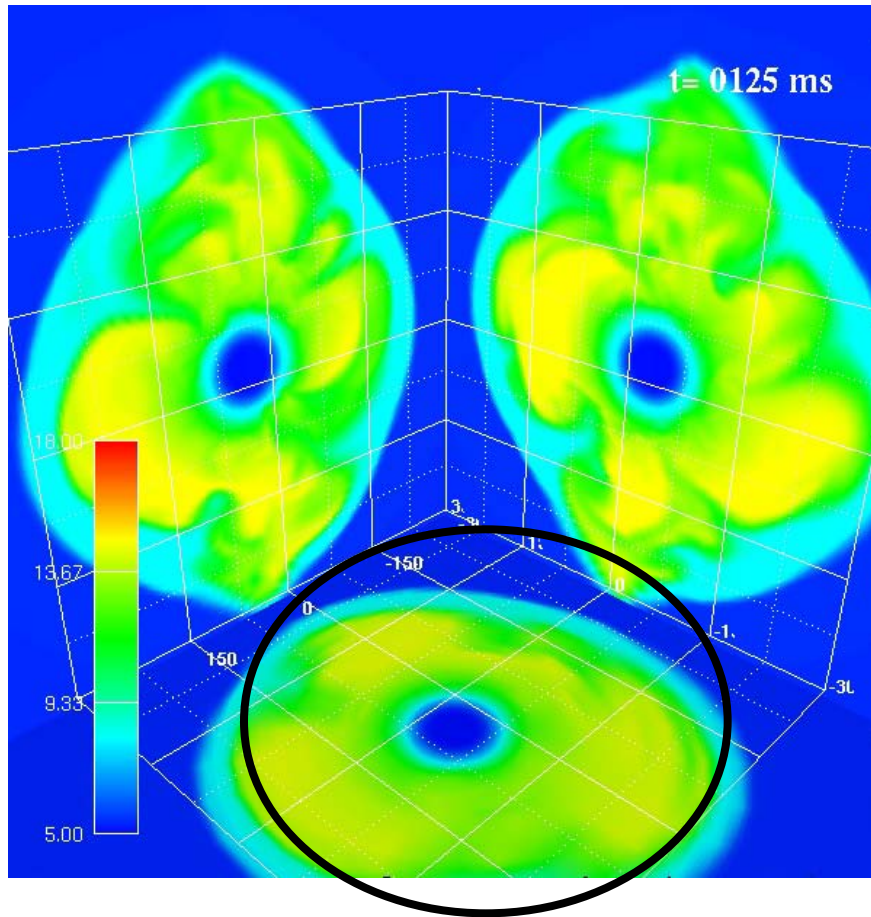


Newton Method is used for solving RHS.  
No message passing during the iteration.

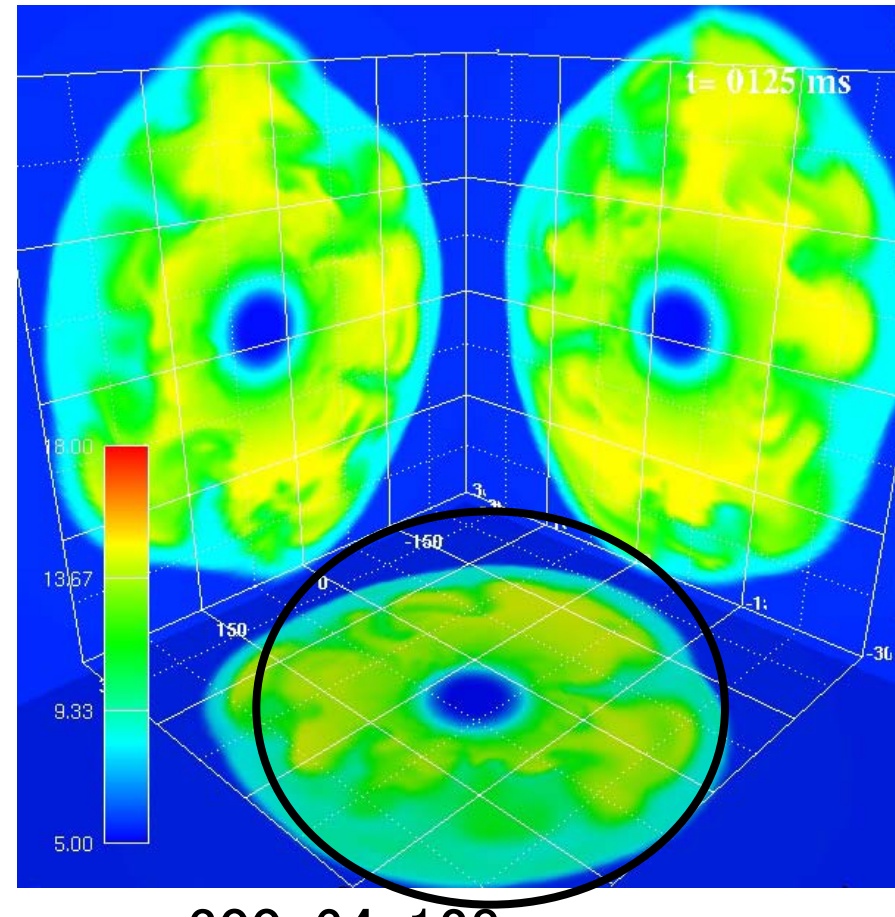


Result!  
11.2M<sub>s</sub>  
LS EOS  
(K=180MeV)

# Difference of Resolution



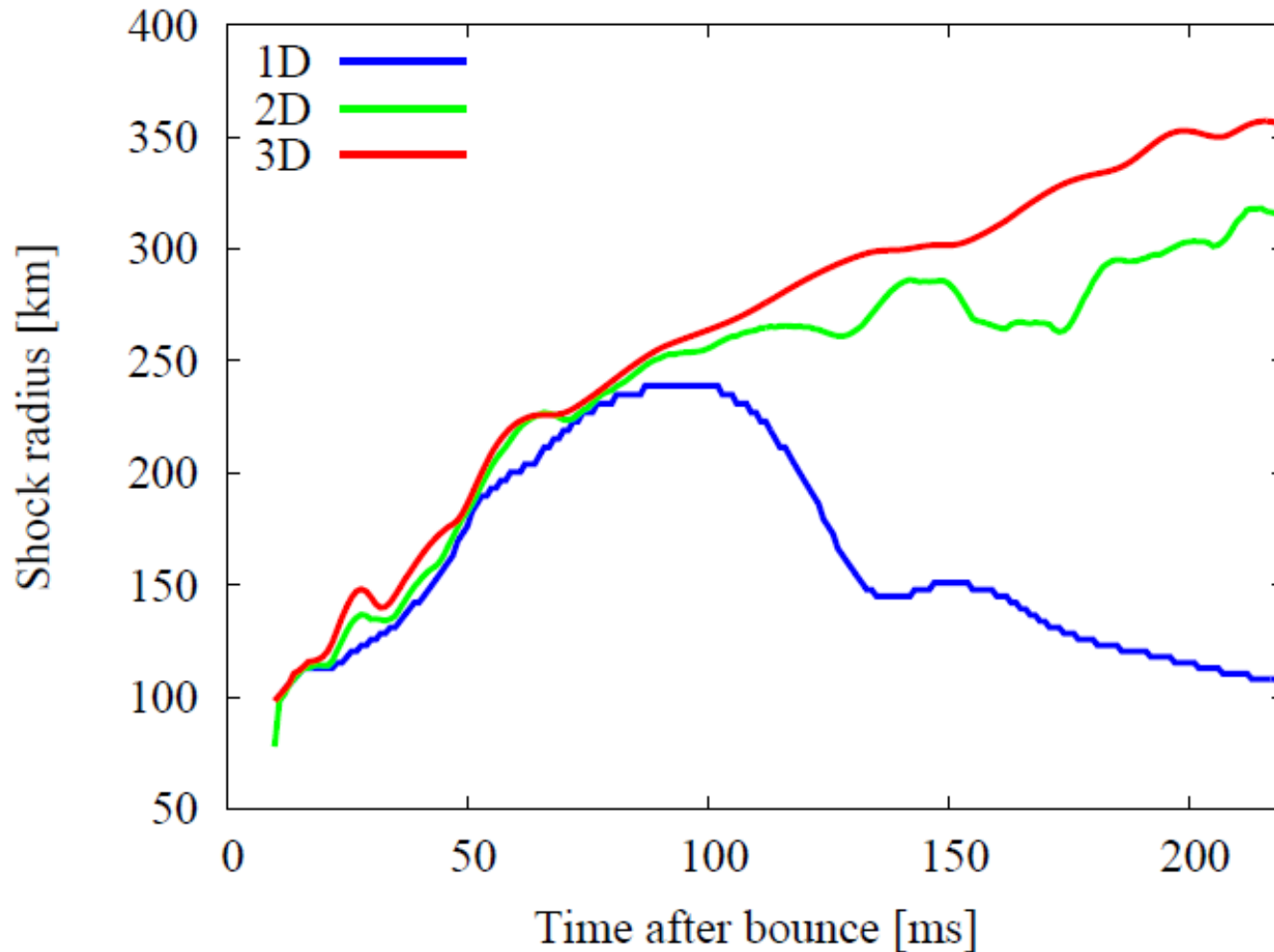
300x64x32



300x64x128

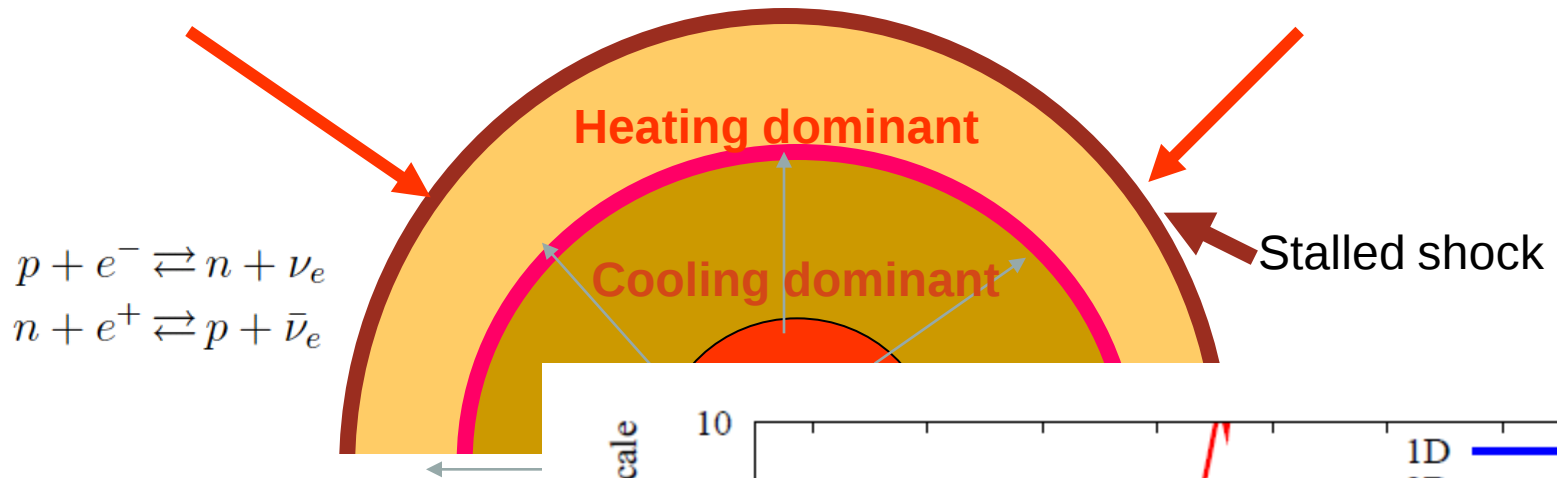
Fine structure inside the shock is produced in high-resolutional model!

# Evolution of Shock



**3D** model is better than **2D** model !

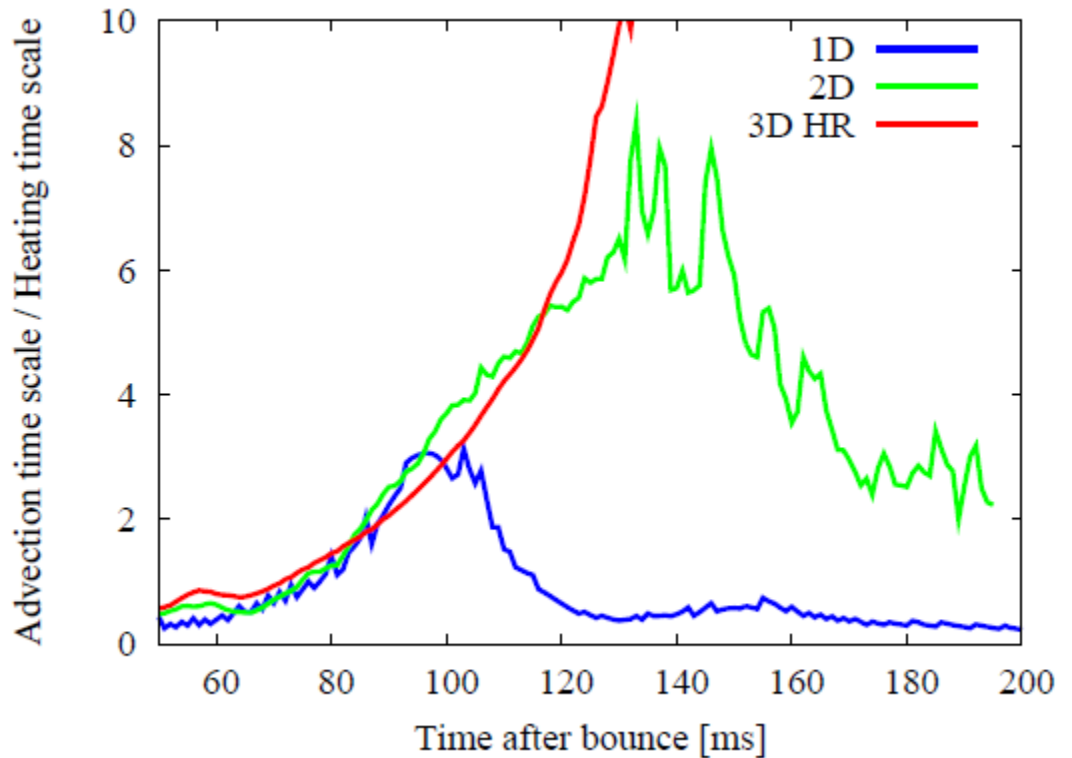
# Advection time vs Heating time



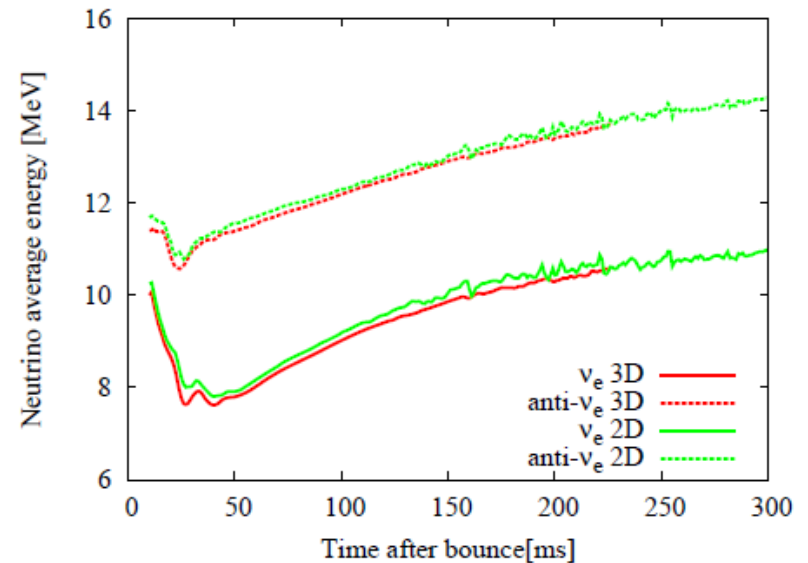
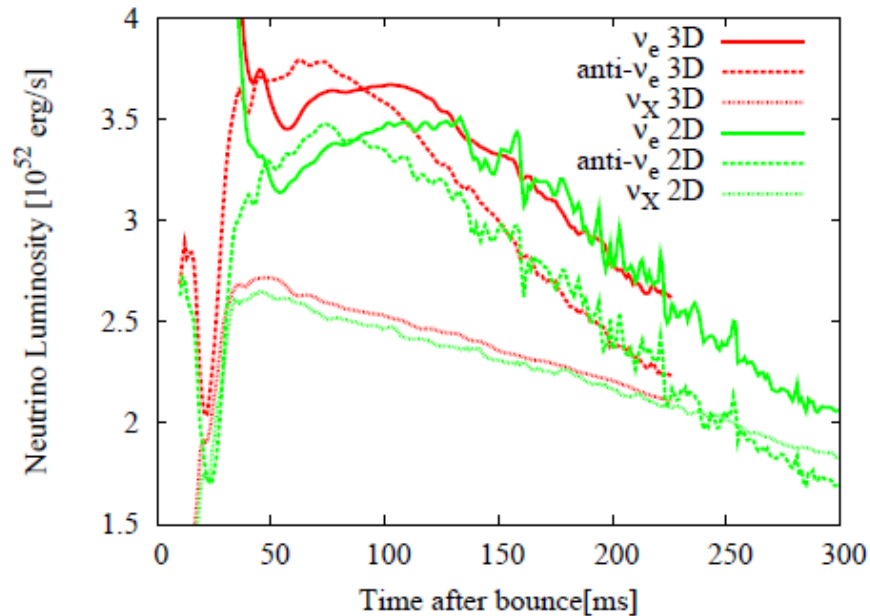
Advection time scale:  
Accreted matter passes heat  
dominant region in this time

$$\tau_{\text{adv}}(t) = - \int_{r_{\text{gain}}(t)}^{r_{\text{sh}}(t)} \frac{1}{v_r(r, t)} dr$$

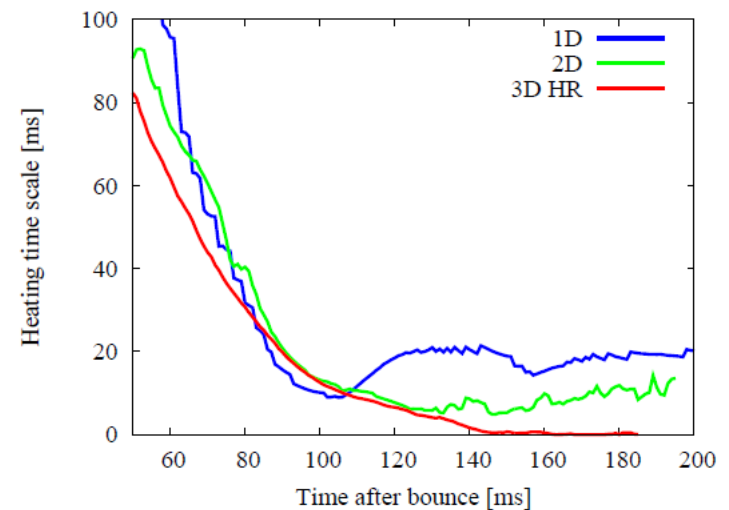
If advection time scale  
explosion will succeed!



# Neutrino Heating

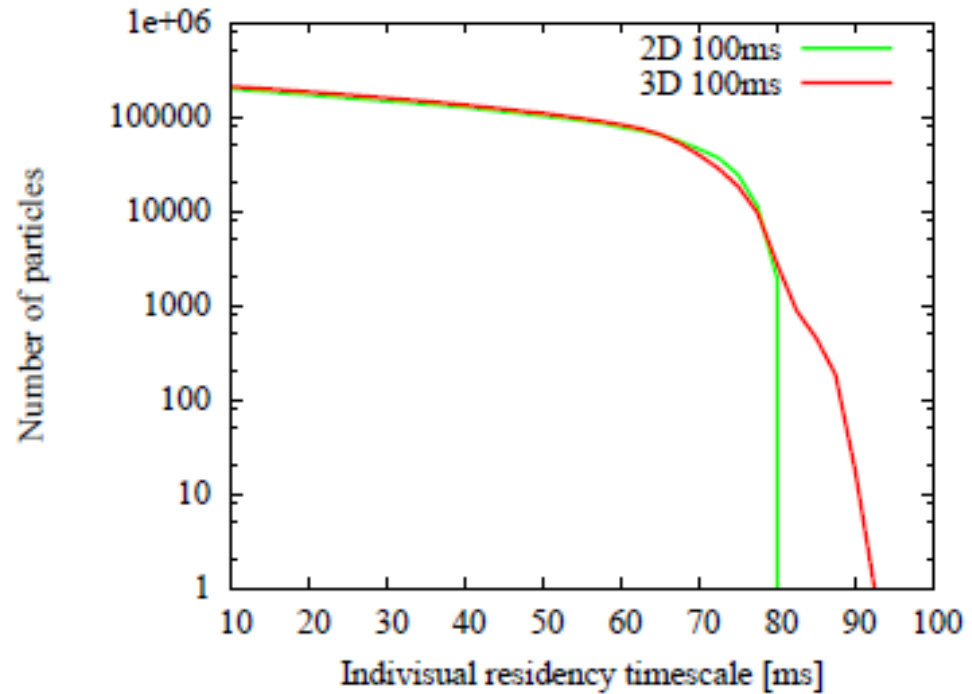
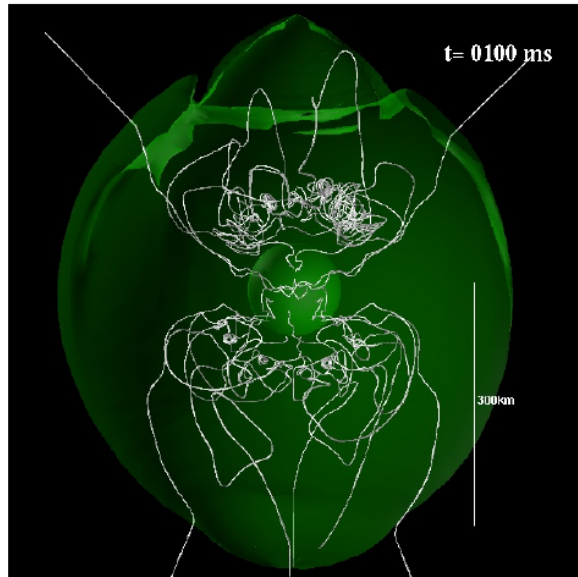


**3D** model is better than  
**2D** model !



# Advection timescale

(Sorry ! This slide is based on the previous work)



**3D** > **2D** ! 3D is good for explosion

(Same analysis should be done at the new work)

# Summary

We perform first 3-dimensional simulation with spectral neutrino transport.

- Advection time scale of **3D model is longer** than that of 2D. 3D is good for explosion.
- Neutrino luminosity of **3D model is bigger** than 2D with same average energy.

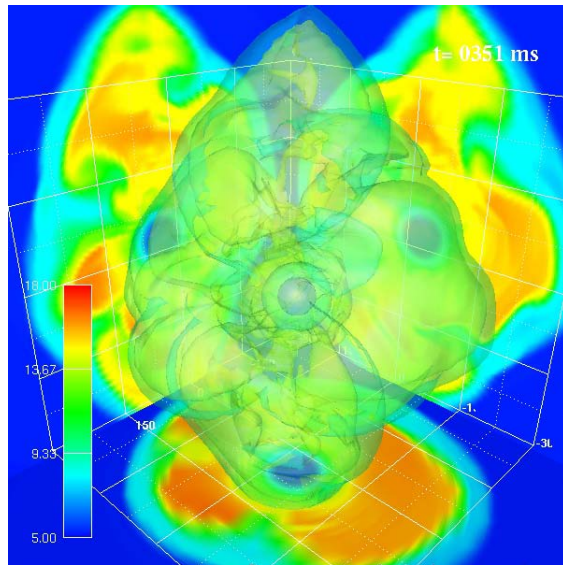
As a result **3D is good** for explosion in this resolution.

3D modeling of supernovae starts Young phase.

I wish this result (or tendency) is confirmed by models with higher resolution, that is computed by K computer.



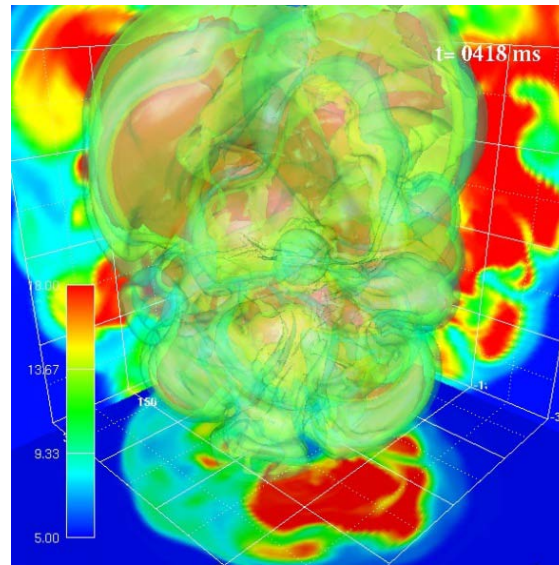
# Simulation with K computer



NAOJ-XT4

300x64x32

256 parallel



T2K-tukuba

320x64x128

4096 parallel



K computer

> 640x128x128

> 16,384 parallel