

Neutrino radiation-hydrodynamics & equation of state



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Brief report on:

- Progress of EOS tables in astrophysics
- 3D neutrino-radiation hydrodynamics



Collaborations on supernova studies

- Quark, Nuclear Physics
 - EOS, ν -reactions

A01, A02

- Massive Star Models
 - Mass, Metallicities

A03

- Simulations of supernovae
 - ν -radiation hydrodynamics

A03

parallel computing
A04

Explosion mechanism

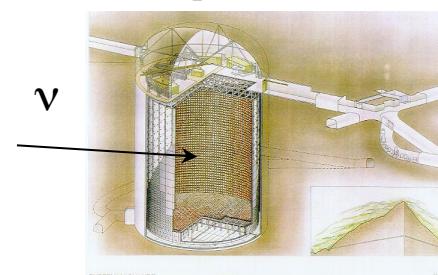


ν

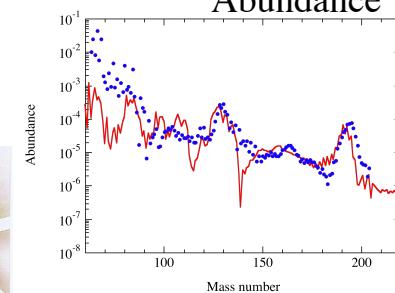
SN1987A

Neutrino Astronomy

Super-Kamiokande



SUPER-KAMIOKANDE INSTITUTE FOR RESEARCH INSTITUTE OF PHYSICS



Progress of EOS tables in astrophysics

- Web pages for EOS table →石塚 12/3
- Nuclear Compositions in supernovae
Furusawa et al. ApJ (2011) →古澤 12/4
- Probe hyperon potential by neutrinos
Nakazato et al. ApJ (2011) accepted
- QCD critical point sweep
Ohnishi et al. Phys. Lett. B (2011) (中里, 大西)

Supernova EOS covering the wide range

- Tables of EOS frequently used
 - Lattimer-Swesty EOS (1991)
• *Skyrme-interaction*
 - H. Shen, Toki, Oyamatsu & Sumiyoshi EOS (1998) **Shen-EOS**
• *Relativistic Mean Field (RMF) approach*

1. Extension to high densities ($\rho > \rho_0 = 0.17 \text{ fm}^{-3}$)

- Hyperons, Quarks
 - *Ishizuka, Nakazato, H. Shen*

Softening of EOS

2. Extension to low densities ($\rho < \rho_0$)

- Mixture of nuclei
 - *Furusawa*

Neutrino reactions

- Nuclear interactions, many body theories
• G. Shen et al. (2011), Hempel et al. (2011)

→富樫 12/3

More massive stars lead to black holes

Fe-core of

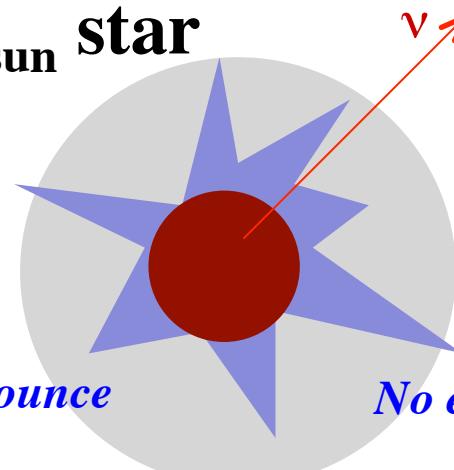
$\sim 40M_{\text{sun}}$ star

Collapse



Core bounce

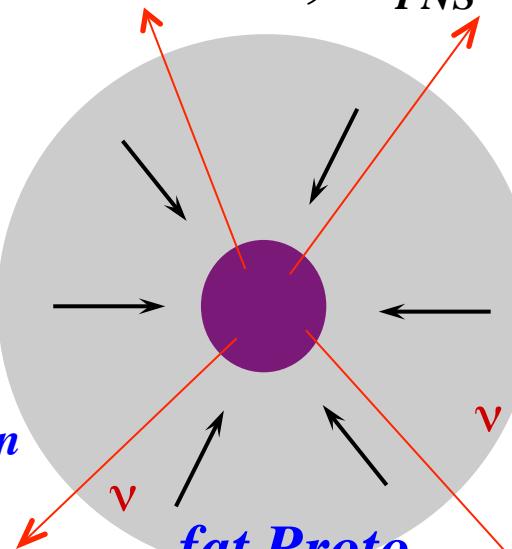
$t=0\text{s}$



$t \sim 0.2\text{s}$

No explosion

Accretion, $M_{PNS} \uparrow$

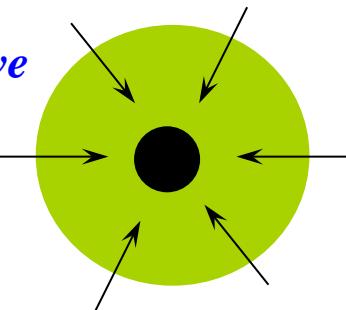


*fat Proto-
neutron star*

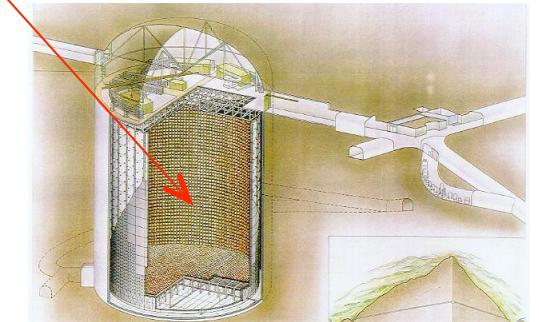
massive

$t \sim 1\text{s}$

Black hole



Super-Kamiokande



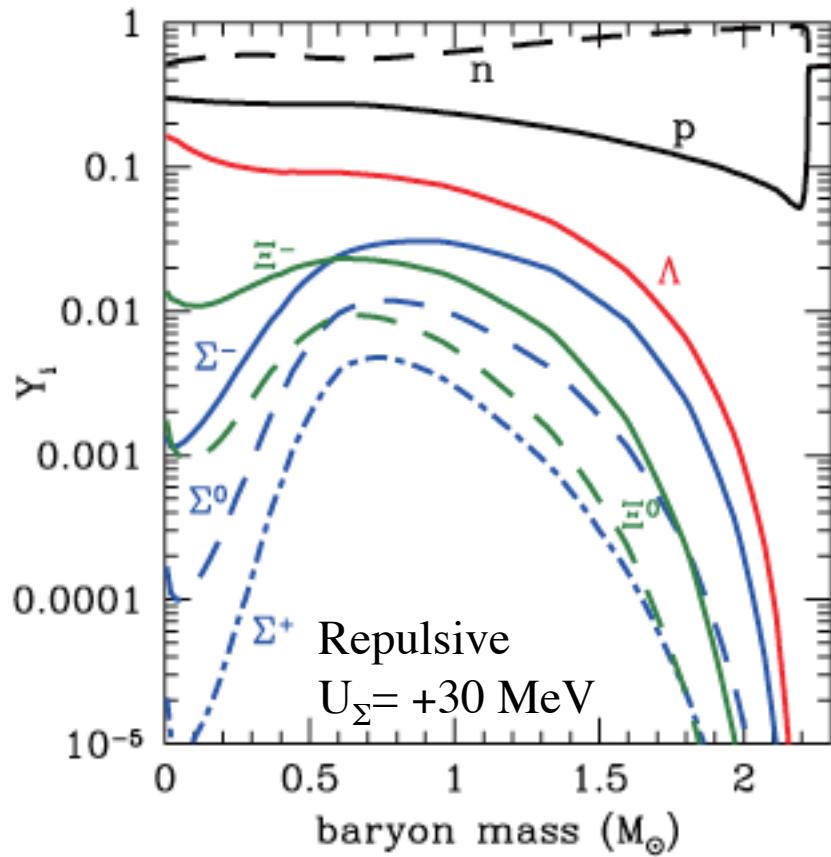
failed supernova ν

- Short duration of neutrino burst:
 - Shen EOS: 1.3s
 - Hyperon EOS: shorter
- Probe of exotic EOS at high ρ and T

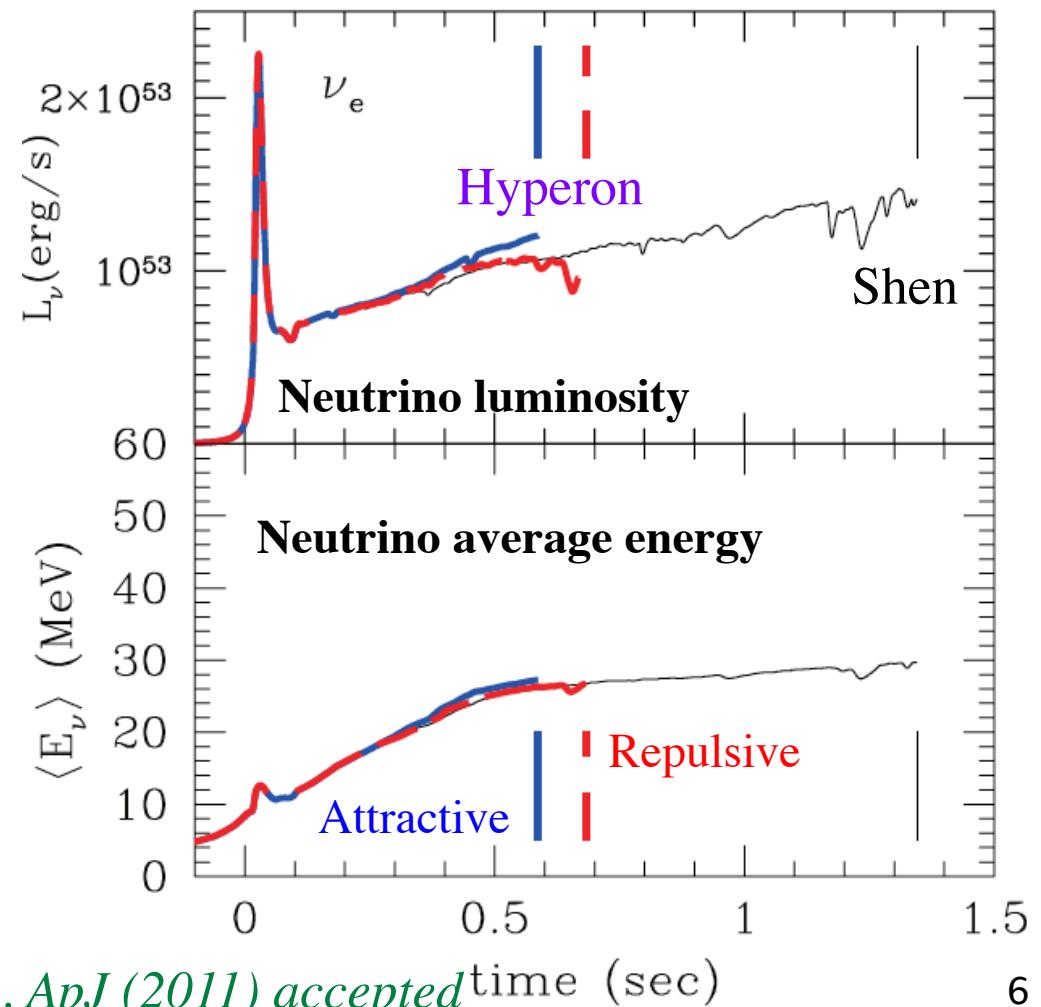
A Galactic case: $10^4 \nu$

Neutrino burst from failed supernovae

- Probe EOS difference due to hyperon potential
 - Repulsive or attractive?: Σ -potential in matter



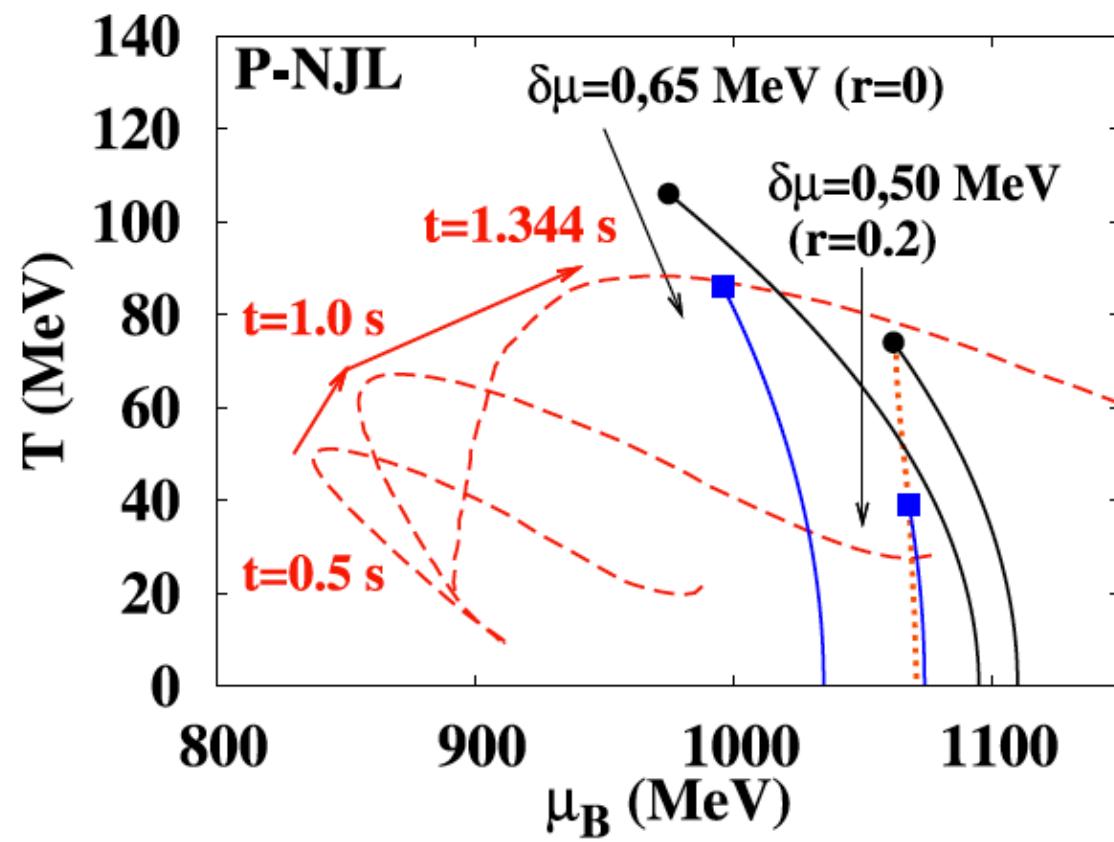
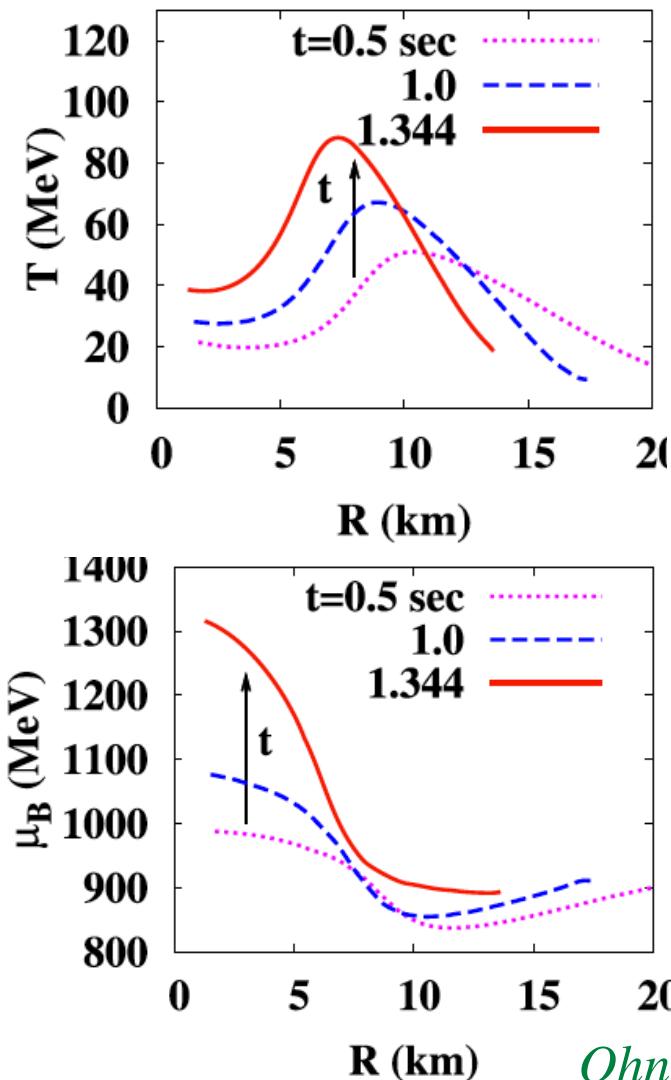
Hyperon mixture
in proto-neutron star



Nakazato et al. ApJ (2011) accepted

Probe of exotic phase during the collapse

- ρ & T sweep critical point / phase boundary



3D neutrino-radiation hydrodynamics

- Code of 3D Neutrino transfer
Sumiyoshi & Yamada, submitted to ApJ (2011)
- Code of Hydrodynamics →長倉 12/5
- Iterative method for matrix →今倉 12/4

Status of neutrino radiation-transfer

- *Affect neutrino heating for explosion*

- 1D: first principle calculations

- 2D, 3D: approximate treatment

- Ray-by-ray (Radial transport only)

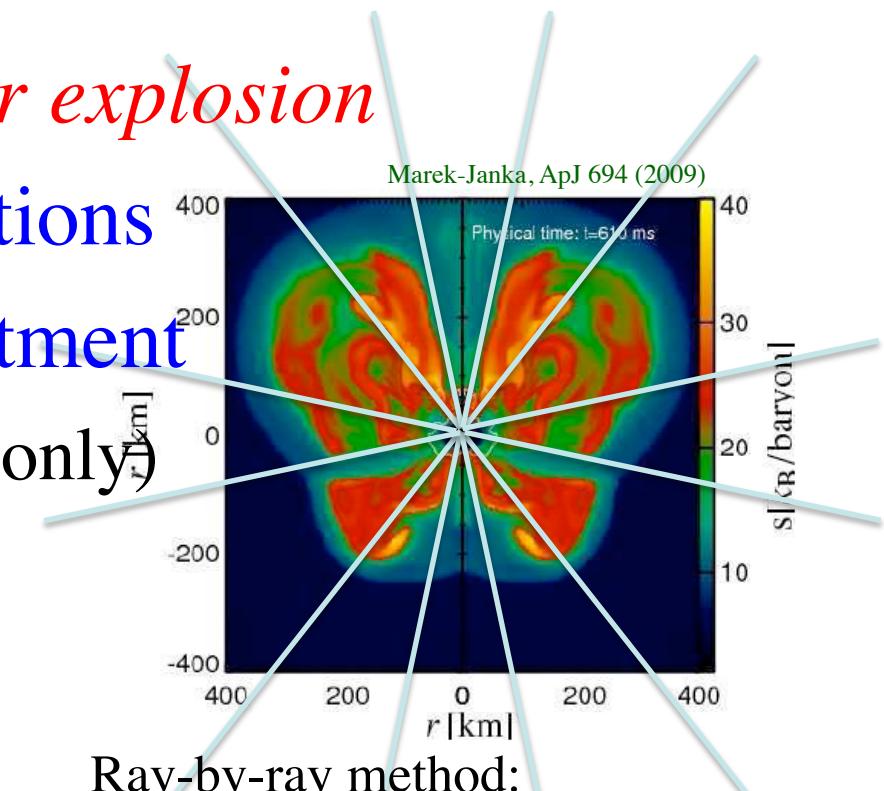
Neglect lateral transport

- Need full 3D calculations

- New code to solve 3D neutrino-transfer

- For the first time in the world

- Applications to supernova cores



Ray-by-ray method:
Solve 1D-transport Independently

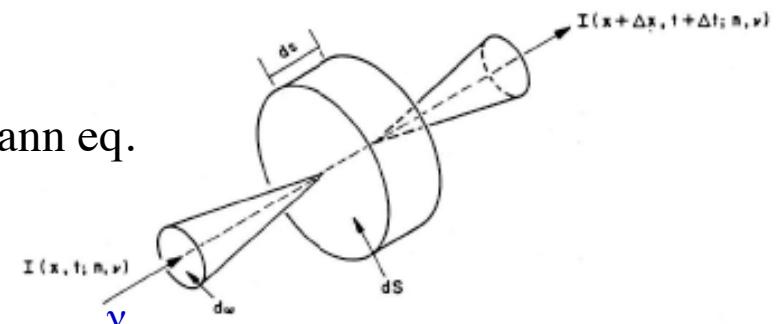
*Sumiyoshi & Yamada,
submitted to ApJ
(2011)*

To solve Neutrino transfer in 3D

- Time evolution of 6D-distribution

$$\frac{1}{c} \frac{\partial f_\nu}{\partial t} + \vec{n} \cdot \vec{\nabla} f_\nu = \frac{1}{c} \left(\frac{\delta f_\nu}{\delta t} \right)_{\text{collision}}$$

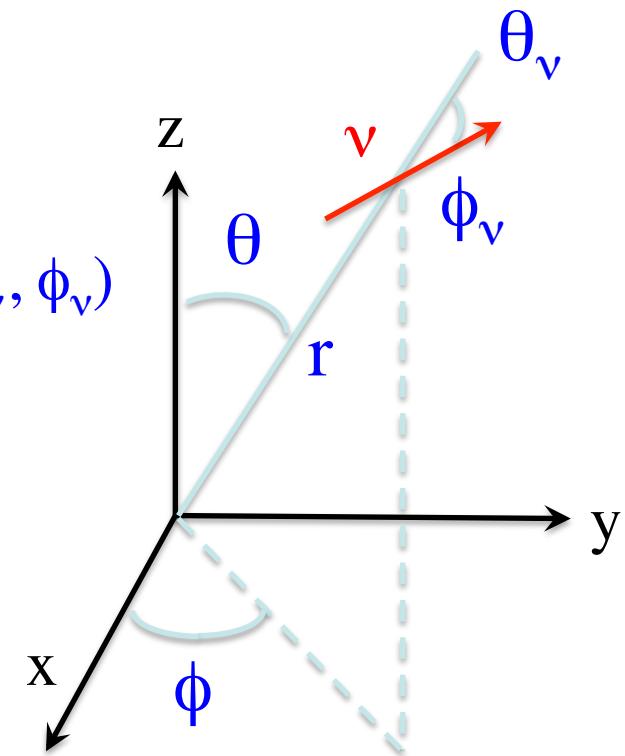
Boltzmann eq.



- Left: Neutrino number change
- Right: Change by neutrino reactions

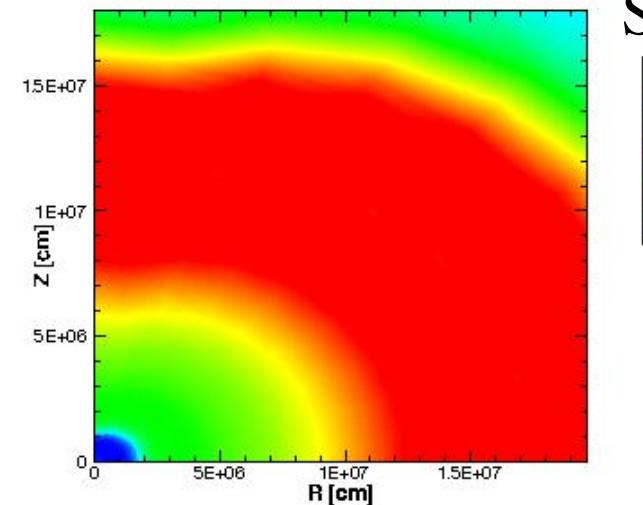
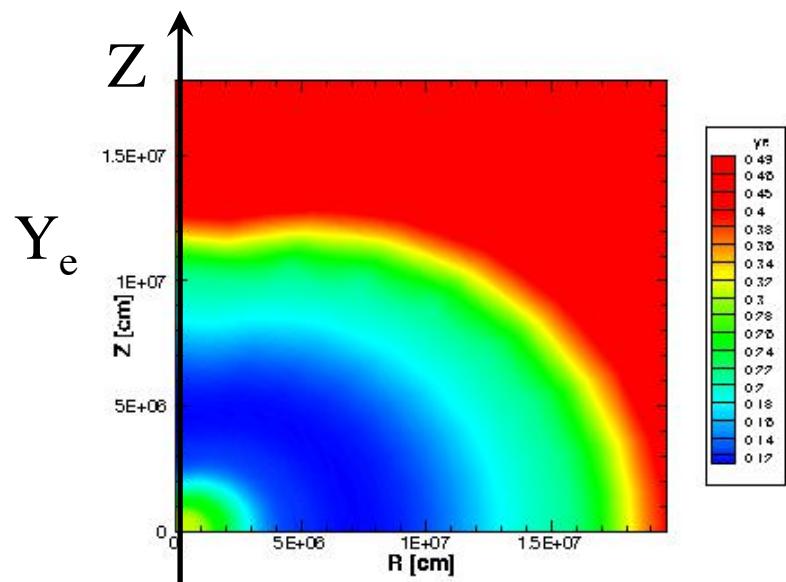
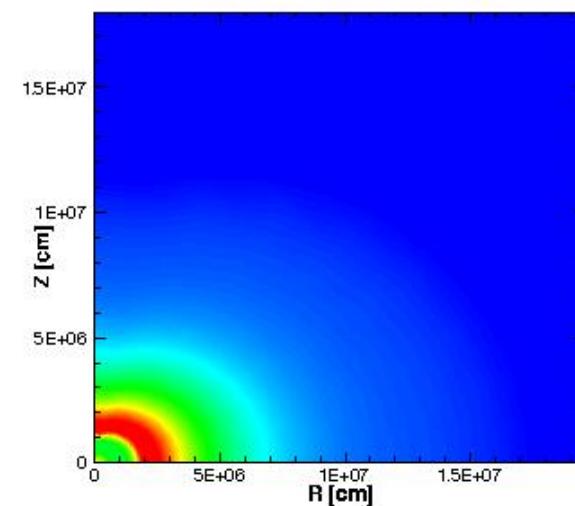
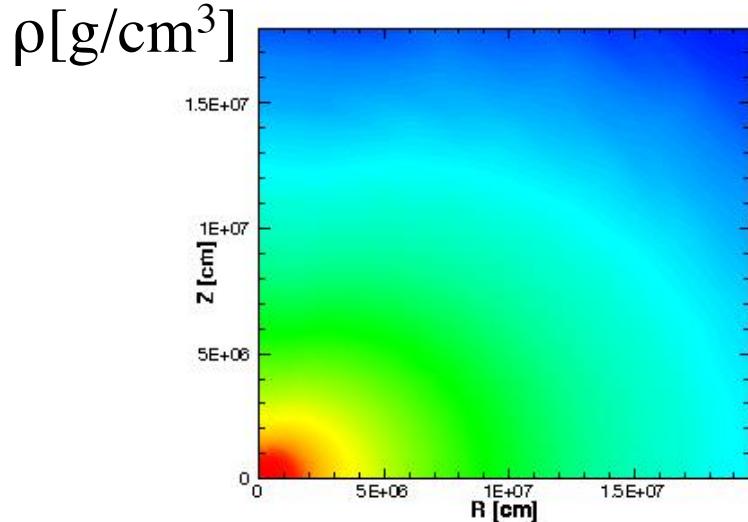
$$f_\nu(r, \theta, \phi; \epsilon_\nu, \theta_\nu, \phi_\nu; t)$$

- Neutrino energy (ϵ_ν), Neutrino angle (θ_ν, ϕ_ν)
 - 3D in spherical symmetry ($r, \epsilon_\nu, \theta_\nu$)
 - **Neutrino reactions, EOS table**
- Code: finite differencing, implicit
 - Linear eq. with large sparse matrix



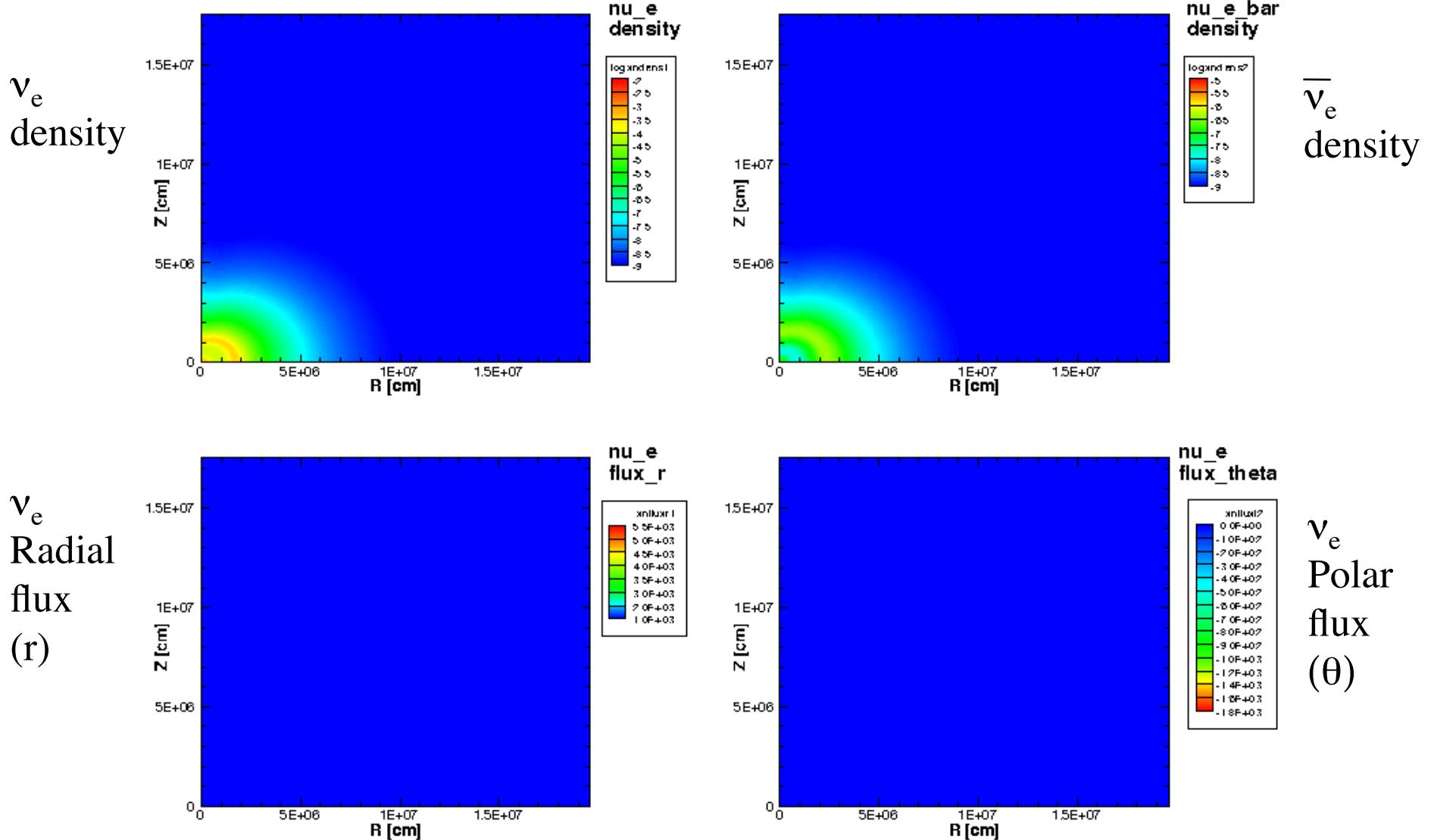
Axially symmetric supernova core

- Fix the ρ , T , Y_e profile & Solve 3D v -transfer



Axially symmetric supernova core

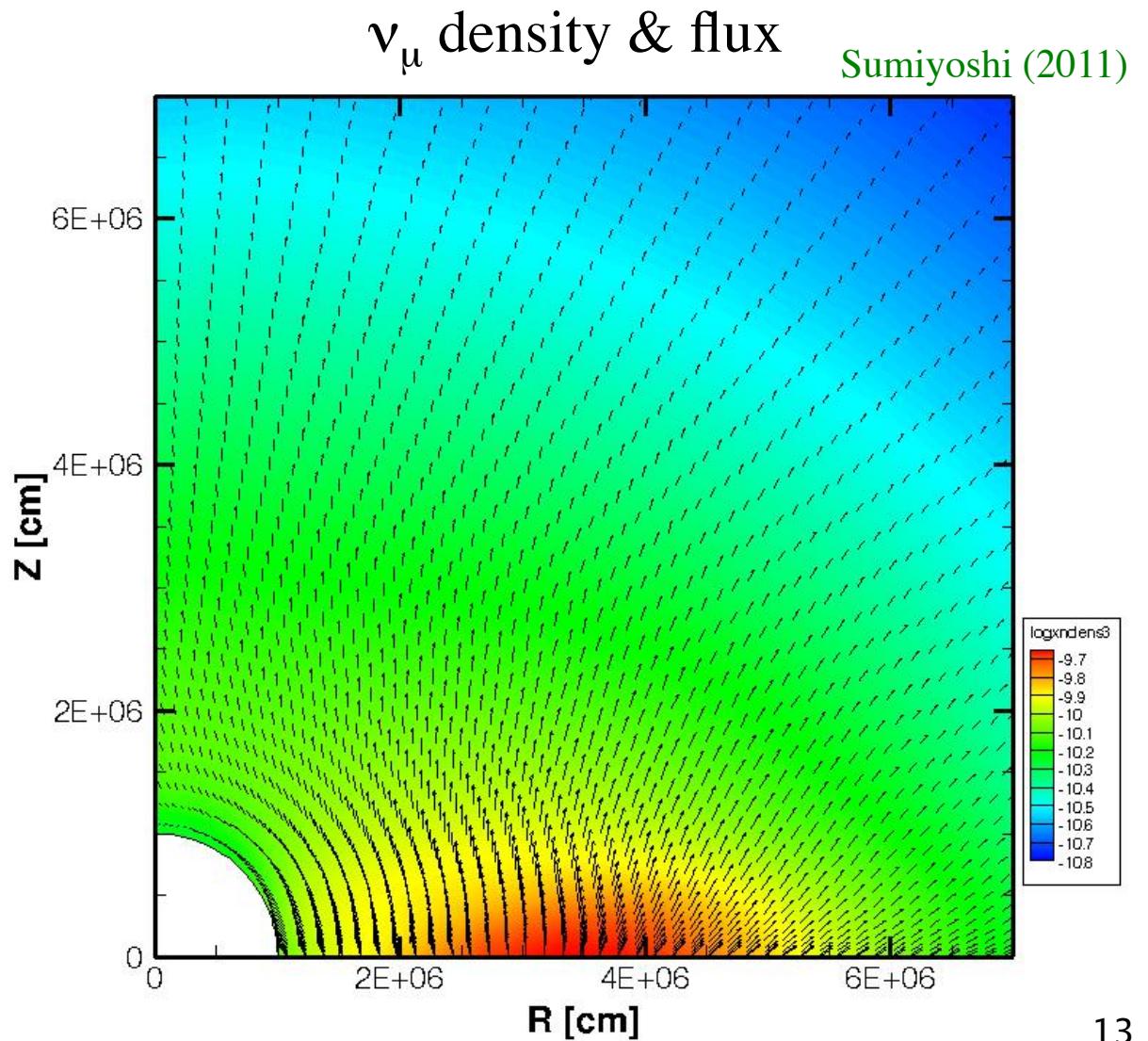
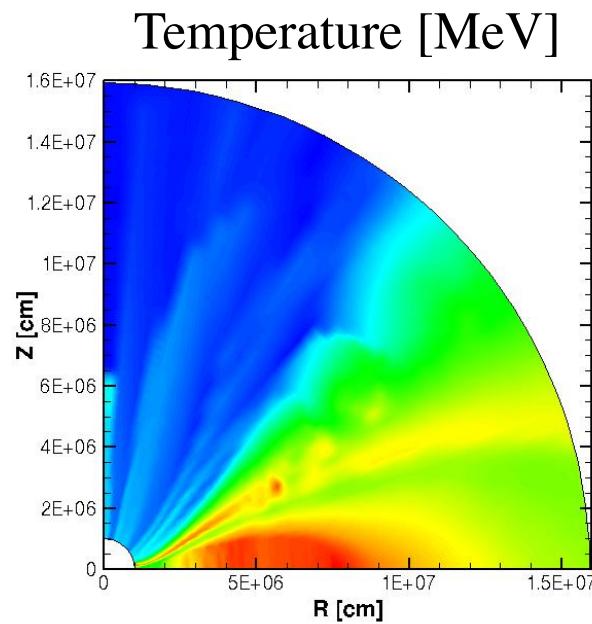
- From small densities, the time evolution until the stationary state



Accretion disk around BH in collapsar

From Sekiguchi (2011)

- Polar flux of thermal neutrinos from disk



Preliminary

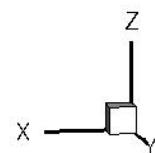
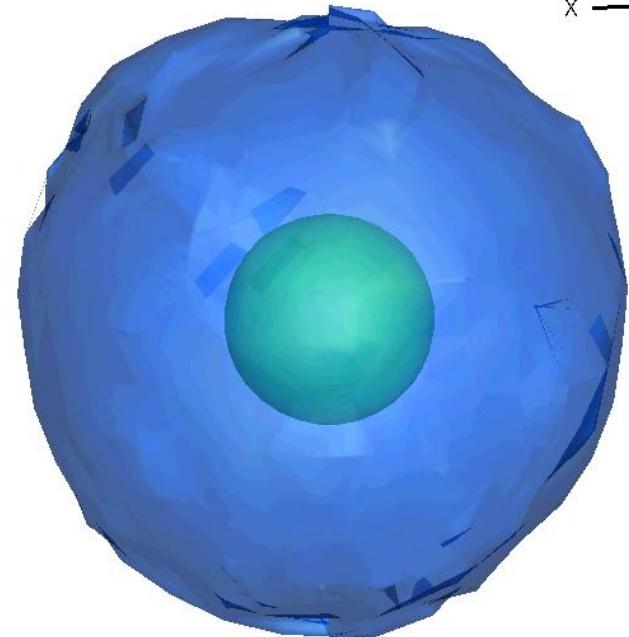
3D supernova core after bounce

From Takiwaki (2011)

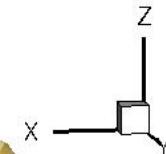
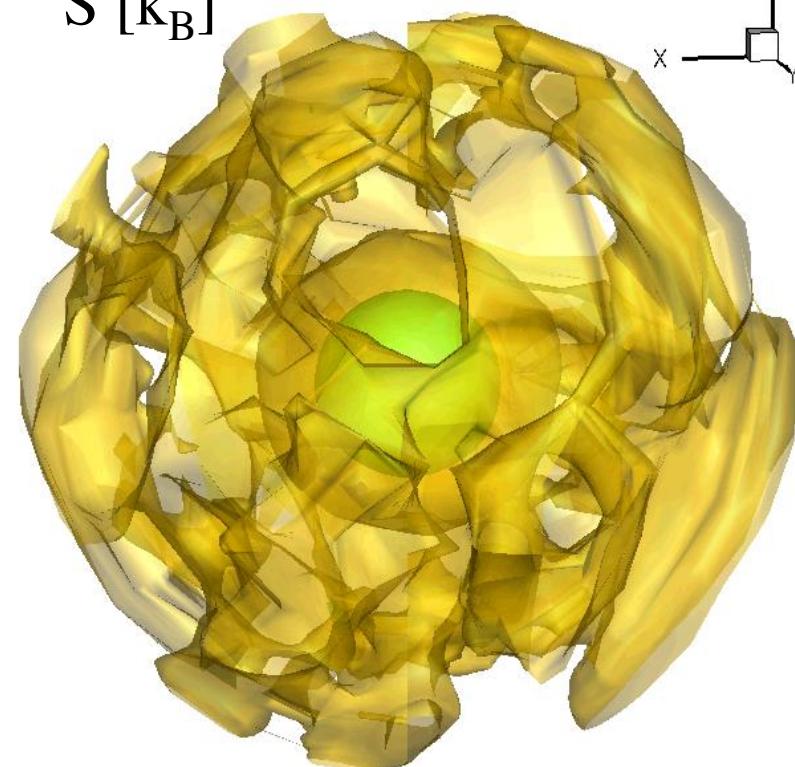
- Fix the ρ , T , Y_e profile & Solve 3D v -transfer

Iso-Surface

ρ [g/cm³]



S [k_B]



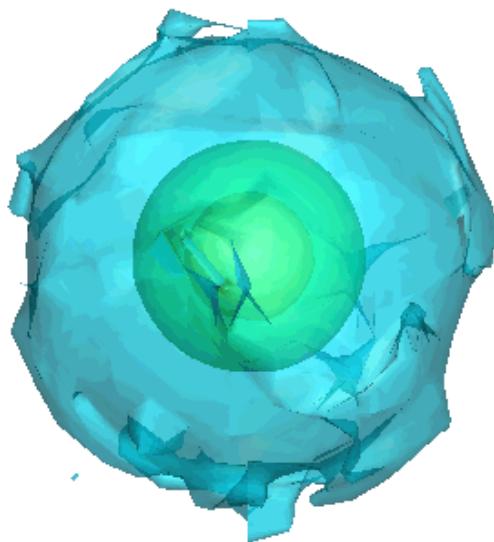
~ 200 km

t=197ms

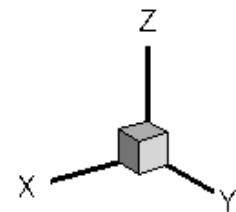
Time evolution of neutrino transfer in 3D

- Emitted neutrinos diffuse out and propagate

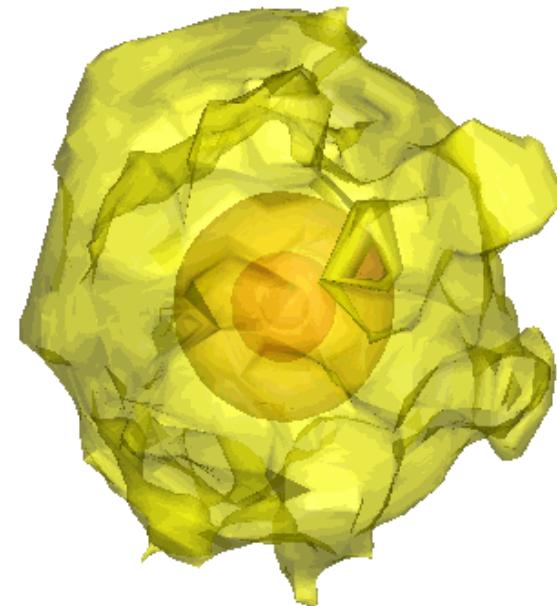
ν_e
density
Iso-Surface



$t=0\sim 0.2\text{ms}$



$\bar{\nu}_e$
density



Preliminary

Development of 3D ν -transfer hydro. code

- 3D-neutrino transfer code: completed
 - Neutrino-reactions, EOS tables: implemented
 - Diffusion, free-streaming tests: checked
 - 1D profile, 2D, 3D formal solution: checked
- Study 3D neutrino-transfer for static profile
 - Applications to 2D, 3D profiles
 - Polar, azimuthal fluxes, beyond diffusion
- MPI parallel version: done by Matsufuru
- Matrix inversion improvement by Imaoka
 - Need further optimizations to large systems
- Coupling with hydrodynamics by Nagakura

Thanks for collaboration with

- Supernova research
 - S. Yamada
 - K. Nakazato
 - H. Suzuki
 - H. Kikuchi
- RMF-EOS table
 - H. Shen
 - K. Oyamatsu
 - H. Toki
- Extension of EOS table
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 - T. Sakurai
- Numerical simulations
 - H. Nagakura
 - T. Takiwaki
 - K. Kotake
 - Y. Sekiguchi
- Many body theory
 - M. Takano
 - H. Togashi and others



World's No.1 on TOP500 List

*Supercomputing resources at KEK, YITP,
UT, RCNP, NAOJ, JAEA*

Core-collapse supernovae is one of
the target simulations on K-computer